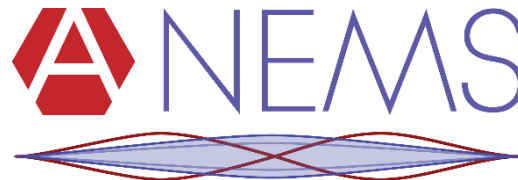


LESSON 5 – MEMS Resonators

Prof. G. Villanueva

Advanced NEMS Lab (ANEMS)

EPFL-IGM NEMS



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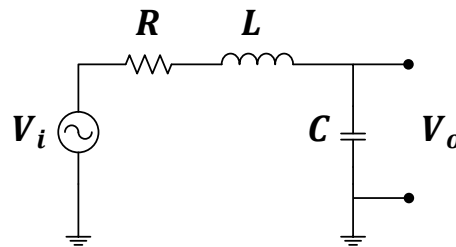
Dates	Lectures	Lecturers	Mean
20.02	Introduction	D. Briand / G. Villanueva	Live
	Transducers review: pre-recorded lectures		
27.02	Sensors part I	D. Briand	Live
	Exercices		
05.03	Sensors part II	D. Briand	Live
	Industrial seminar #1		
12.03	Students presentations	D. Briand / G. Villanueva	Live
19.03	Actuators and Optical MEMS	D. Briand	Live
	Industrial seminar #2		
26.03	Acoustic and Ultrasonic MEMS	G. Villanueva	Live
	Industrial seminar #3		
09.04	Acoustic and Ultrasonic MEMS	G. Villanueva	Live
16.04	RF-MEMS NEMS	G. Villanueva	Live
23.04	Interactive session	D. Briand / G. Villanueva	Live
30.04	Thermal and gas sensors	D. Briand	Live
	Industrial seminar #4		
07.05	Packaging	D. Briand	Live
14.05	Packaging	D. Briand	Live
	Industrial seminar #5		
21.05	PowerMEMS	D. Briand	Live
28.05	Quiz + oral exam instructions	All	Live
	Evaluation of the course		

- **Introduction**
 - What is a Resonator?
 - Different applications
 - Why MEMS resonators?
 - Market perspectives
- **Types of MEMS resonators**
- **MEMS filters (passive)**
- **MEMS oscillators (active)**

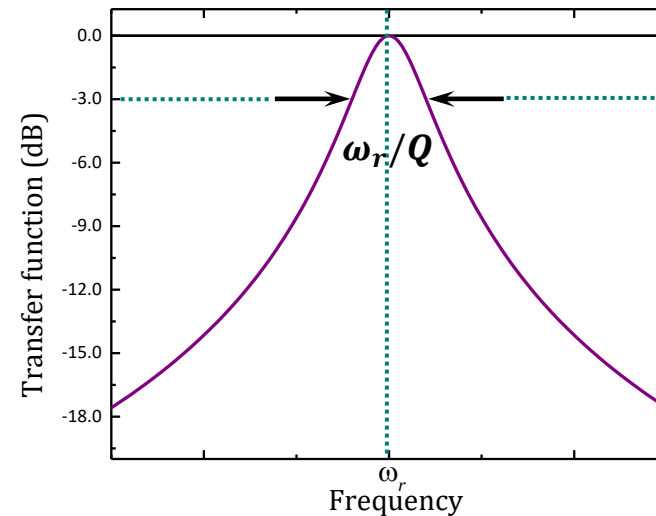
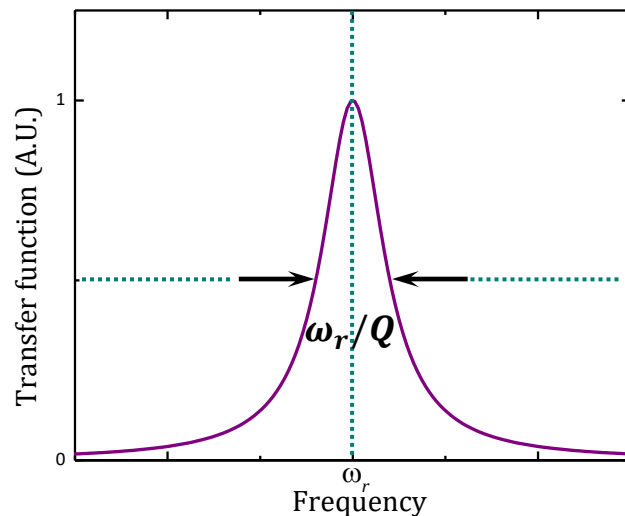
- Wikipedia says...

System that tends to oscillate with greater amplitude at some frequencies than at others

...and Wikipedia is usually right.



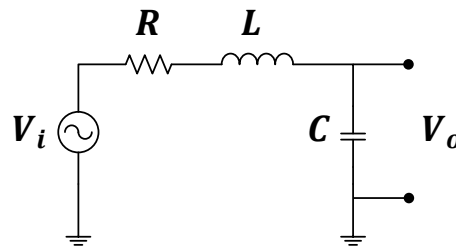
$$S_{21} = \left| \frac{V_o}{V_i} \right|^2 = \frac{1}{(1 - (LC\omega)^2)^2 + (\omega RC)^2}$$
$$= \frac{1}{\left(1 - \left(\frac{\omega}{\omega_r}\right)^2\right)^2 + \left(\frac{\omega}{\omega_r Q}\right)^2}$$



- Wikipedia says...

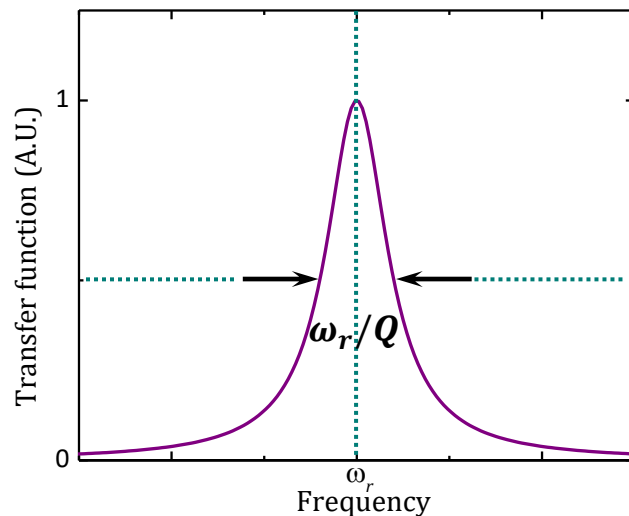
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$$S_{21} = \left| \frac{V_o}{V_i} \right|^2 = \frac{1}{(1 - (LC\omega)^2)^2 + (\omega RC)^2}$$

$$= \frac{1}{\left(1 - \left(\frac{\omega}{\omega_r}\right)^2\right)^2 + \left(\frac{\omega}{\omega_r Q}\right)^2}$$



- Q* - Quality factor**

- *Measure of how good/bad a resonator is*
- $Q = 2\pi \frac{E_{\text{stored}}}{E_{\text{lost}}}$; $Q = \frac{\omega_r}{FWHM}$; $Q = \frac{S_{21}(\omega_r)}{S_{21}(\omega=0)}$
- *Establishes level of interaction with the “outside”*

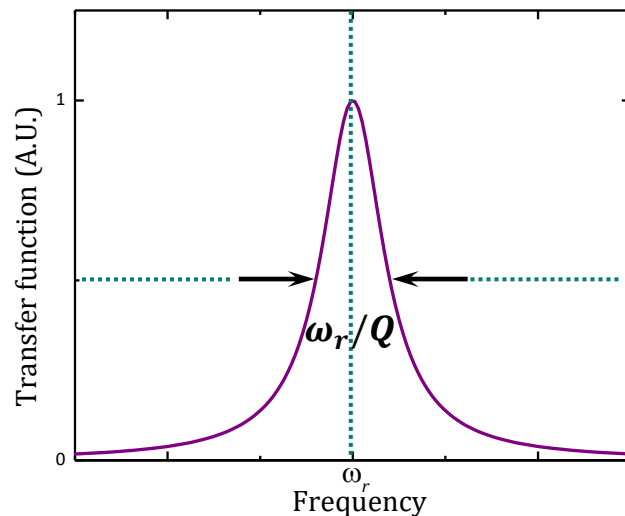
- It depends on the application
- Trade-off
 - Less influence from external noise
 - Time required to settle down the transients
 - Every mechanical structure has resonances

$$\tau \sim 2\pi \frac{Q}{\omega_r}$$

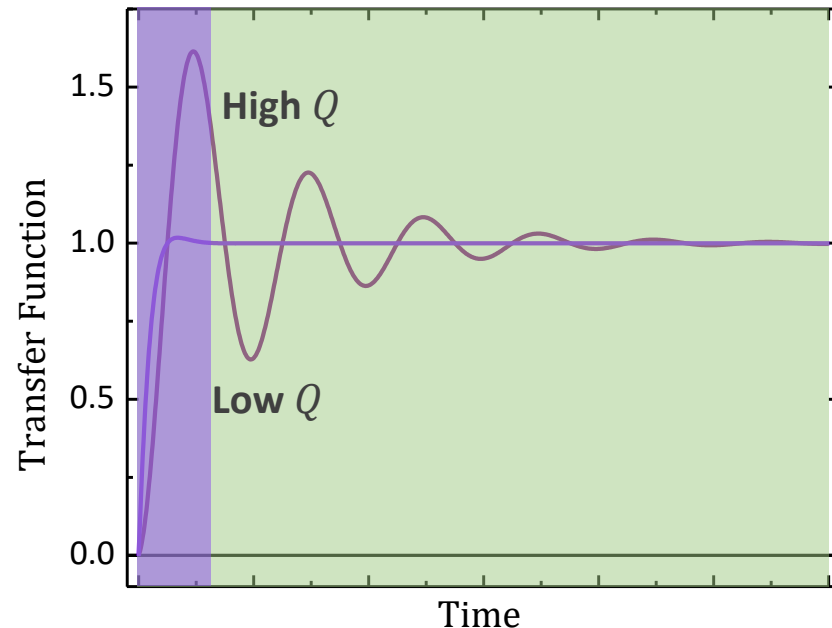


If your application “resonates” – then better as high as possible

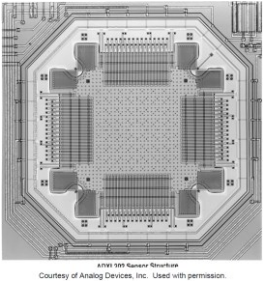
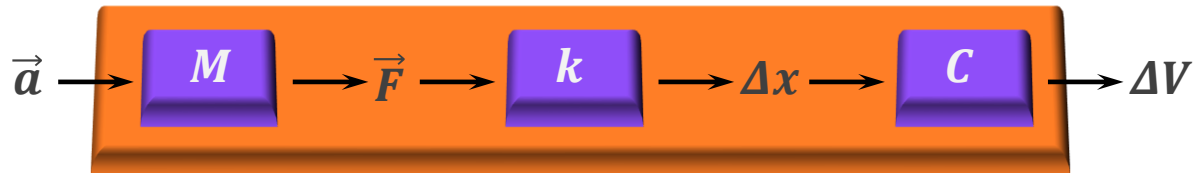
↓
Resonator



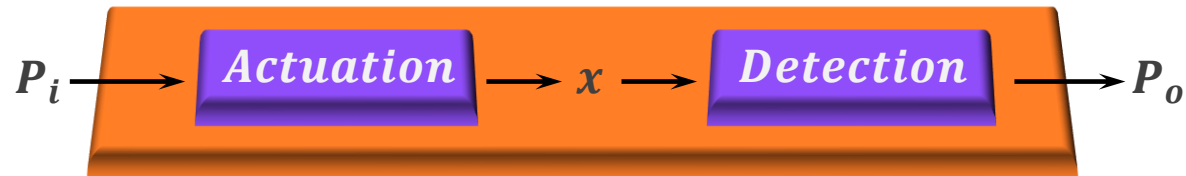
Response to a stepped stimulus



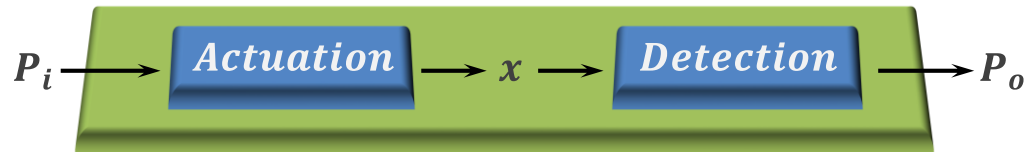
Accelerometer (DC)



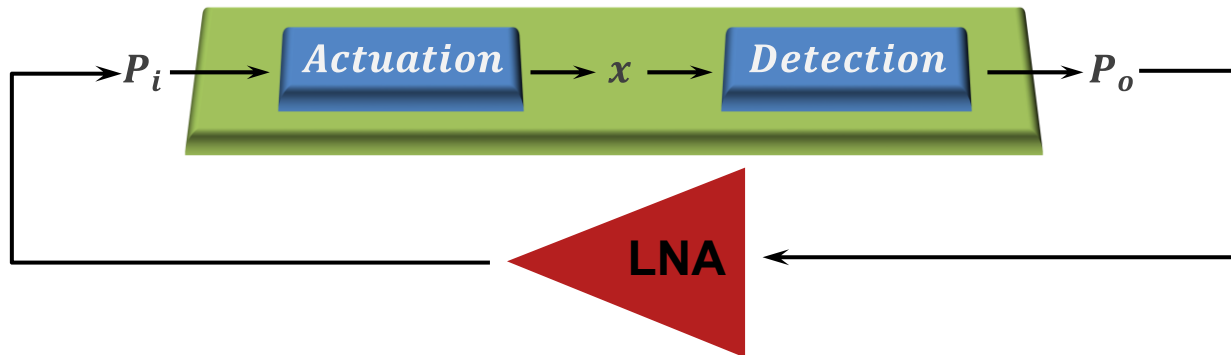
MEMS Resonator



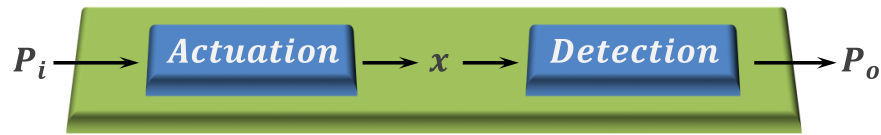
RF Filter



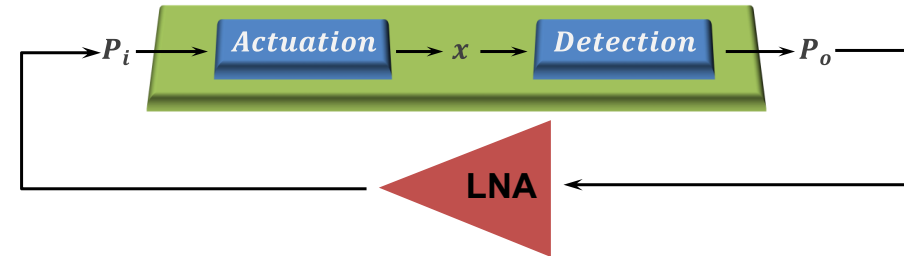
Oscillator



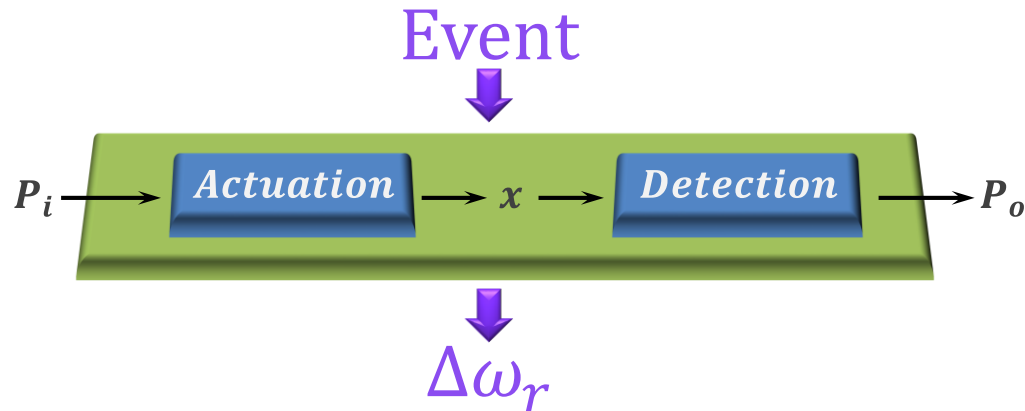
RF Filter



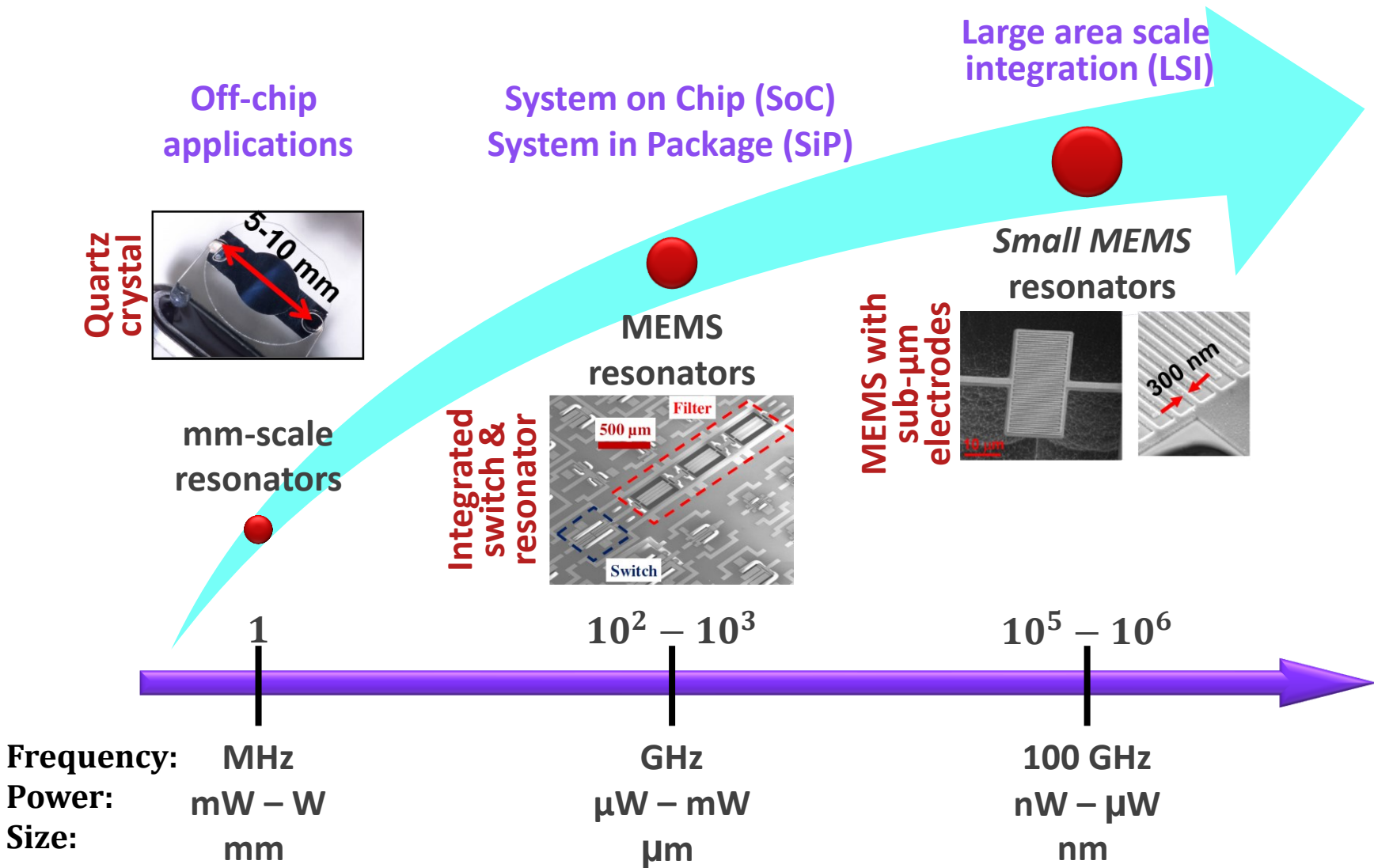
Oscillator



Resonant sensor

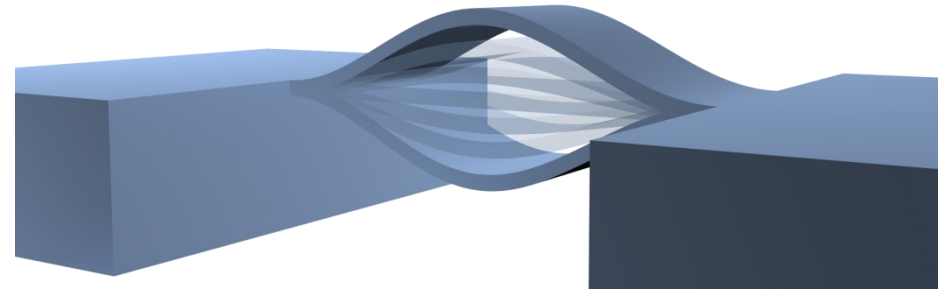
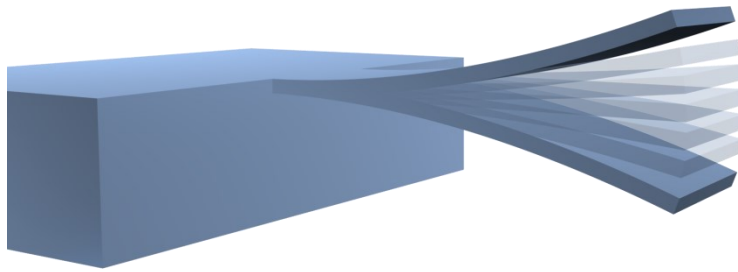


What kind of event could it be?



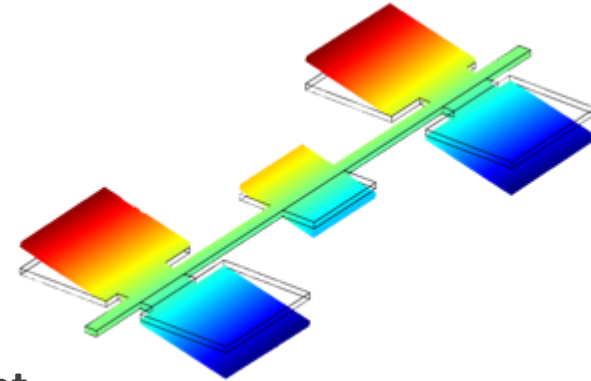
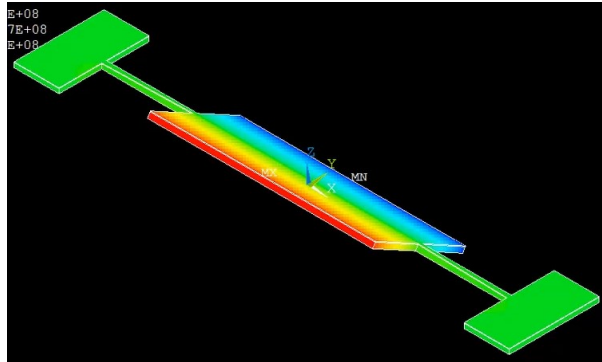
Source: Prof. G. Piazza

TYPES OF MEMS RESONATORS



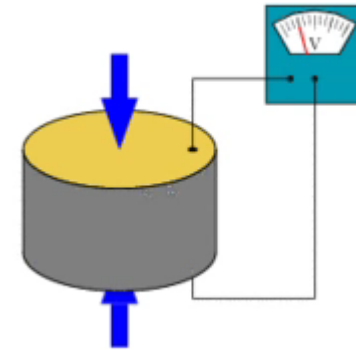
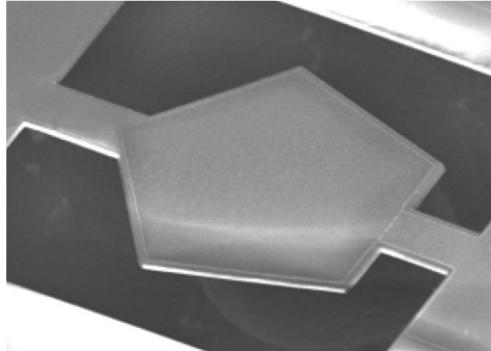
- Bending of mechanical structures is involved
- 1D: cantilevers (C-F), beams (C-C), free-free (F-F); 2D: membranes (CCCC), plates (CFFF)
- Equation of motion is a 4th order differential equation
 - Solution is a combination of trigonometric and hyperbolic functions
- *Typical frequencies: 10kHz – 100MHz*
- *Applications: Low frequency oscillators, sensors*
- *Advantages:*
 - Intuitive and clear understanding of motion
 - Low mass – preferred for sensing
- *Disadvantages: gas or liquid damping is very important*

$$f \propto \sqrt{\frac{E}{\rho} \frac{t}{L^2}}$$



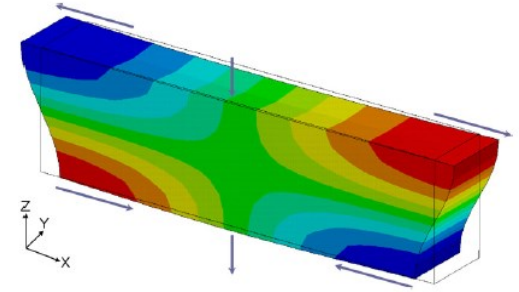
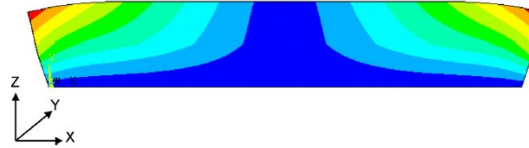
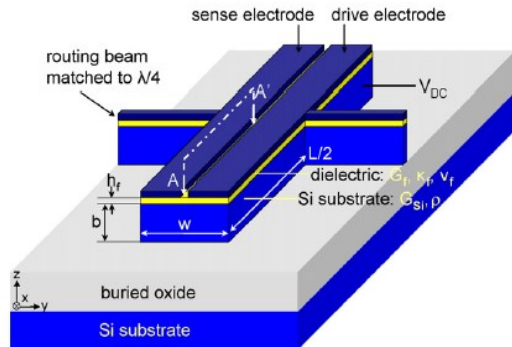
- Motion based on torsion, torque-based movement
- Usually paddle-like structures
- Equation of motion is a 2nd order differential equation
 - Solution is a combination of trigonometric functions
- *Typical frequencies: 10kHz – 10MHz*
- *Applications: Low frequency oscillators, sensors*
- *Advantages:*
 - Intuitive and clear understanding of motion
 - Low interaction with substrate (thin supporting rods)
- *Disadvantages: very fragile and costly to fabricate (very thin rods)*

$$f \propto \sqrt{\frac{G}{\rho}} \sqrt{\frac{t^3}{L_r L_p W_p^3}}$$



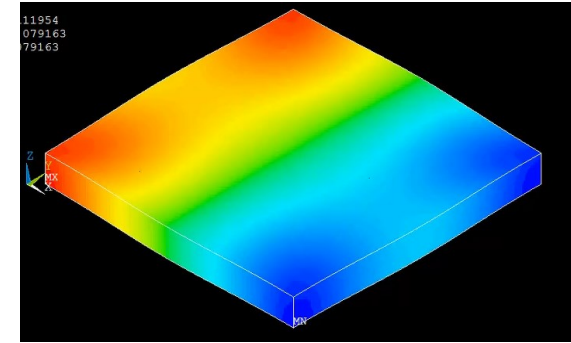
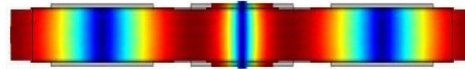
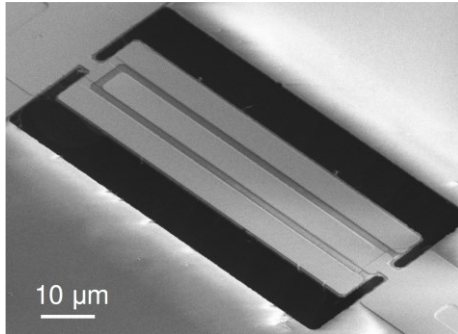
- Acoustic waves constructive interaction
- Movement is 3D (due to Poisson's ratio) – Reduced to 1D if $w > t$
- Equation of motion is a 2nd order differential equation – wave equation
 - Solution is a trigonometric function, Frequencies are multiples
- Typical frequencies: 100MHz – 10GHz
- Applications: Filters, Oscillators
- Advantages:
 - High frequency, high Q
 - Easy electromechanical modelling
- Disadvantages:
 - Complicated design (to trim properties)
 - One frequency per wafer

$$f \propto \sqrt{\frac{E n}{\rho t}}$$



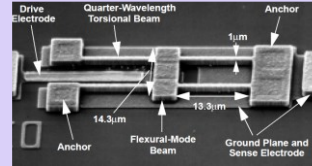
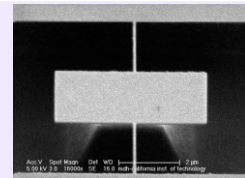
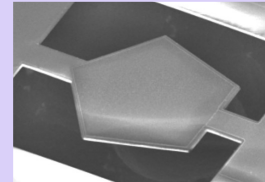
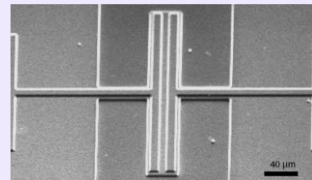
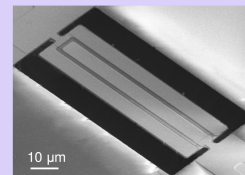
- **Acoustic waves constructive interaction**
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- **Equation of motion is a 2nd order differential equation – wave equation**
 - Solution is a trigonometric function, Frequencies are multiples
- *Typical frequencies: 100MHz – 10GHz*
- *Applications: Filters, Oscillators*
- *Advantages:*
 - High frequency, high Q
 - Easy electromechanical modelling
- *Disadvantages:*
 - Complicated design (to trim properties)
 - Even less intuitive than previous one

$$f \propto \sqrt{\frac{G n}{\rho t}}$$



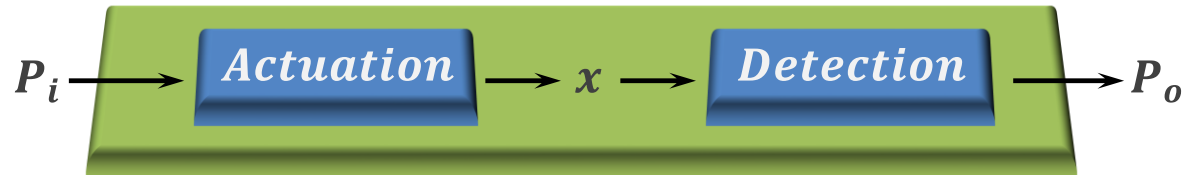
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 - Solution is a trigonometric function, Frequencies are multiples
- Typical frequencies: 100MHz – 10GHz
- Applications: Filters, Oscillators
- Advantages:
 - Frequency defined by lithography, high frequency, high Q
 - Easy electromechanical modelling
- Disadvantages:
 - Complicated design (to trim properties)

$$f \propto \sqrt{\frac{E}{\rho} \frac{n}{w}}$$

Type	Frequency		Example
Flexural	$f \propto \sqrt{\frac{E}{\rho} \frac{t}{L^2}}$	100 kHz – 100 MHz	
Torsional	$f \propto \sqrt{\frac{G}{\rho}} \sqrt{\frac{t^3}{L_r L_p W_p^3}}$	10 kHz – 10 MHz	
Thickness	$f \propto \sqrt{\frac{E n}{\rho t}}$	100 MHz – 10 GHz	
Shear	$f \propto \sqrt{\frac{G n}{\rho t}}$		
Lateral	$f \propto \sqrt{\frac{E n}{\rho w}}$		

$$Q = 2\pi \frac{E_{stored}}{E_{lost}}$$

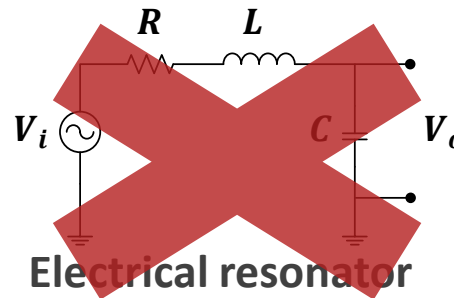
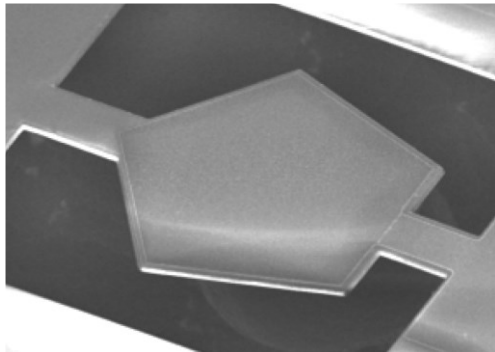
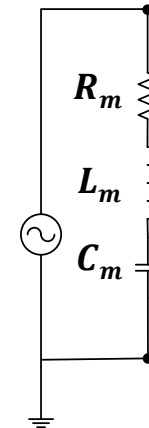
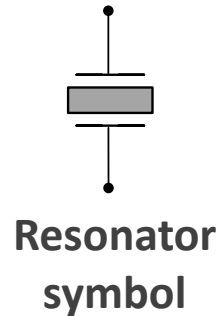
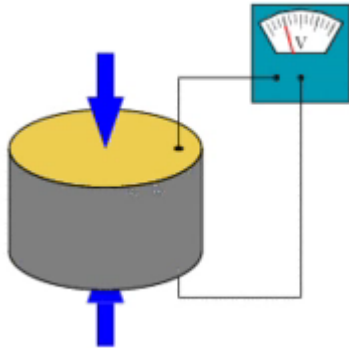
- **Viscous damping**
 - Displacement of gas or liquid molecules
 - Pressure and mode-shape dependent
- **Anchoring losses**
 - Radiation of energy to the substrate
 - Minimized using phononic crystals (artificial mirror for acoustic energy)
- **Material losses**
 - Surface states
 - Volume losses
 - Defects motion
 - Thermo-elastic damping
 - Akhiezer effect (electro-phonon dissipative coupling)



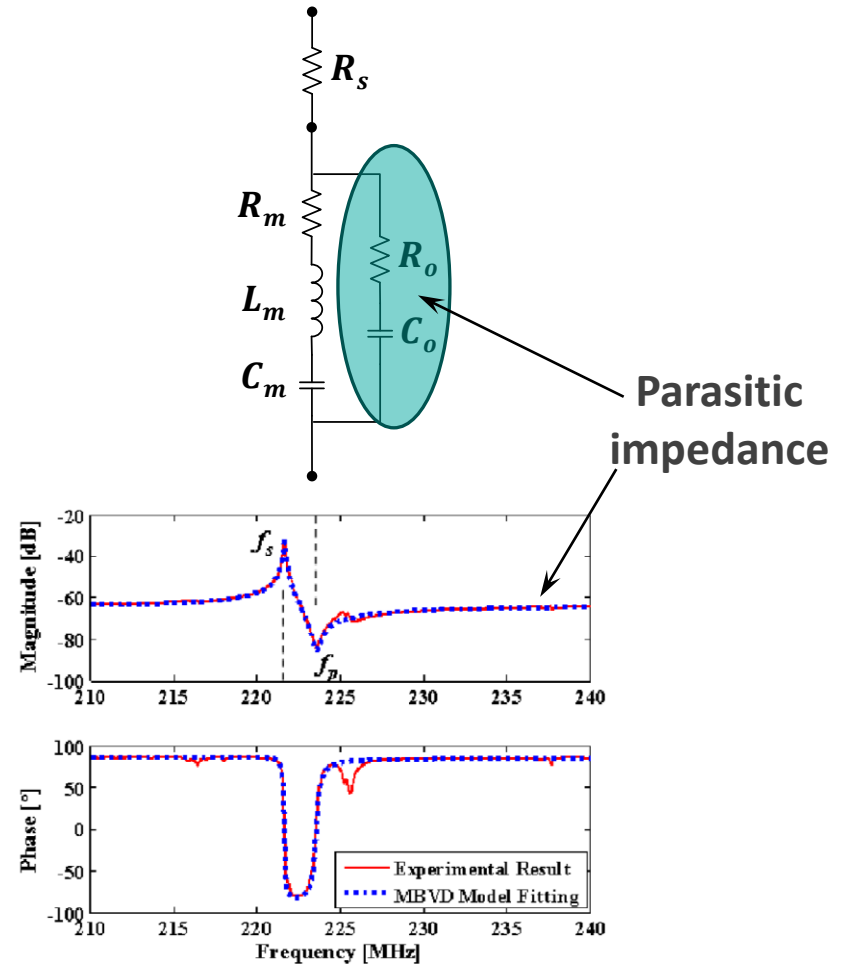
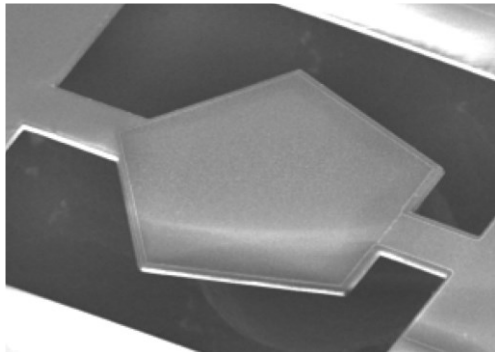
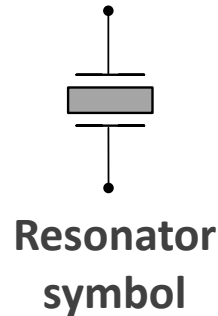
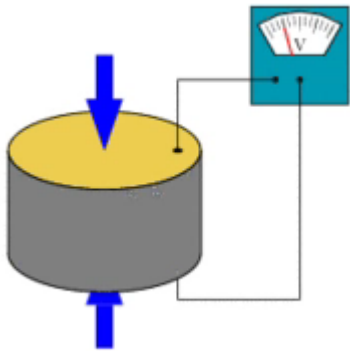
- Capacitive/Electrostatic
 - Thermal
 - Piezoresistive
 - Piezoelectric
 - Electrostrictive
 - Polarizing a dielectric material – effectively turning it piezoelectric
-
- Non dissipative
 - Based on material property
 - No need for external DC
 - Good scaling with frequency

- It's difficult to compare “*apples and oranges*”
- Figures Of Merit (FOM)
 - Useful to get much information into a single parameter
- $FOM_1 = f_r \cdot Q$
 - Determines which resonator would work better as an *oscillator*
 - It can be seen that there is kind-of a trade-off between f_r and Q
- $FOM_2 = k_t^2 \cdot Q$
 - k_t^2 measures how much mechanical energy gets converted into electrical energy
 - This FOM determines which resonator would work better as a *filter*
 - Piezoelectric resonators have the highest values

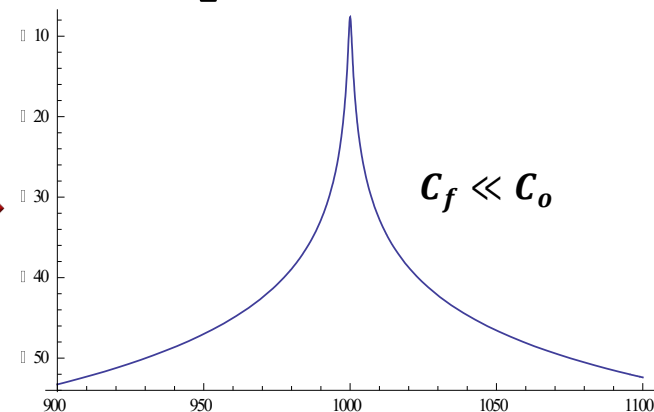
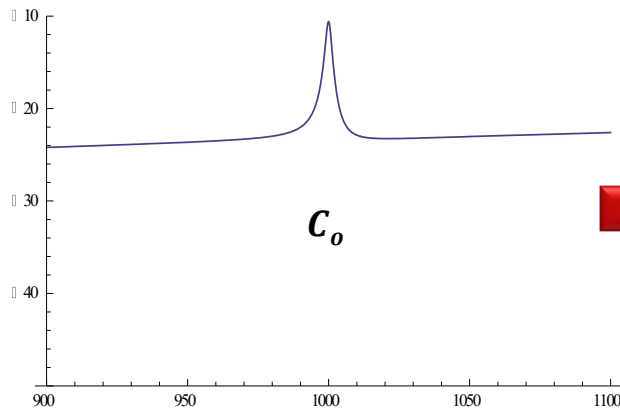
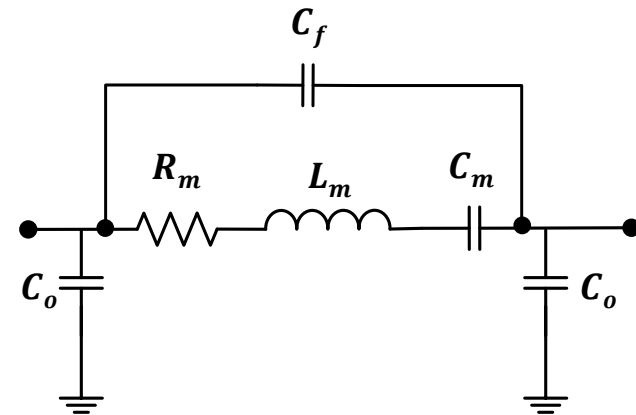
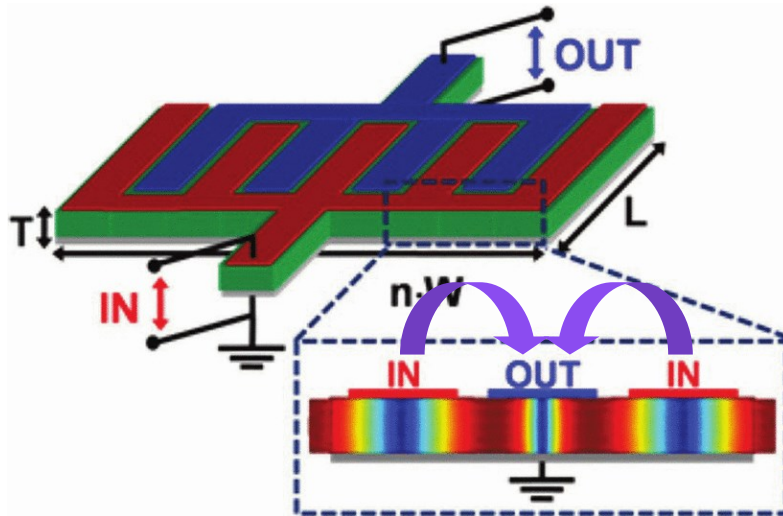
- Equivalent circuit
 - Allows to reproduce mechanical resonator behavior with circuit simulation tools
- Historically, the first one to be developed was a 1-port model for Quartz crystals



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 - Allows to reproduce mechanical resonator behavior with circuit simulation tools
- Historically, the first one to be developed was a 1-port model for Quartz crystals

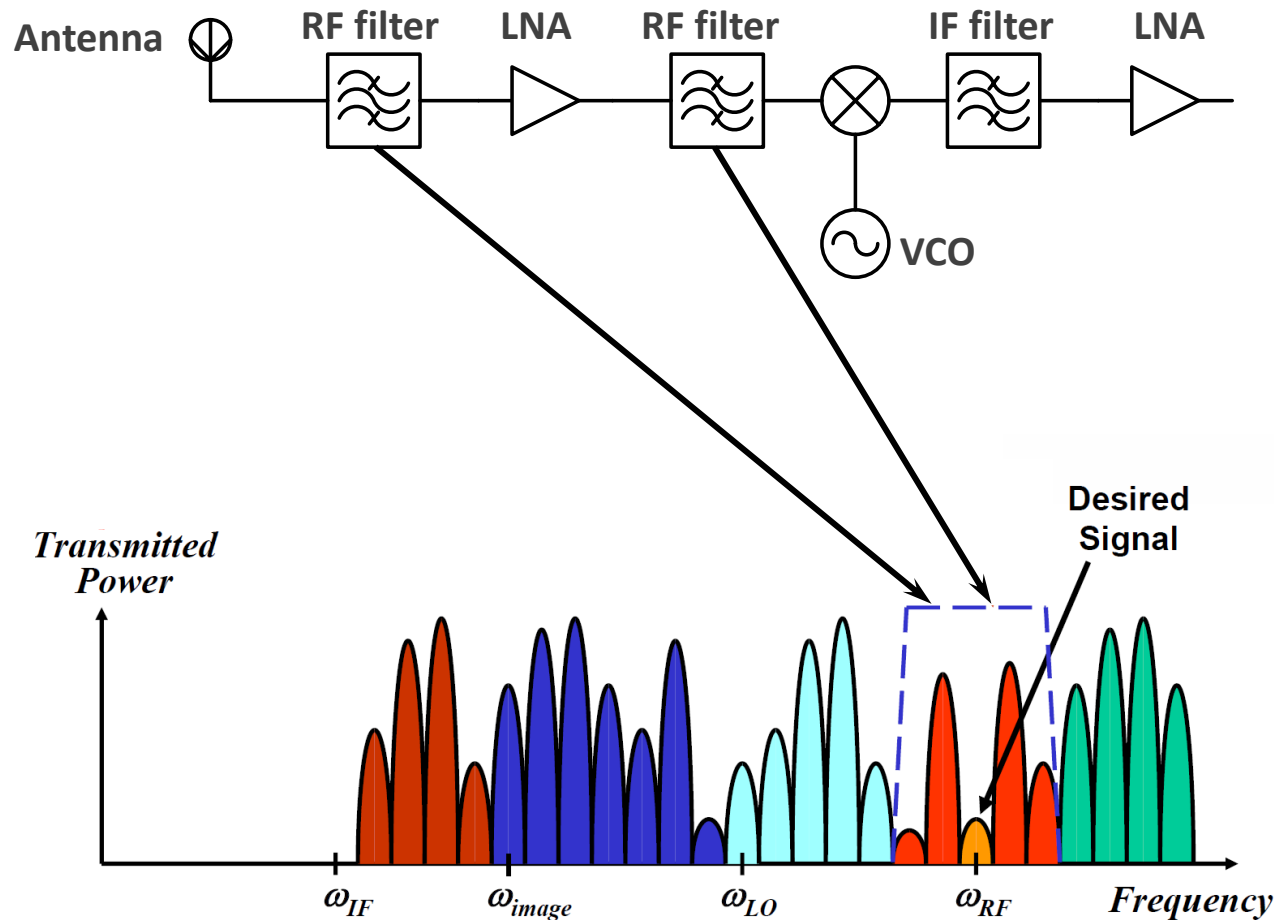


- In order to reduce the effect of parasitics
 - Two separate ports for excitation and readout

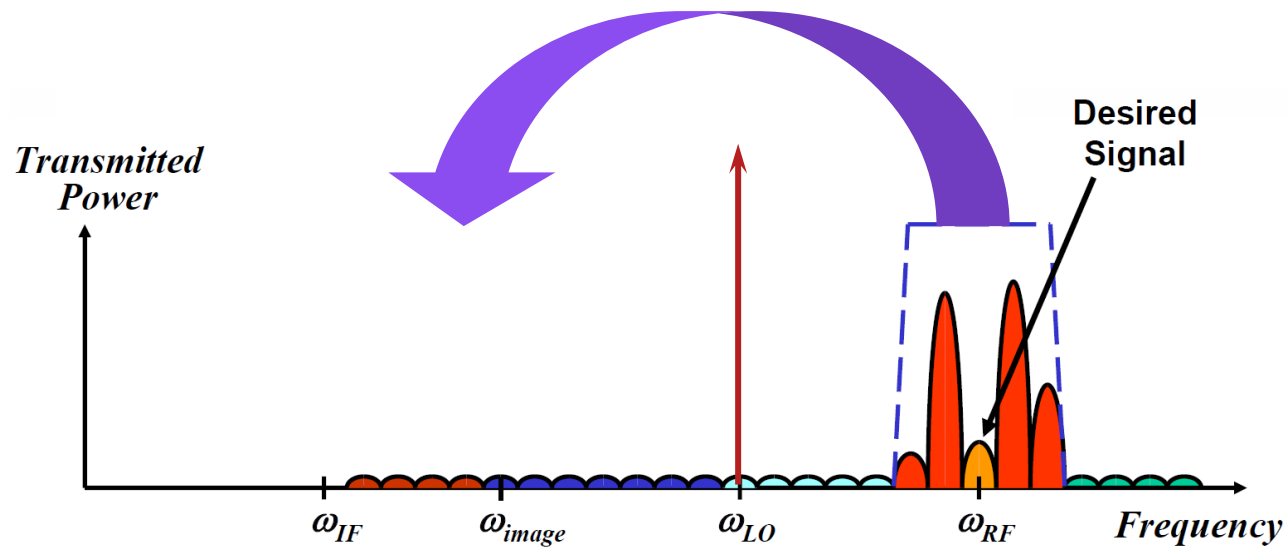
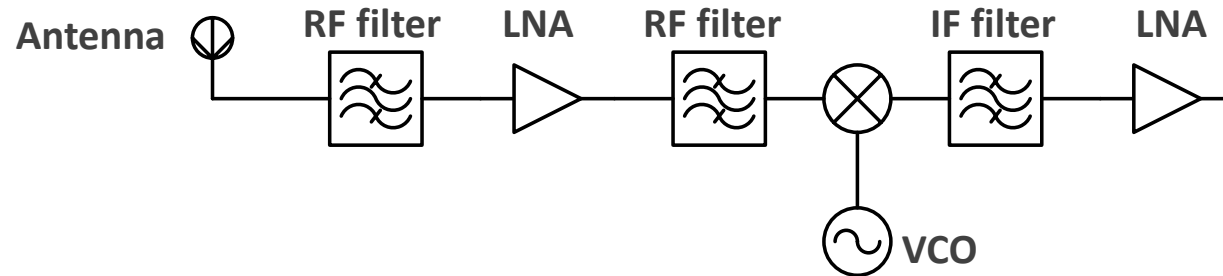


MEMS RF-FILTERS

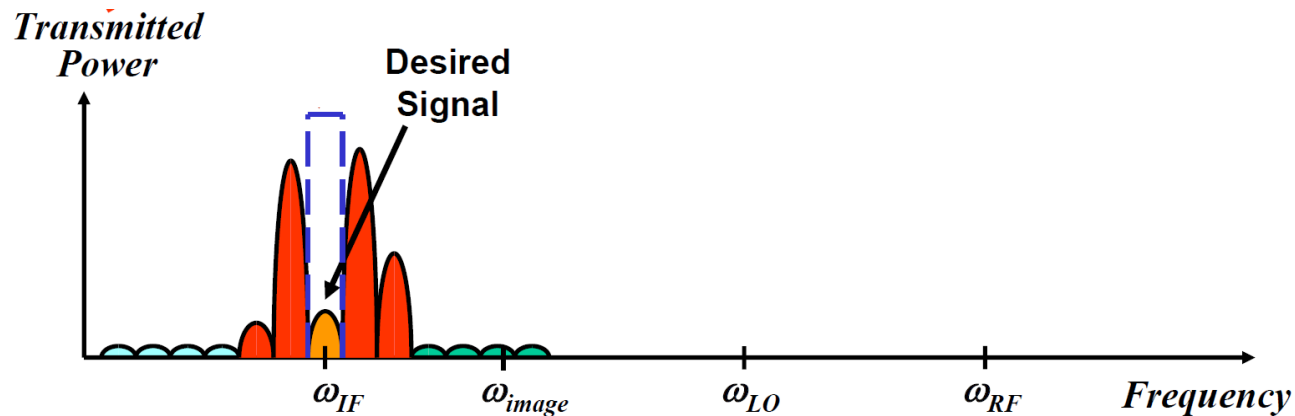
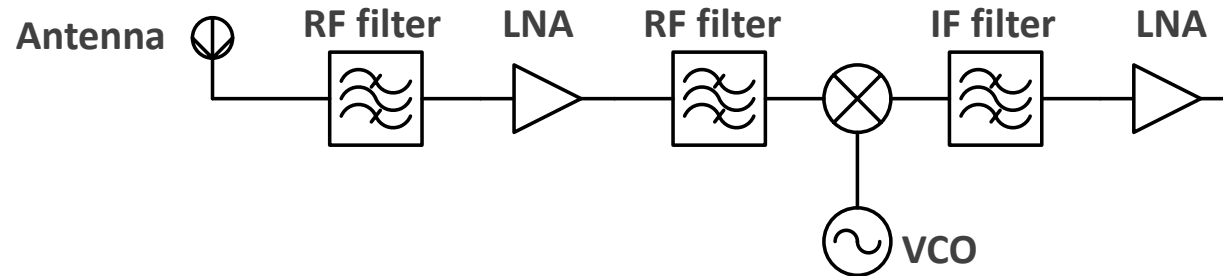
- Typically – Receivers work using heterodyne conversion



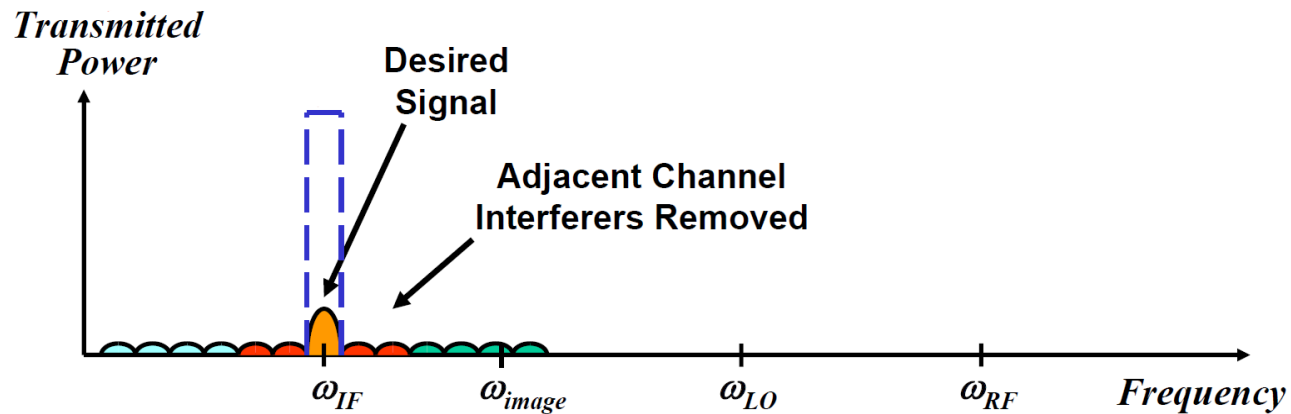
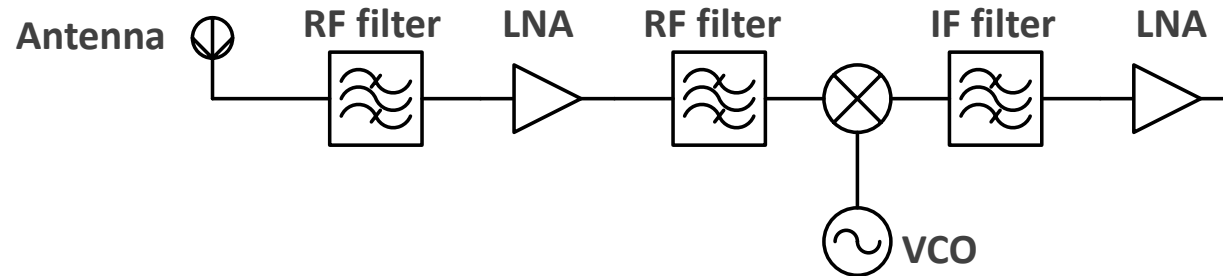
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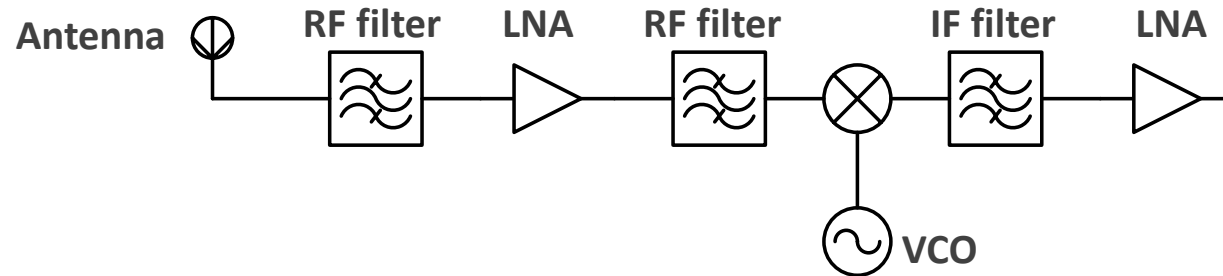
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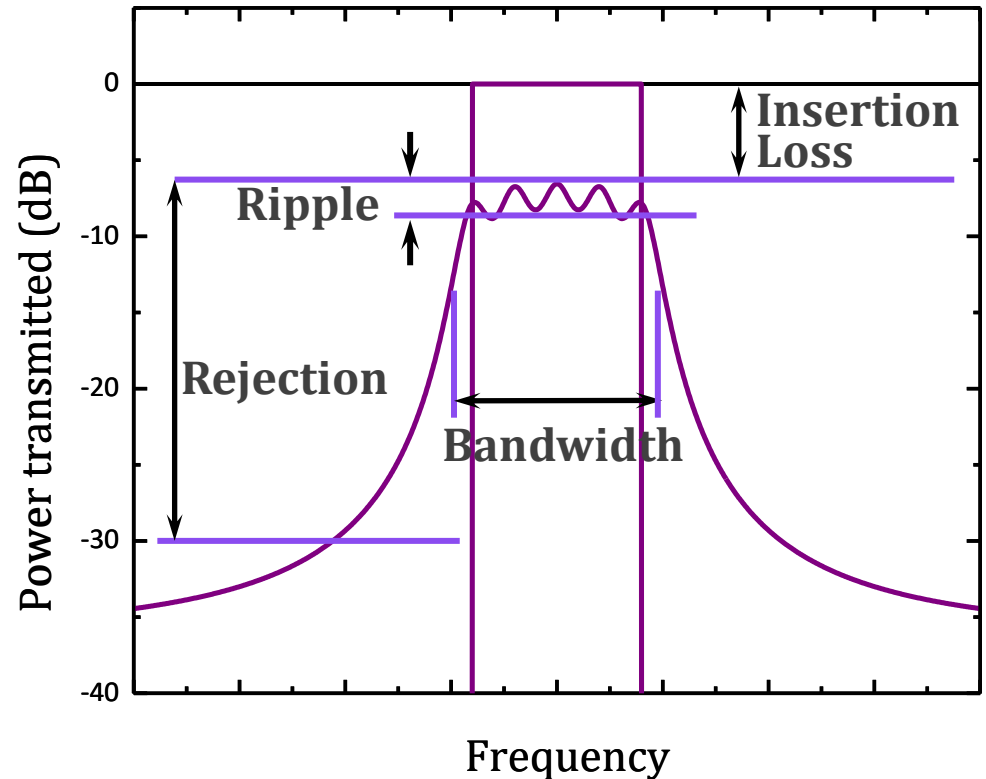


- Typically – Receivers work using heterodyne conversion

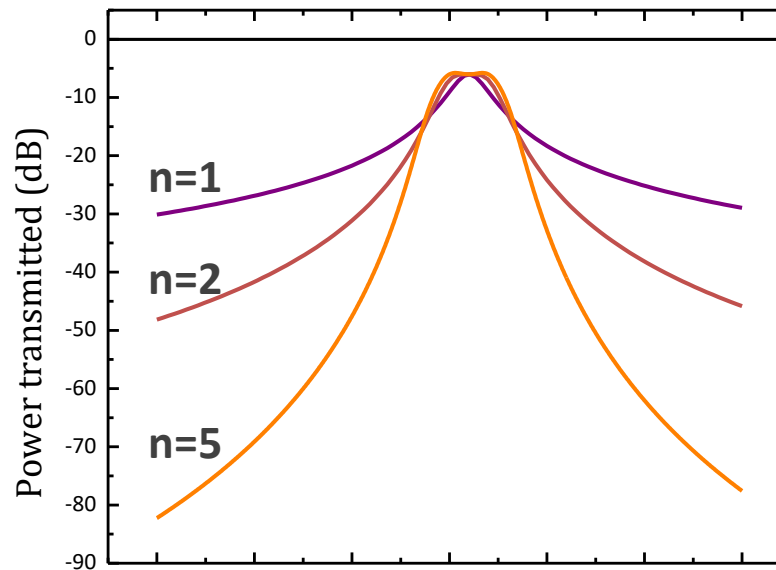
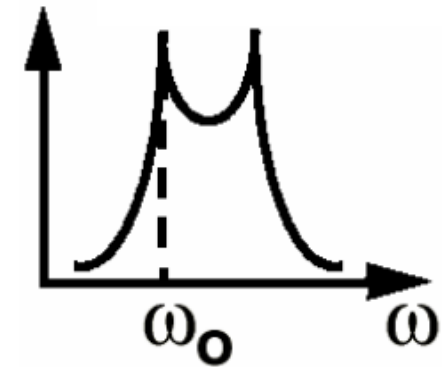
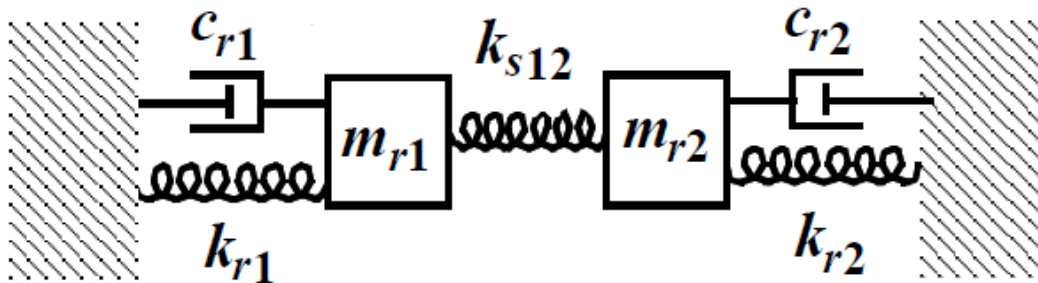


- It is necessary to do conversion down to IF because at RF, Q s are not good
- With RF-MEMS filters – Direct filtering is possible

- Ideal is a rectangular filter
- Filter design focus is mainly on
 - Insertion loss (and ripple)
 - Bandwidth
 - Rejection
 - Impedance
- Arrays of coupled resonators
 - High Q = high rejection
 - Separation = Bandwidth
- Coupling can be
 - Electrical
 - Mechanical
 - Acoustical



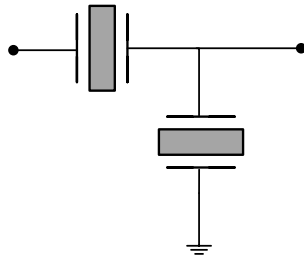
- Basic idea
 - 2 coupled resonators
 - Symmetric and Anti-Symmetric motion
 - New frequencies are defined by coupling factor



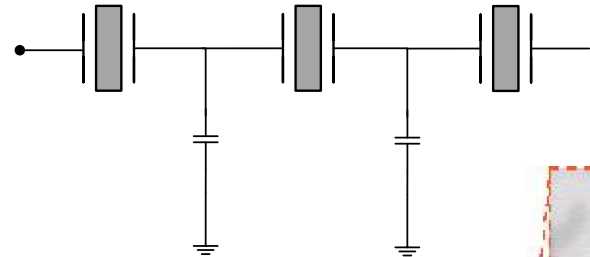
Sharper rejection for a larger Bandwidth with more coupled resonators

- Electrical

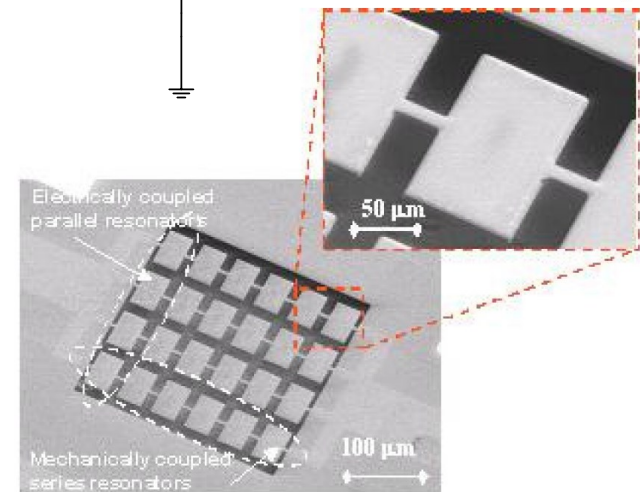
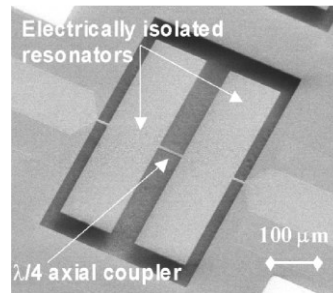
- Ladder-like



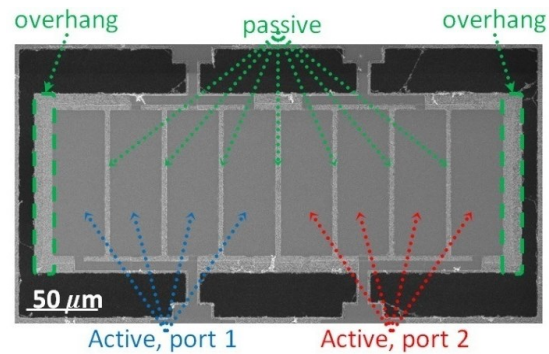
- Series



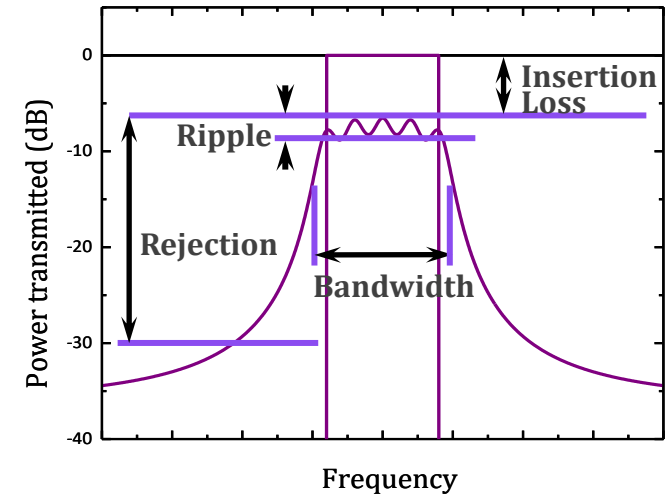
- Mechanical



- Acoustic



- Depends on transduction and geometry
- Piezoelectric contour-mode resonators:
 - Bandwidth
 - Set by the electromechanical coupling coefficient
 - Insertion Loss
 - Set by $FOM_2 = k_t^2 \cdot Q$
 - Rejection
 - Controlled by parasitics (C_f)
 - Impedance
 - Termination capacitance, can be tuned



$$BW \sim \frac{3}{\pi^2} k_t^2$$

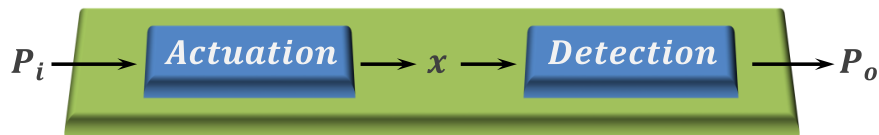
$$IL \sim -20 \log \left(\frac{4}{4 + (3\pi^2)/(k_t^2 Q)} \right)$$

$$Reject \sim -20 \log \left(\frac{C_f}{C_o} \right) - IL$$

$$IL \sim \left| \frac{1}{j\omega_c C_o} \right|$$

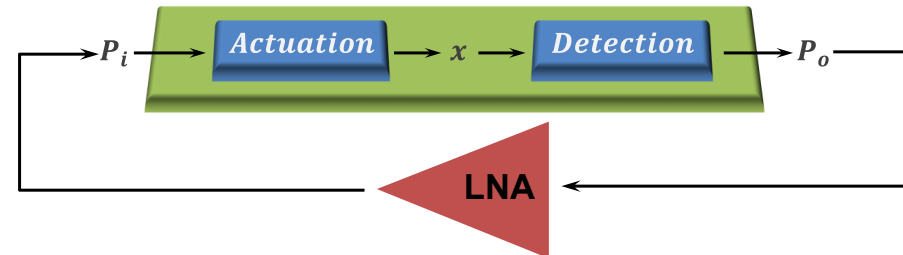
MEMS OSCILLATORS

Passive/Resonator



- Power output linearly depends on power input
- Requires a harmonic drive to have response

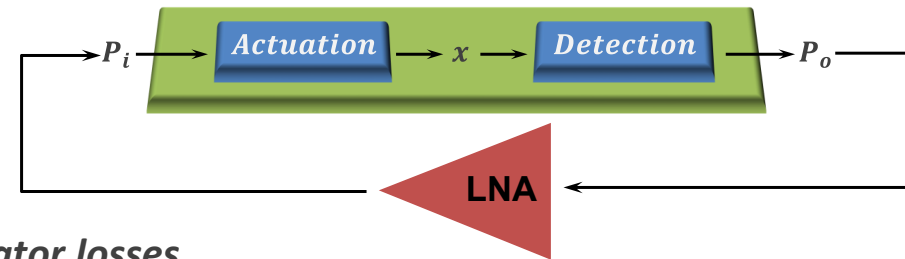
Active/Oscillator



- Outputs a harmonic signal by only applying DC power

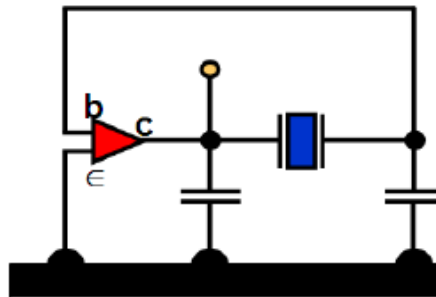
- Idea

- Amplify P_o enough to *compensate resonator losses*
- Feed it back to device with *appropriate phase*
- *Barkhausen's criteria*

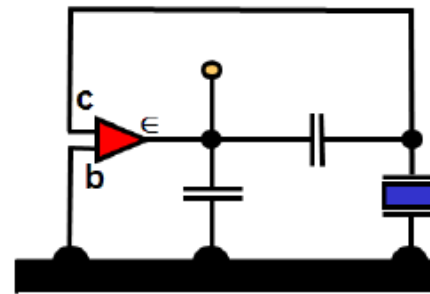


- Two simplest implementations

- Pierce & Colpitts oscillators
- 1 transistor, 2 capacitors – oscillator is running!



Pierce



Colpitts

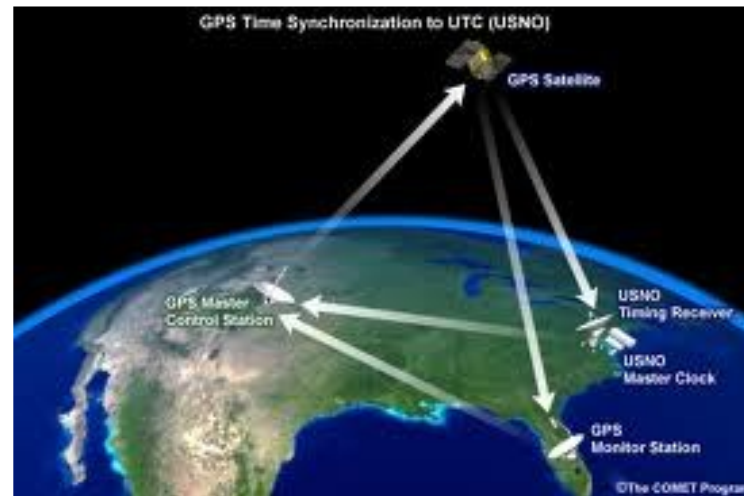
- Every watch has an oscillator inside – to keep track of time
- Oscillator's beats are later translated into seconds (e.g. by a counter)
- For a precise watch – necessary a precise oscillator
- Precision is required in the long term (this is important)



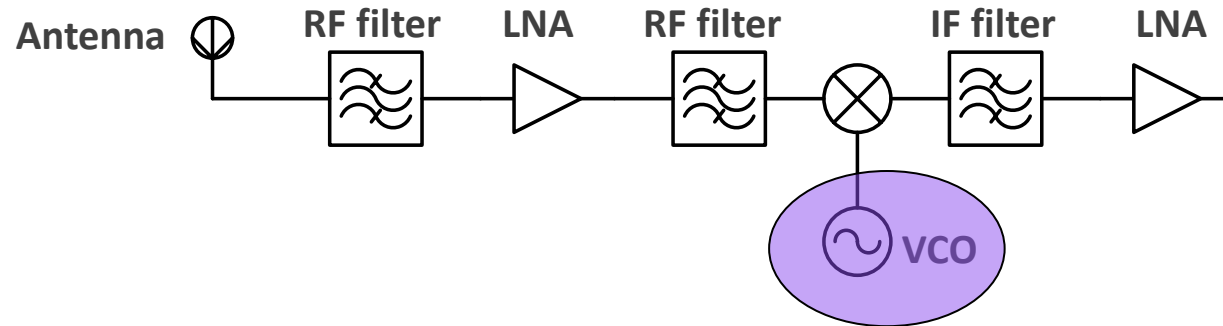
- What is the most precise clock?
 - Atomic Clock – *30 fs error per day!!!!*



- Applications that require very high precision?
 - Geolocation (GPS, Galileo...)
 - Radar, LiDAR,...



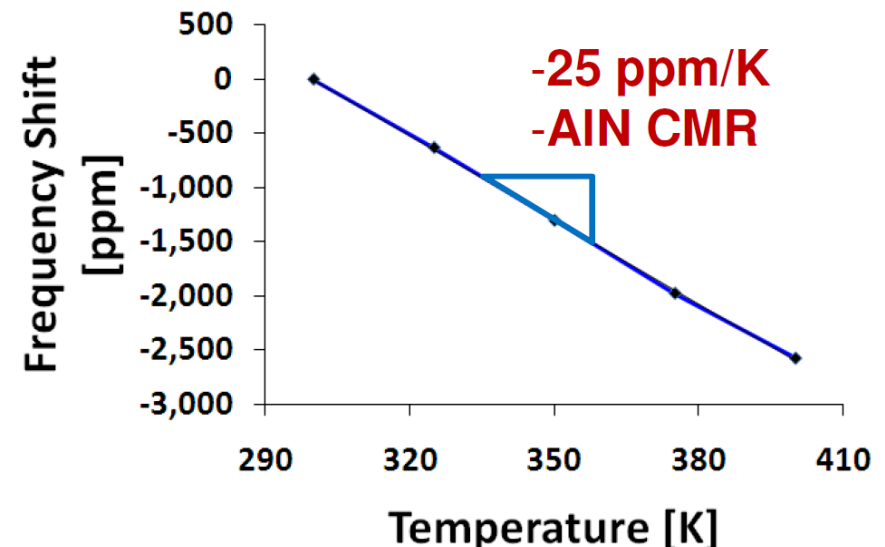
- **Communications**
 - **Front-End/Receiver**



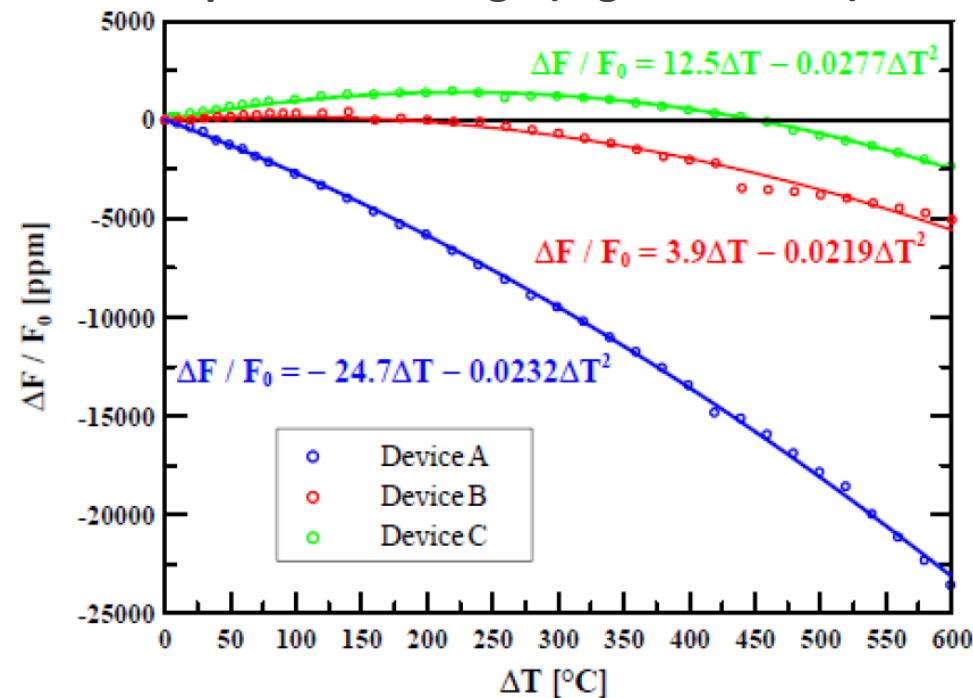
- **Oscillator signal is used to encode and decode signals**
- **Clean communication needs a precise oscillator**
- **Precision is important at very short timescales, < 1 ms**

- **Phase noise**
- **Temperature stability**
- **Acceleration stability**
 - Vibrations affect resonant frequency
 - $f = f_0(1 + \Gamma \cdot |\vec{a}|)$
 - $\Gamma \sim 10^{-5} \text{g}^{-1}$ for most MEMS devices
- **Power consumption**
 - More autonomous devices
 - Stand-by and clocking applications
 - 32.768 kHz ($= 2^{15} \text{Hz}$)
 - $\sim 1 \mu\text{W}$
- **Size**
 - Smaller footprint = Cheaper

- Frequency depends on temperature
 - $f = f_0(1 + \text{TCF} \cdot \Delta T)$
- TCF can have different origins
 - Change in Young's modulus $\partial E / \partial T$
 - Change in volume/dimensions/density $\alpha = \partial L / \partial T$
 - Change in tension, surface stress, etc.
- Specification asks for ~ 10 ppm over the whole operational range (e.g. $-30 - 70^\circ\text{C}$)
 - $\partial E / \partial T \sim \pm 10$ ppm/K!!!!!!
- Solutions for compensation
 - Quartz crystals get special cuts

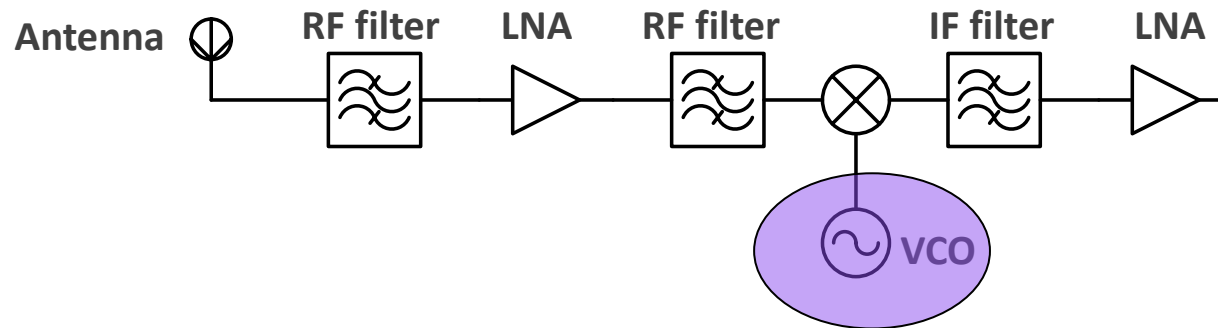


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 - MEMS – hybrid structures to balance (using positive and negative $\partial E / \partial T$)
 - Not linear over wide T range

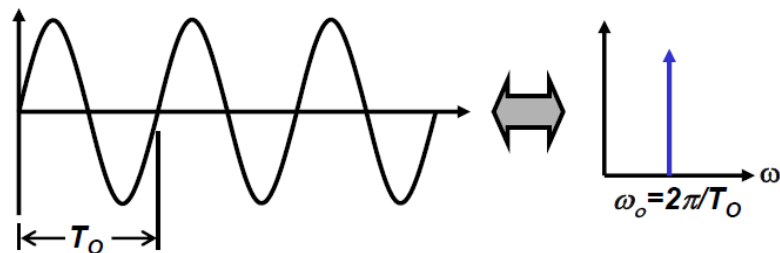


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- Solutions for compensation
 - Quartz crystals get special cuts
 - MEMS – hybrid structures to balance
(using positive and negative $\partial E / \partial T$)
 - Not linear over wide T range
 - Circuit compensation
 - Use external circuit to detect T and correct the frequency
 - Best results but causes Power consumption to increase
 - Cheaper resonators

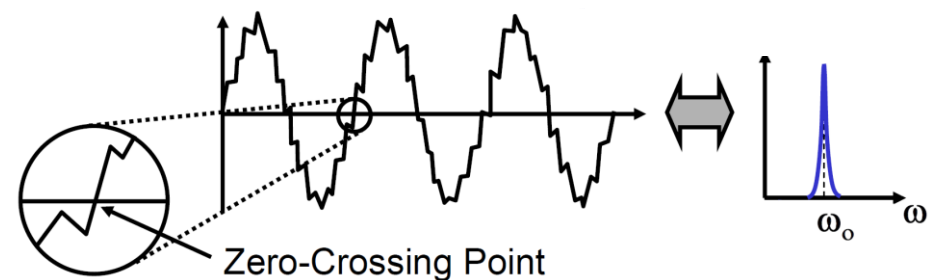
- Communications

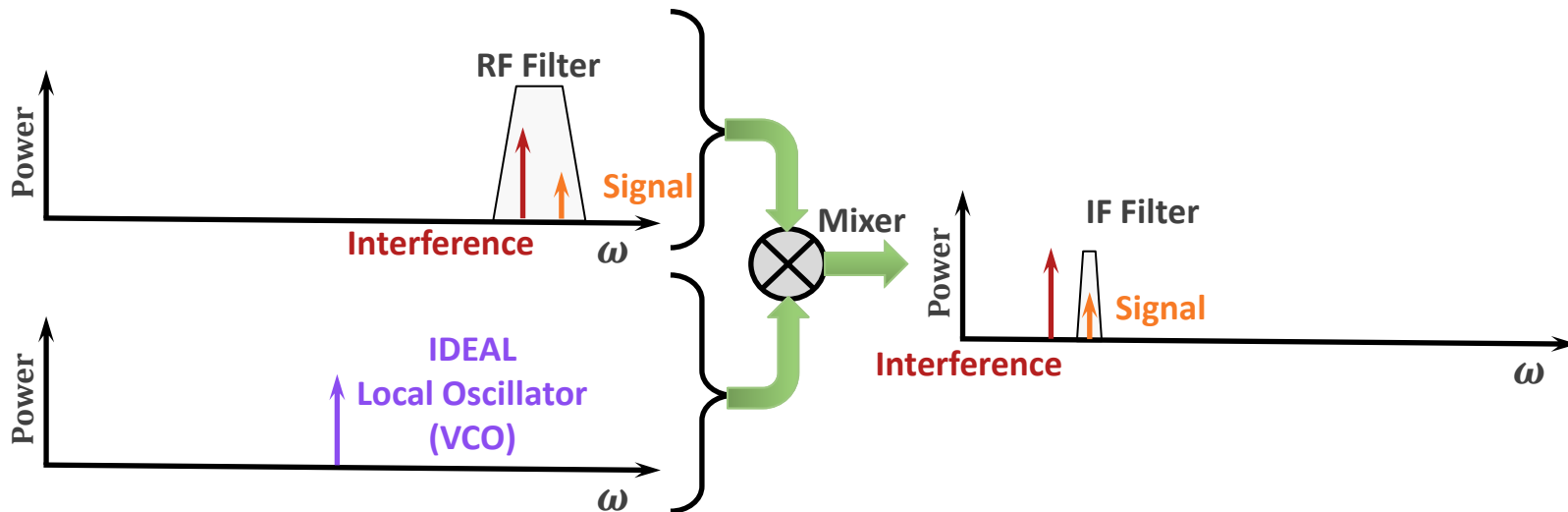
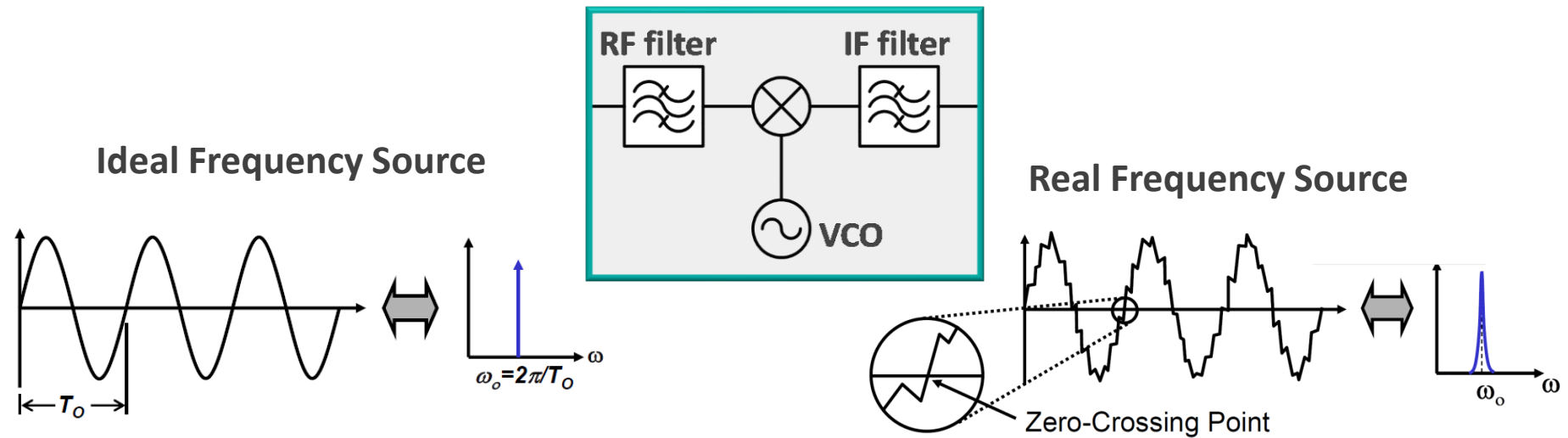


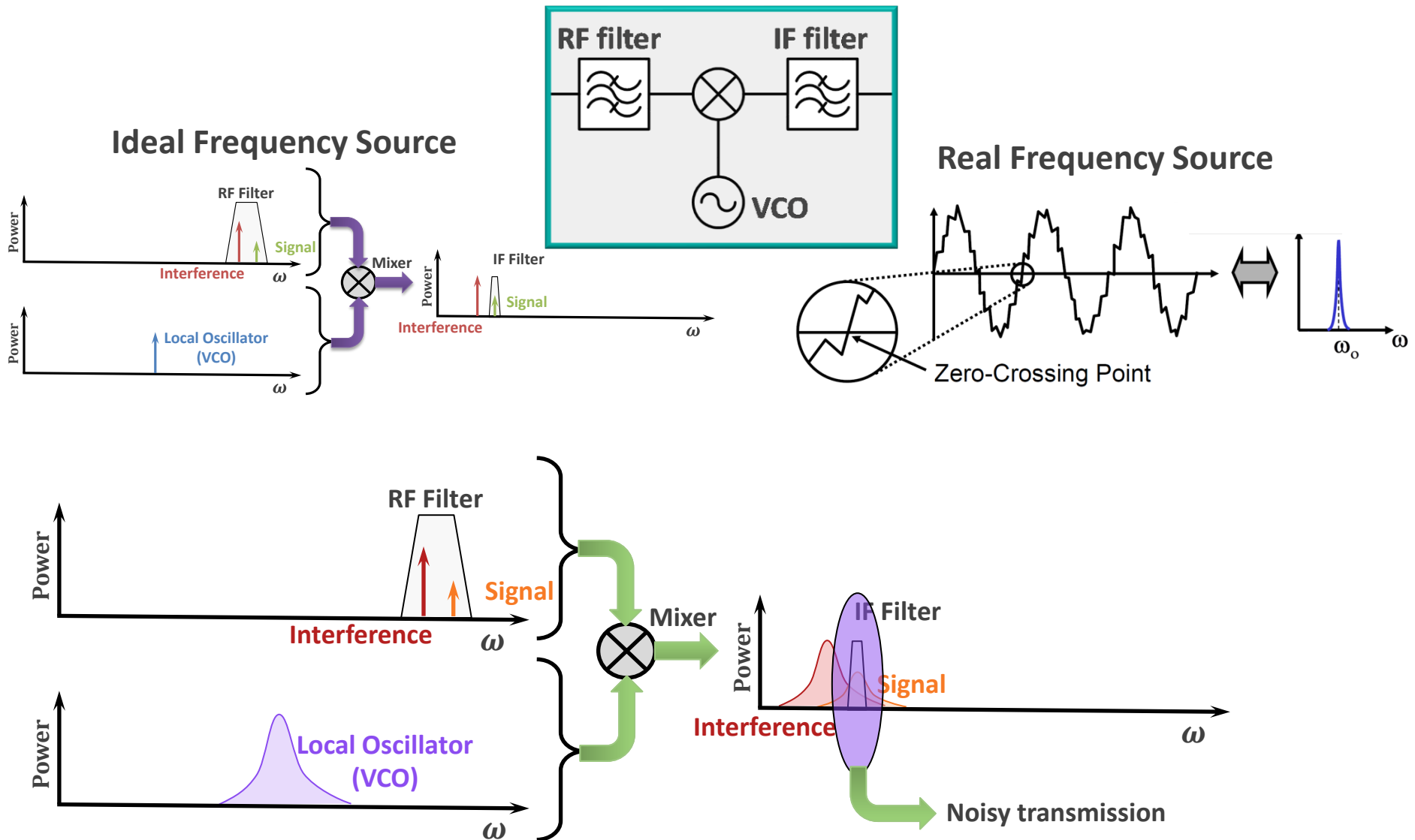
Ideal Frequency Source



Real Frequency Source







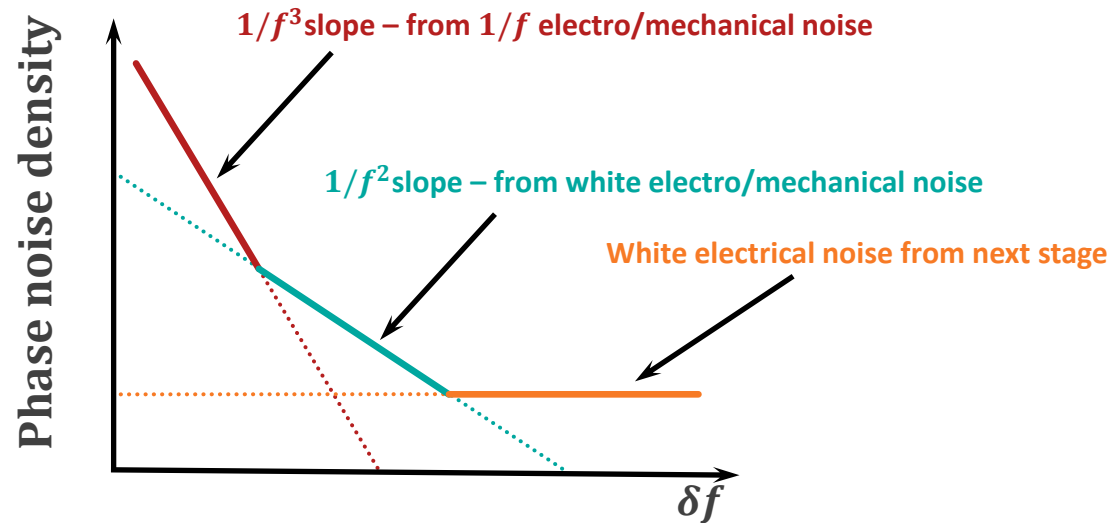
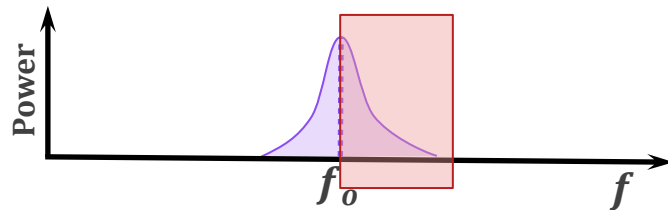
- Phase noise determines the precision of the oscillator
 - How accurate the generated frequency signal is
- It is measured in relative power to the total carrier power per Hz

- $\frac{dBc}{Hz}$

- Leeson's formula

- $S_{\phi}(\delta f) = 10 \log \left(F \frac{k_B \cdot T \cdot f_0}{Q \cdot E} \frac{1}{\delta f^2} \right)$

- Incomplete, needs some modifications/additions



- Phase noise determines the precision of the oscillator
 - How accurate the generated frequency signal is
- It is measured in relative power to the total carrier power per Hz

$$- \frac{dBc}{Hz}$$

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- Incomplete, needs some modifications/additions

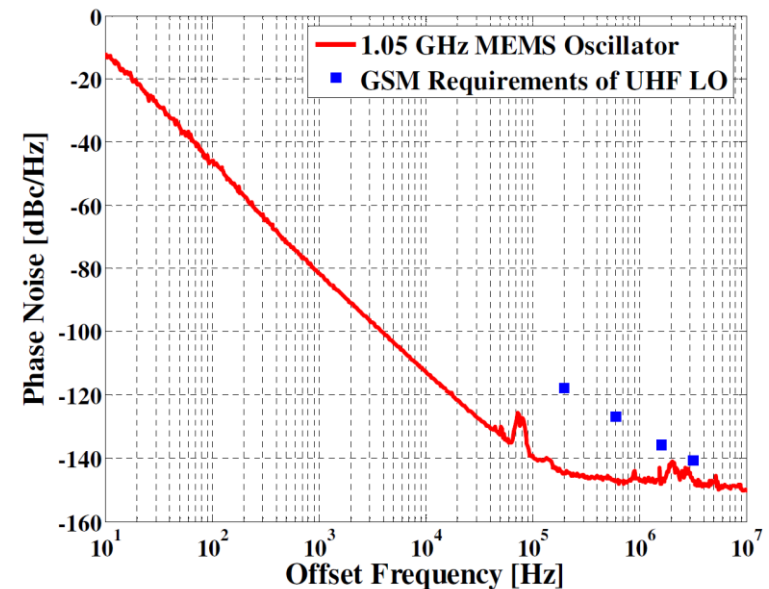
- Specifications/Requirements

- Depend on the *carrier frequency*
 - High frequencies can be divided
 - “Averages” $1/f^2$ noise
- Great advantage of MEMS
 - High $FOM_1 = f_r \cdot Q$

- Phase noise is a very critical parameter because it cannot be filtered out or adjusted externally

GSM Requirements	
f_m	PN
kHz	dBc/Hz
200	≤ -118
400	≤ -124
600	≤ -127
800	≤ -130
1600	≤ -136
> 3200	≤ -141

[Q. Gu, Springer 2005]



It's About Time

The logo for the MEMS First Process, featuring a complex, symmetrical, multi-layered geometric design in a light gray color. The design consists of several concentric, interlocking shapes that form a central square-like structure with rounded corners and intricate internal patterns.

MEMS First™ Process

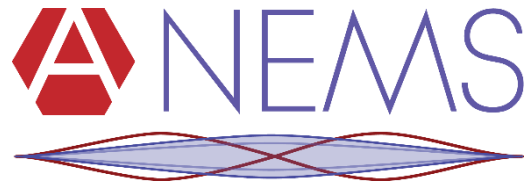
- **What is a Resonator?**
- **Quality factor**
 - High or low?
 - What determines if it's high or low?
- **Why MEMS resonators?**
- **Types of MEMS resonators**
 - Frequency dependence on dimensions
 - Major application fields
- **MEMS filters (passive)**
 - What are the most important parameters to optimize?
- **MEMS oscillators (active)**
 - Why is phase noise important?
 - Why is T stability important and how is it achieved?

Lecture 6 – NEMS

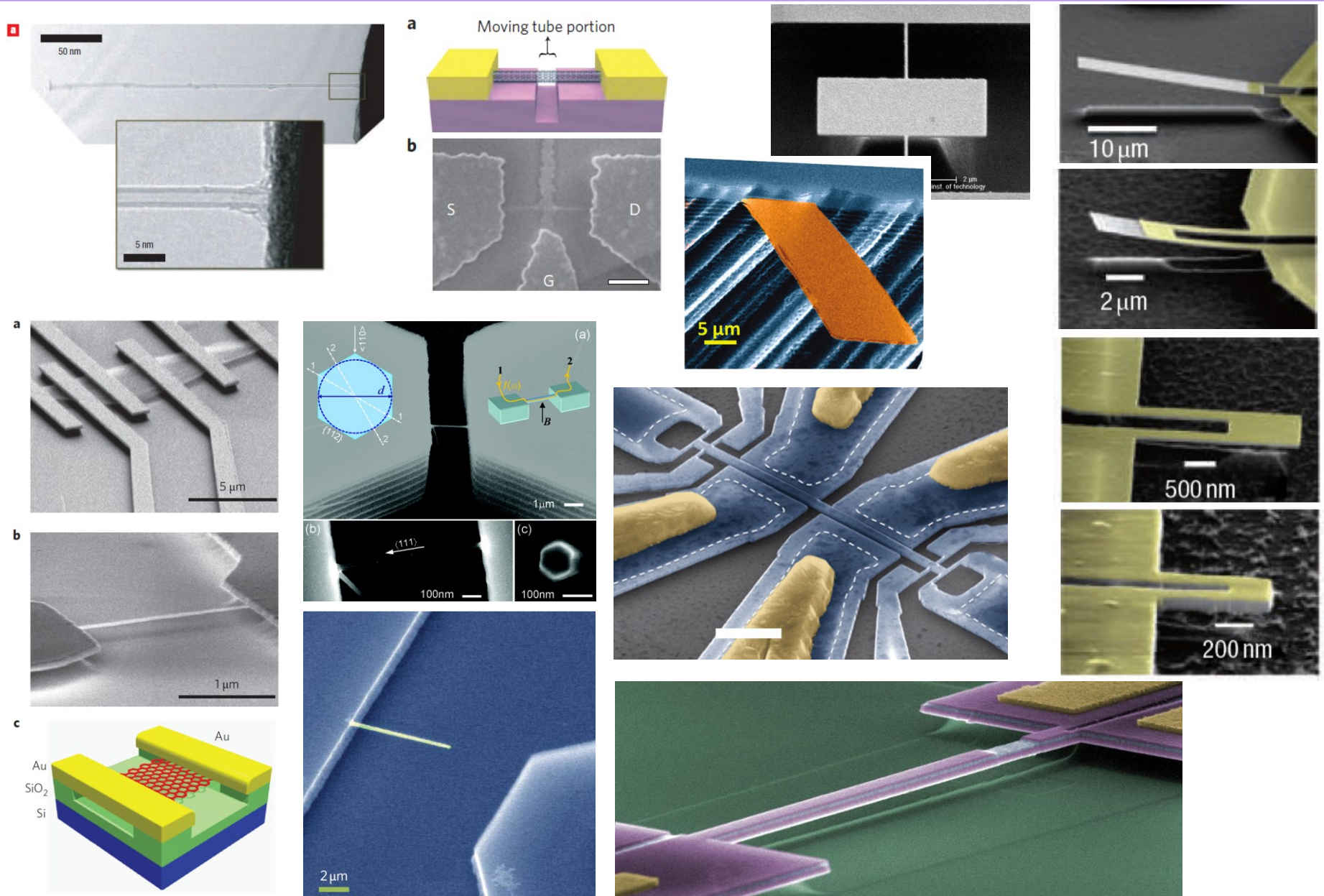
Prof. Guillermo Villanueva

Advanced NEMS Lab (ANEMS)

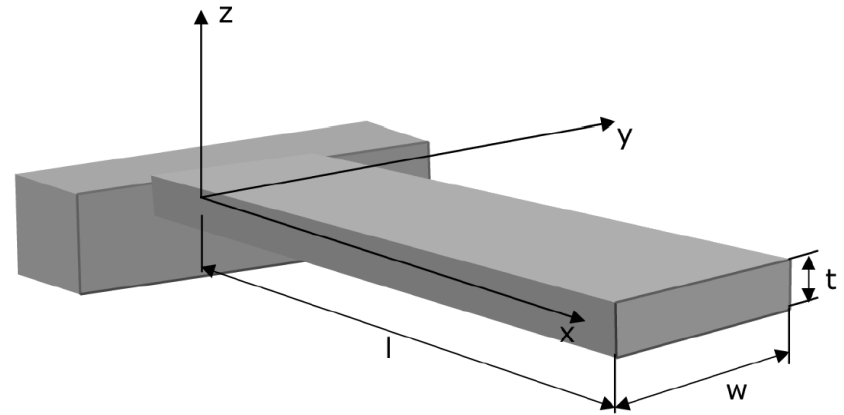
EPFL-IGM NEMS



- **Introduction**
 - **NEMS examples**
 - **NEMS definition(s)**
 - **Why NEMS?**
 - **NEMS Fabrication**
 - **Main challenges**



- NEMS tends to include “small MEMS”
- 1 possible definition
 - 2 out of 3 dimensions $\leq 1\mu m$
- But then...
 - What about graphene resonators?
 - Or extremely thin MEMS?



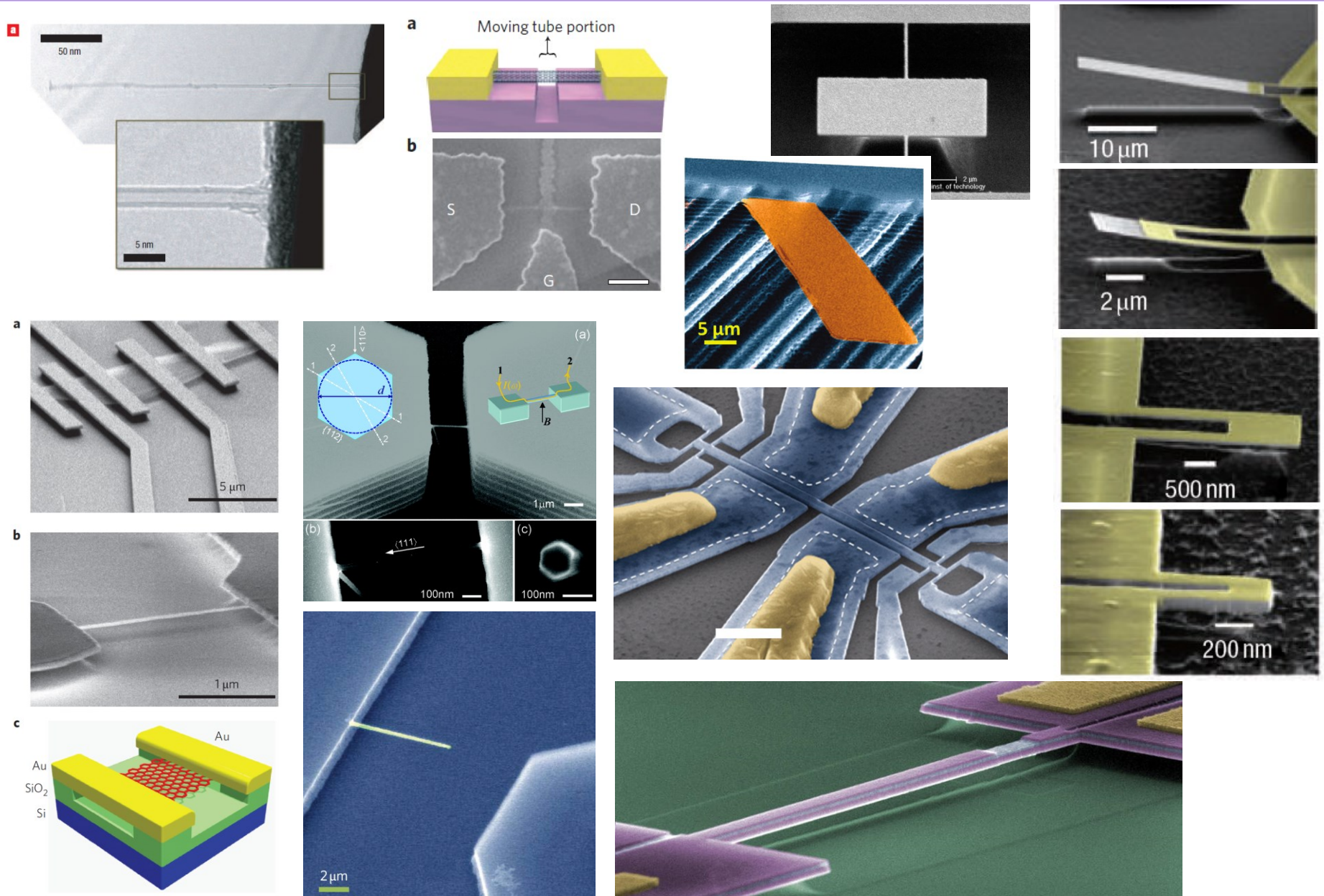
- Another possible definition – “mesoscopic system”
 - Referring to number of atoms in the mechanical device
 - Golden Gate – $\sim 10^{34}$ atoms
 - Trampoline – $\sim 10^{28}$ atoms
 - Guitar string – $\sim 10^{23}$ atoms
 - MEMS accelerometer – $\sim 10^{16}$ atoms
 - Thin plate – $\sim 10^{12}$ atoms
 - Si-based NEMS – $\sim 10^{10}$ atoms
 - CNT – $\sim 10^5$ atoms
- Macroscopic
- Microscopic
- Mesoscopic

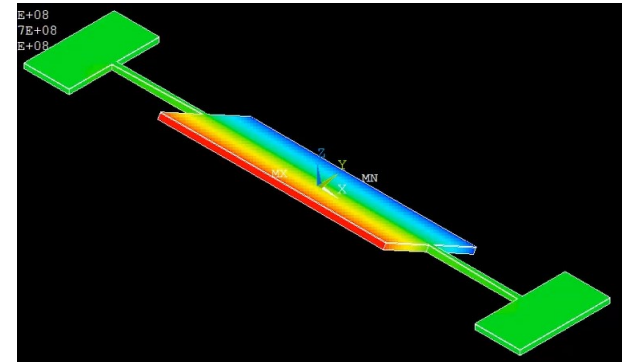
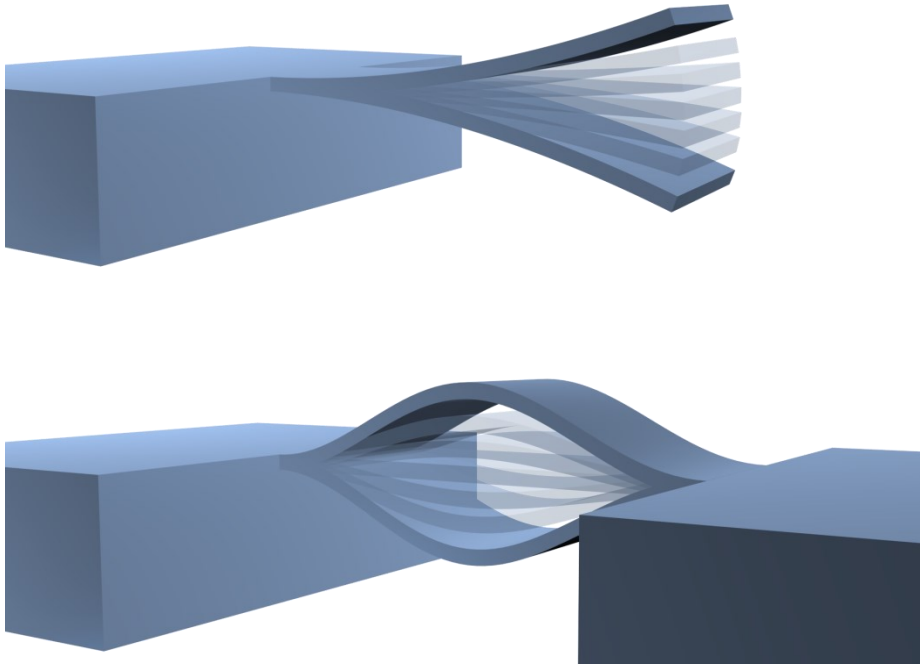
- **Top-Down**

- Pushing down the dimensions of standard μ fab tools
- EBL, DUV, NIL, Stencil, FIB – To improve the resolution of UV Lithography
- Finer tuning of etching and deposition recipes
 - Smooth edges
 - Accurate thicknesses
- Easy integration and connection to “macro” world
- Very high cost to reduce dimensions

- **Bottom-up**

- Direct growth/synthesis of structures
- Highly based on chemical processes and reactions
 - CVD, VLS method, Arc-discharge...
- Very cheap to produce millions of devices
- Very difficult to integrate and connect them (eventually using top-down techniques)





- Intuitive and clear understanding of motion
- Very low masses
- Very low stiffness

- **Size**
 - Higher level of integration
 - Very thin – good for stress-based sensing
- **Mass**
 - Low thermal mass – good for T or heat sensing
 - Low mass – good for detection of small mass landing
 - Gravity/Acceleration can be mostly neglected
- **Stiffness**
 - Low stiffness for a given frequency – good for Force sensing
- **Frequency**
 - High frequency – less influence from vibrations & faster measurement

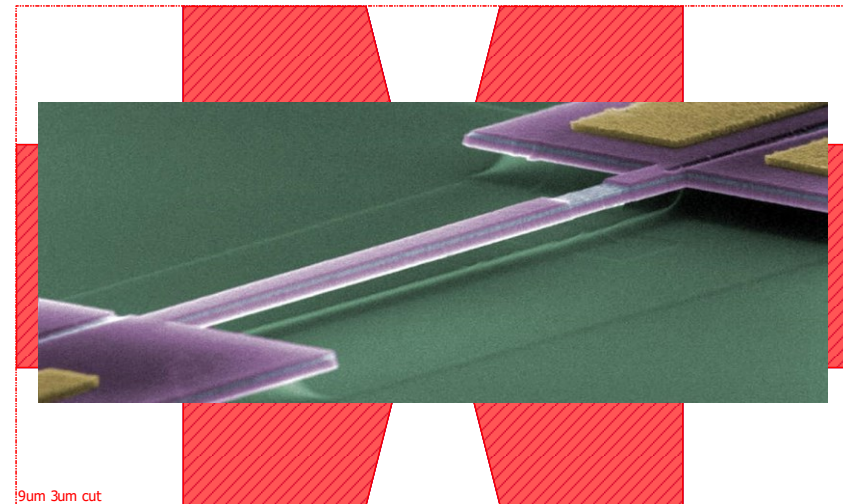
- **Fabrication**

- Expensive (top-down)
- Difficult to contact (bottom-up)
- Imperfections become (relatively) too large
 - Surface roughness
 - Surface contaminants
 - Material defects
 - Grain boundaries

- Low reproducibility
- Mechanical properties deteriorate
- Lower Q factors

- **Measurement**

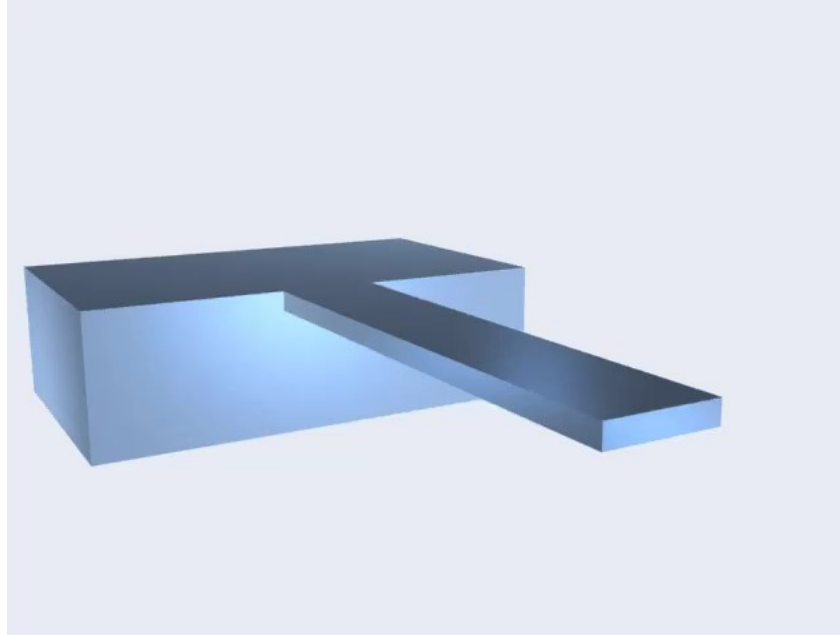
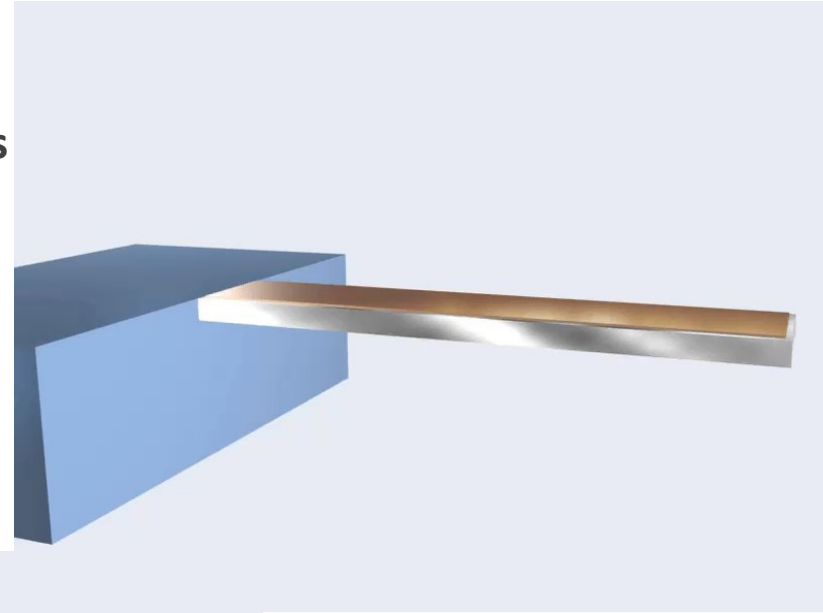
- Connection to “macro” world unavoidable
- Motional signal is “buried” in parasitics
- Very challenging to
 - Match impedance
 - Remove background
 - Amplify signal



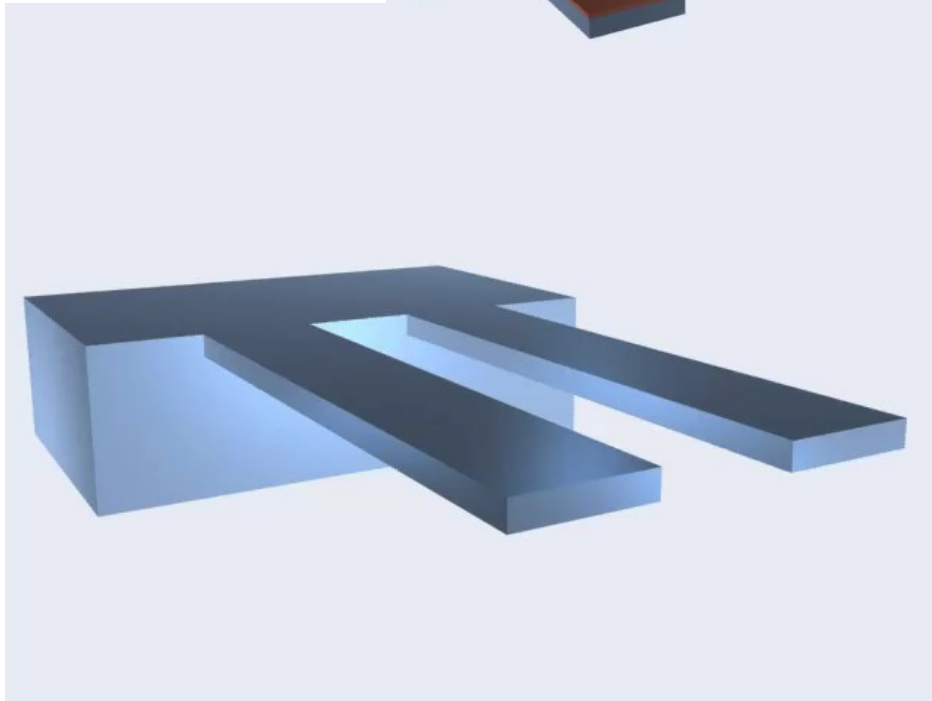
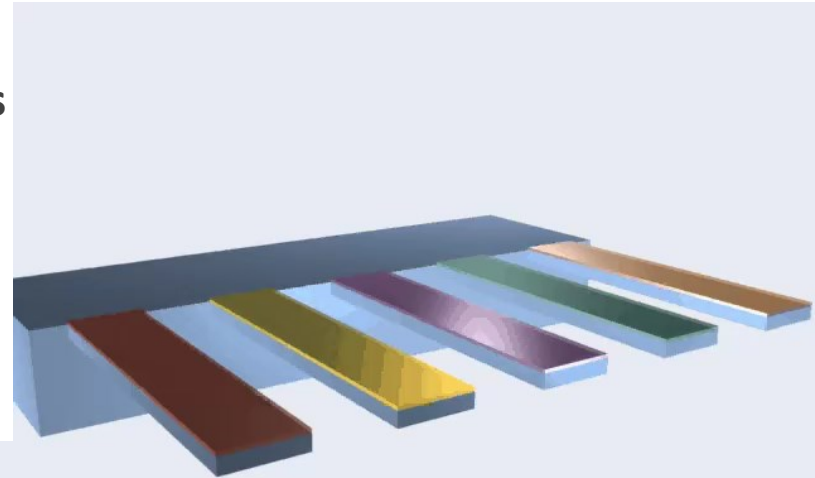
STATIC DETECTION

- **Mechanical system is not moving at first**
- **Event happens and mechanical device responds**

- Mechanical system is not moving at first
- Event happens and mechanical device responds
- Temperature
 - Thermal expansion gradient
- Gas sensor
 - T based

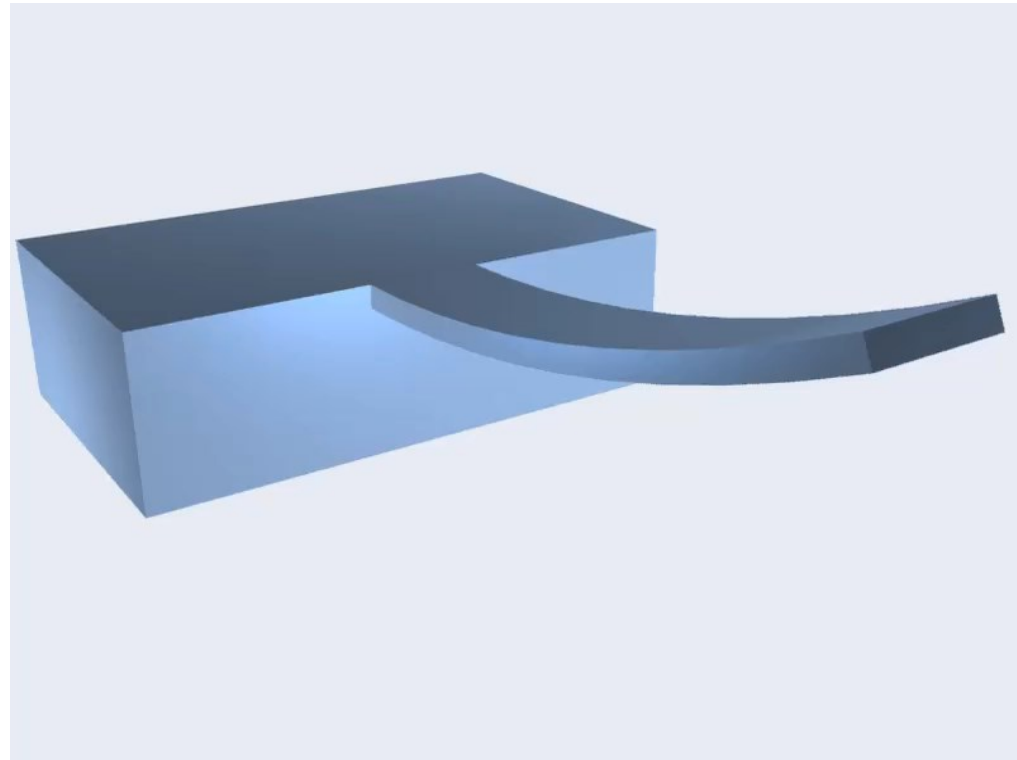
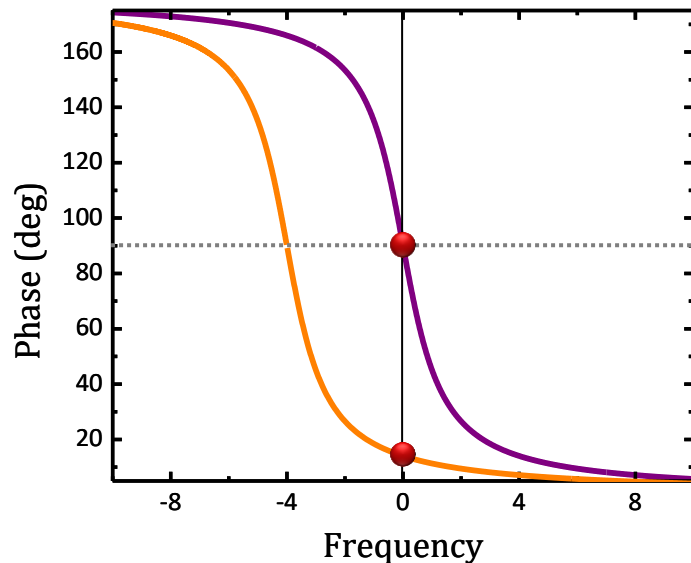


- Mechanical system is not moving at first
- Event happens and mechanical device responds
- Temperature
 - Thermal expansion gradient
- Gas sensor
 - T based
 - Surface stressed based
- Reference always needed



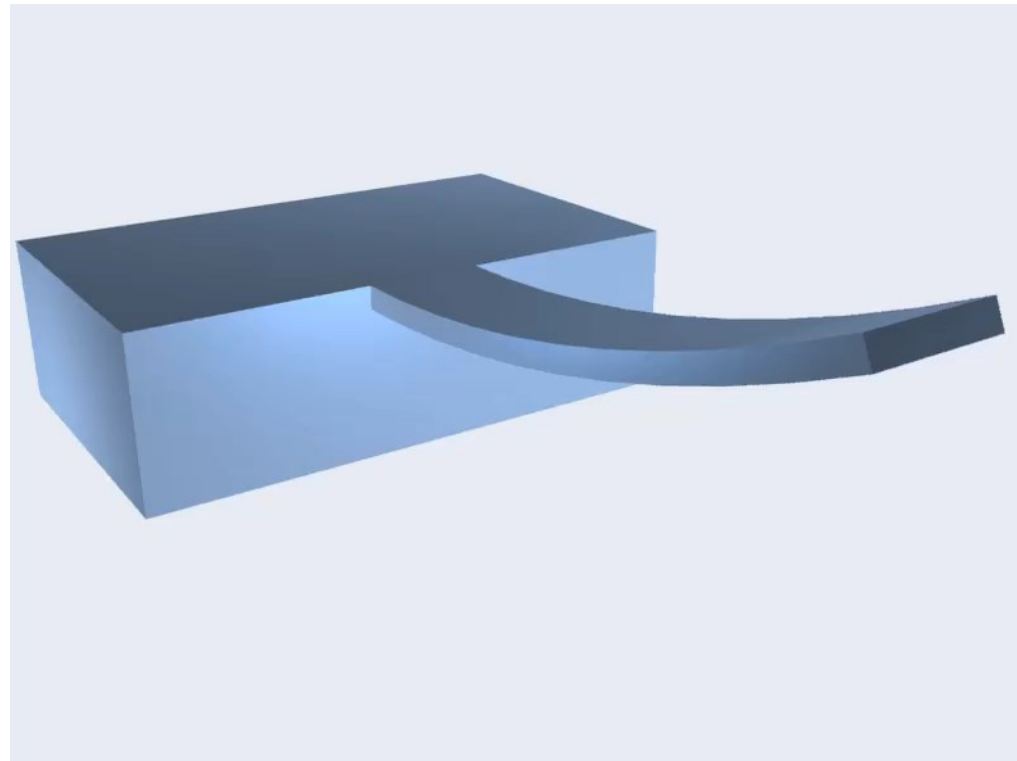
DYNAMIC DETECTION

- Mechanical system moving constantly
 - At or close to the resonance frequency
- Event happens and mechanical device responds
 - By changing its resonance frequency
- Frequency is the magnitude that is tracked
 - PLL or oscillator
 - Frequency counter



- **Mechanical system moving constantly**
 - At or close to the resonance frequency
- **Event happens and mechanical device responds**
 - By changing its resonance frequency
- **Frequency is the magnitude that is tracked**
 - PLL or oscillator
 - Frequency counter
- **Mass**
 - Deposition or removal of material
 - Gases, mass spectrometry
- **Material properties**
- **Temperature**
- **Stiffness**
- **Stress**

Noise in frequency determines device performance



- **Why NEMS?**
- **Static & dynamic sensing**
 - How do they work in general?
 - What are the main differences between NEMS and MEMS?
 - Why is it interesting to go to NEMS?
 - Examples
 - What is most important?
 - How to build a better sensor?