

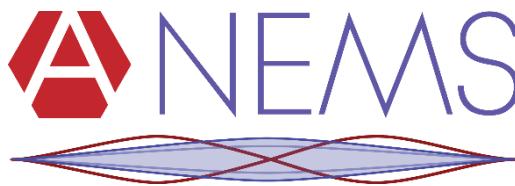
Advanced MEMS and Microsystems

LESSON 5 – MEMS Resonators

Prof. G. Villanueva

Advanced NEMS Lab (ANEMS)

EPFL-IGM NEMS



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Course content and schedule

Dates	Lectures	Lecturers	Mean
20.02	Introduction Transducers review: pre-recorded lectures	D. Briand / G. Villanueva	Live
27.02	Sensors part I Exercices	D. Briand	Live
05.03	Sensors part II Industrial seminar #1	D. Briand	Live
12.03	Students presentations	D. Briand / G. Villanueva	Live
19.03	Actuators and Optical MEMS Industrial seminar #2	D. Briand	Live
26.03	Acoustic and Ultrasonic MEMS Industrial seminar #3	G. Villanueva	Live
09.04	Acoustic and Ultrasonic MEMS	G. Villanueva	Live
16.04	RF-MEMS NEMS	G. Villanueva	Live
23.04	Interactive session	D. Briand / G. Villanueva	Live
30.04	Thermal and gas sensors Industrial seminar #4	D. Briand	Live
07.05	Packaging	D. Briand	Live
14.05	Packaging Industrial seminar #5	D. Briand	Live
21.05	PowerMEMS	D. Briand	Live
28.05	Quiz + oral exam instructions Evaluation of the course	All	Live

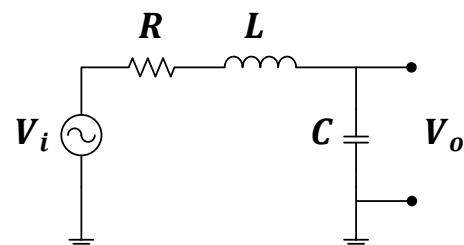
- **Introduction**
 - What is a Resonator?
 - Different applications
 - Why MEMS resonators?
 - Market perspectives
- **Types of MEMS resonators**
- **MEMS filters (passive)**
- **MEMS oscillators (active)**

What is a Resonator?

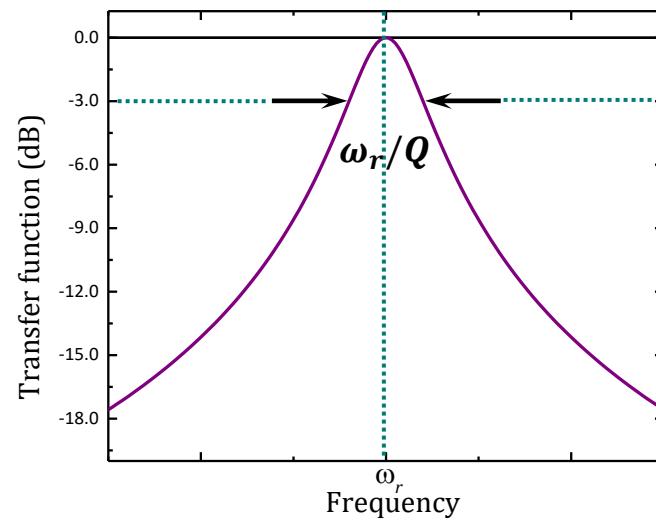
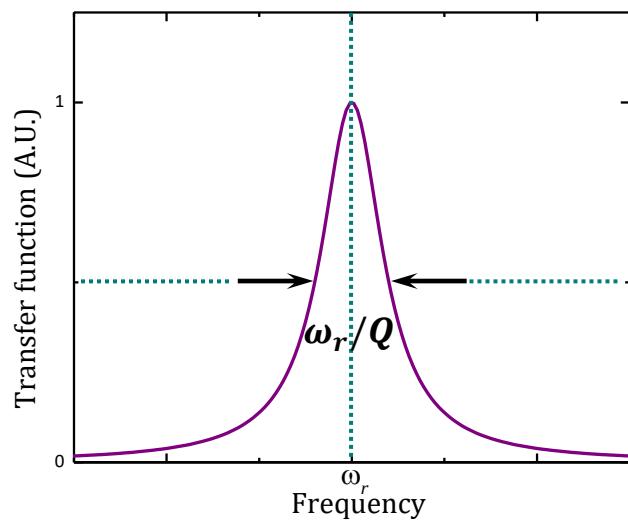
- Wikipedia says...

System that tends to oscillate with greater amplitude at some frequencies than at others

...and Wikipedia is usually right.



$$S_{21} = \left| \frac{V_o}{V_i} \right|^2 = \frac{1}{(1 - (LC\omega)^2)^2 + (\omega RC)^2}$$
$$= \frac{1}{\left(1 - \left(\frac{\omega}{\omega_r} \right)^2 \right)^2 + \left(\frac{\omega}{\omega_r Q} \right)^2}$$

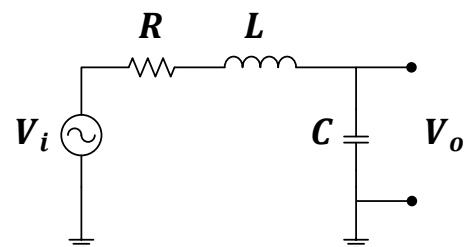


What is a Resonator?

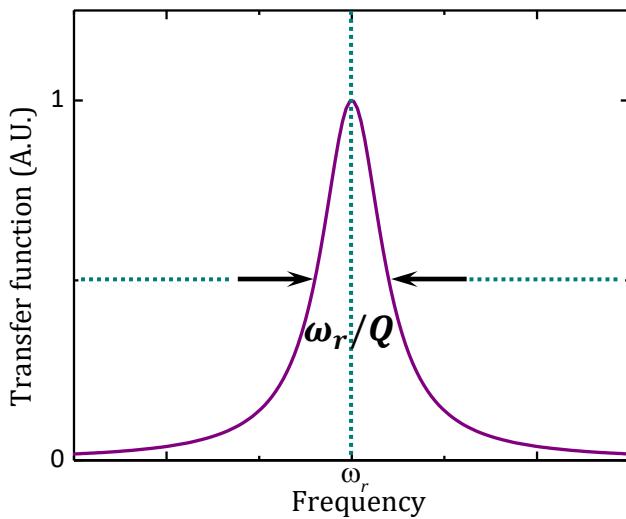
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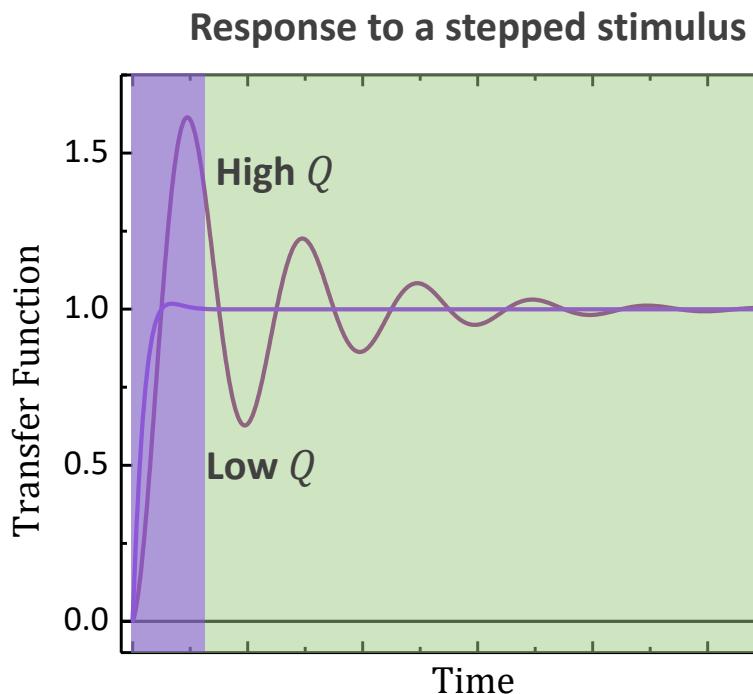
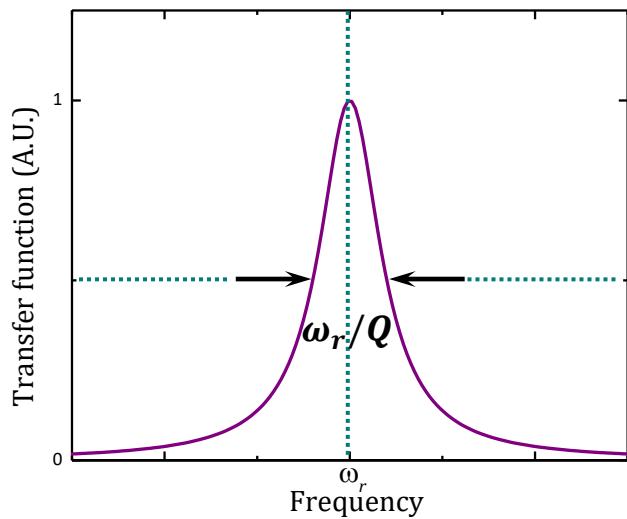
- **Q - Quality factor**
 - *Measure of how good/bad a resonator is*
 - $Q = 2\pi \frac{E_{stored}}{E_{lost}}$; $Q = \frac{\omega_r}{FWHM}$; $Q = \frac{S_{21}(\omega_r)}{S_{21}(\omega=0)}$
 - *Establishes level of interaction with the “outside”*

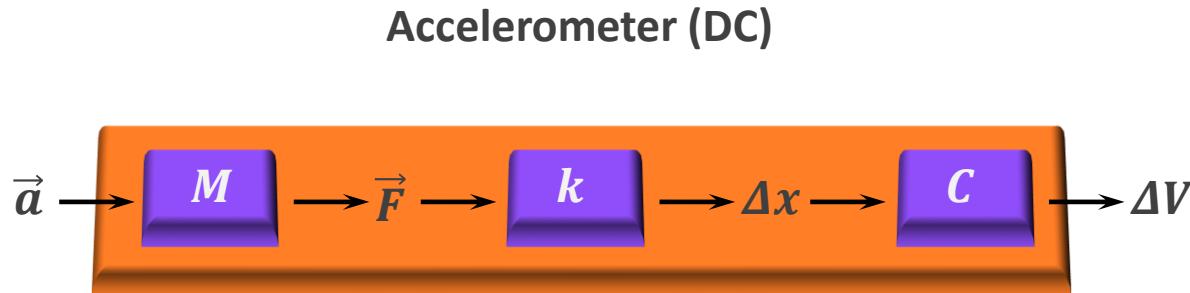
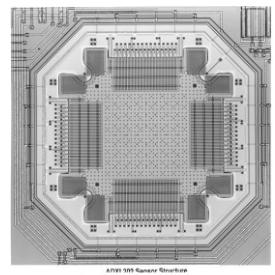
- It depends on the application
- Trade-off
 - Less influence from external noise
 - Time required to settle down the transients
 - Every mechanical structure has resonances

$$\tau \sim 2\pi \frac{Q}{\omega_r}$$

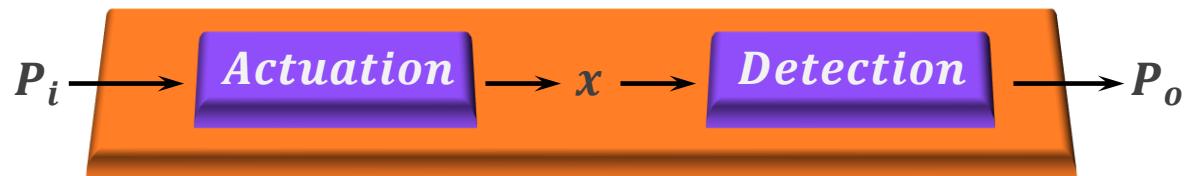
If your application “resonates” – then better as high as possible

↓
Resonator

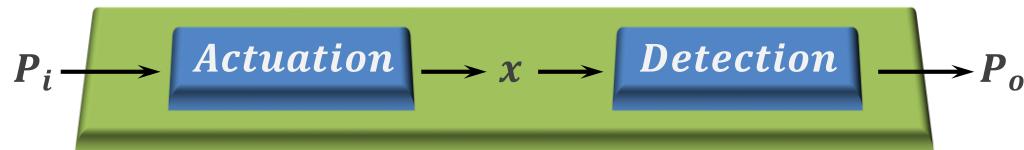




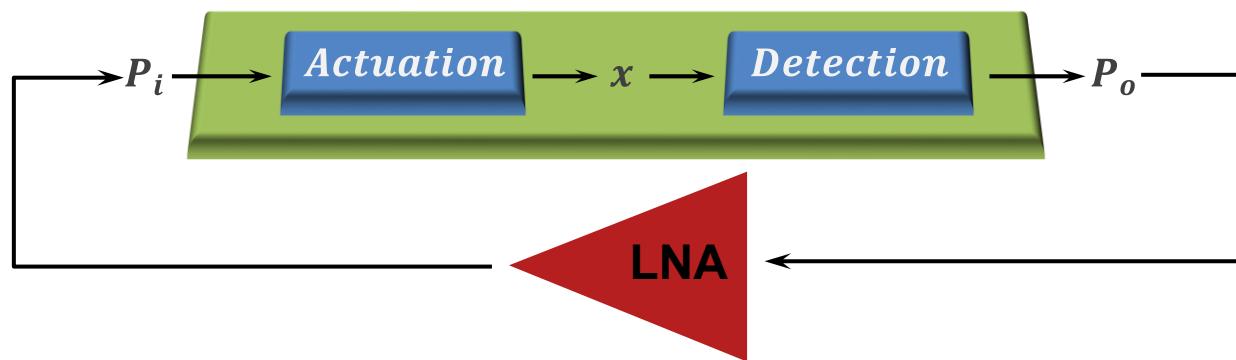
MEMS Resonator



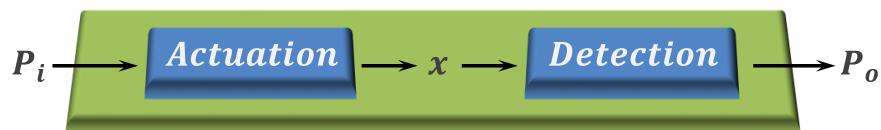
RF Filter



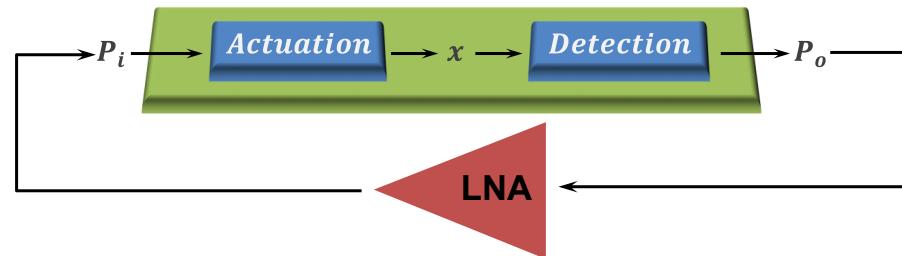
Oscillator



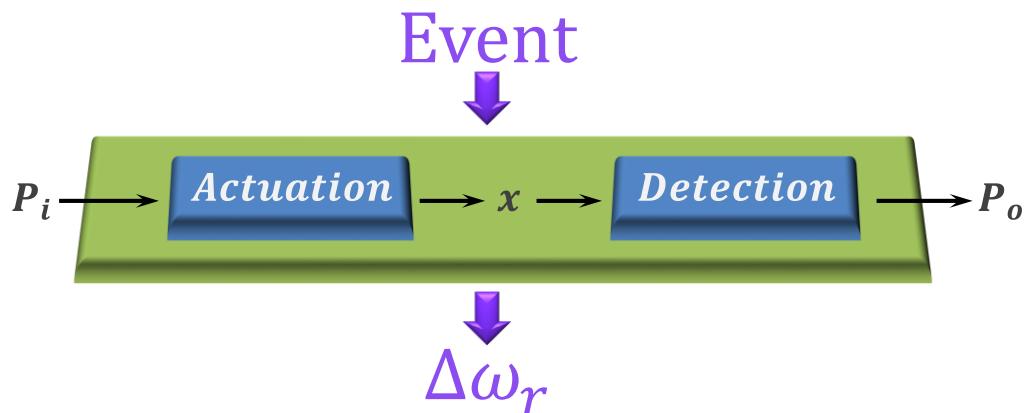
RF Filter



Oscillator

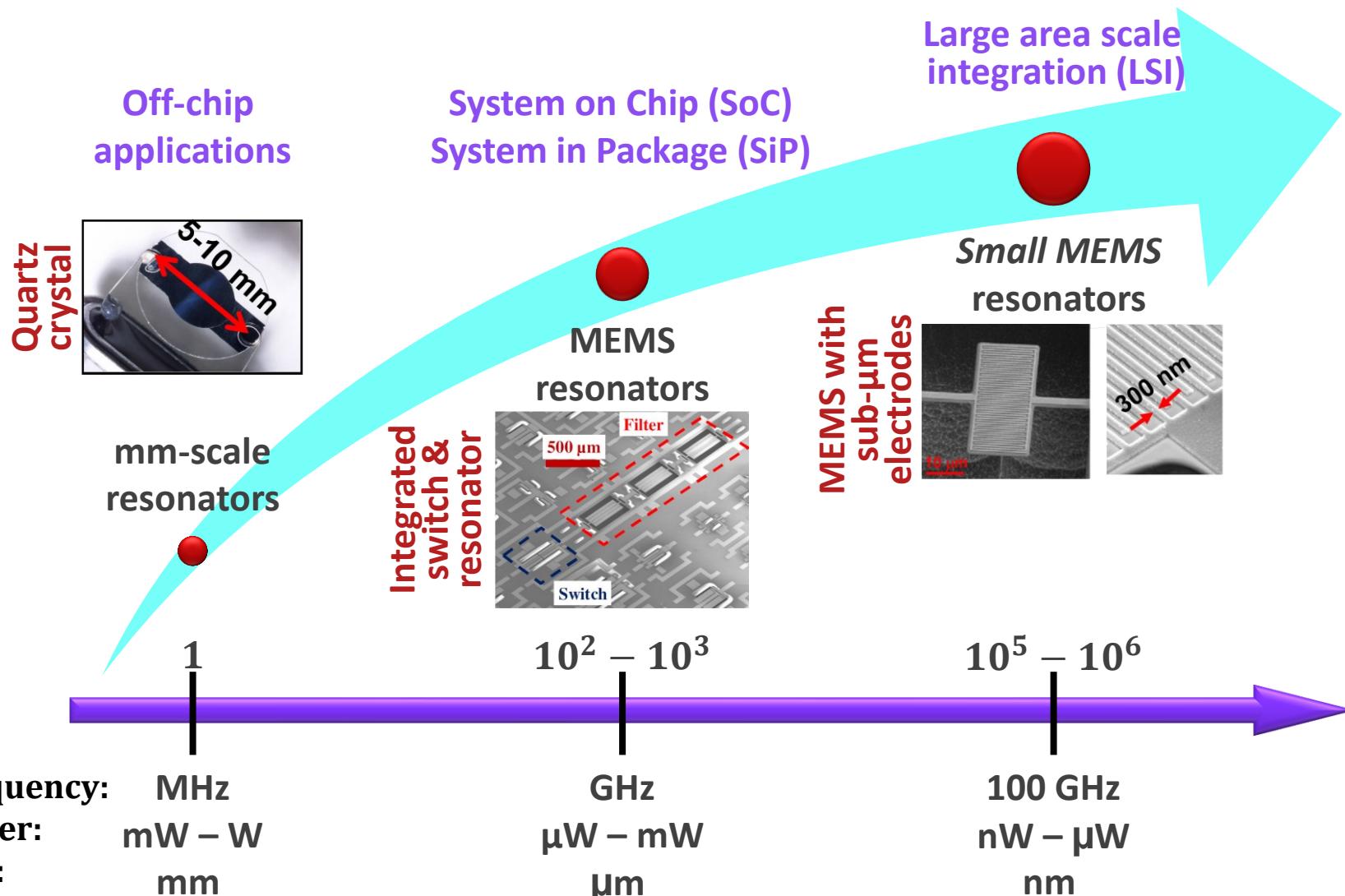


Resonant sensor



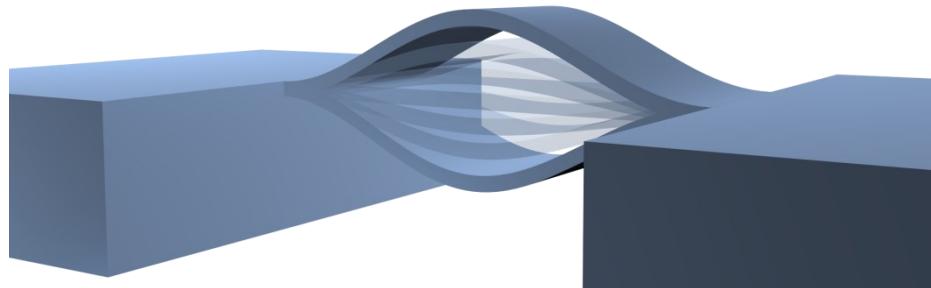
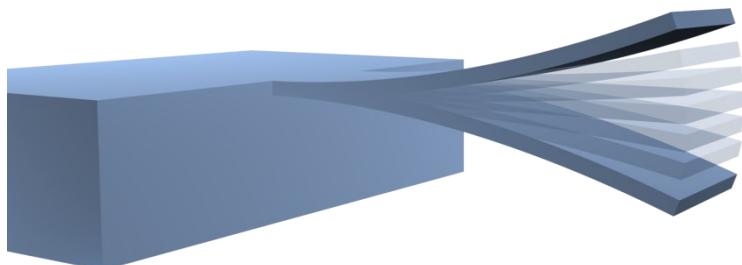
What kind of event could it be?

Why MEMS resonators?



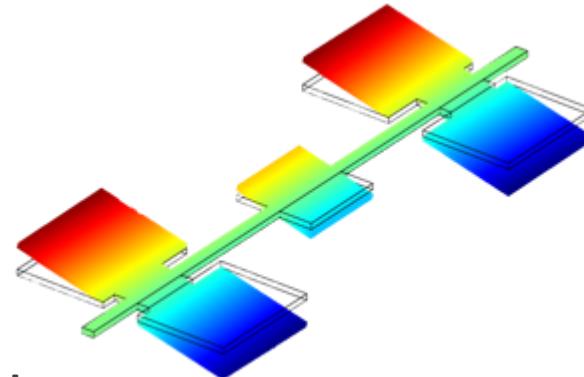
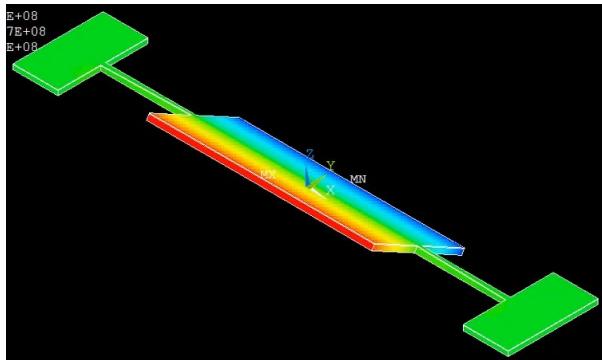
Source: Prof. G. Piazza

TYPES OF MEMS RESONATORS



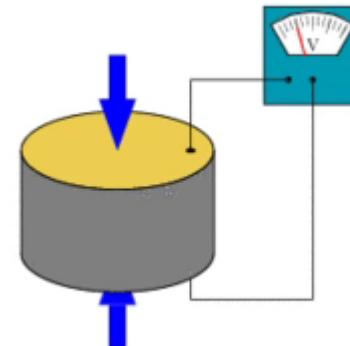
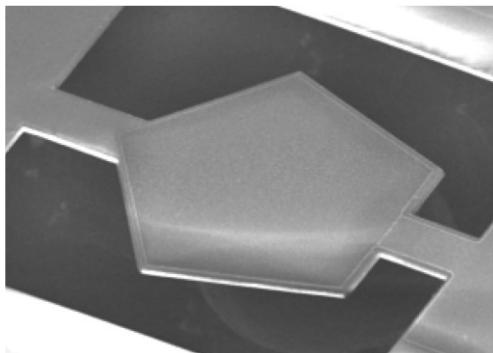
- Bending of mechanical structures is involved
- 1D: cantilevers (C-F), beams (C-C), free-free (F-F); 2D: membranes (CCCC), plates (CFFF)
- Equation of motion is a 4th order differential equation
 - Solution is a combination of trigonometric and hyperbolic functions
- Typical frequencies: 10kHz – 100MHz
- Applications: Low frequency oscillators, sensors
- Advantages:
 - Intuitive and clear understanding of motion
 - Low mass – preferred for sensing
- Disadvantages: gas or liquid damping is very important

$$f \propto \sqrt{\frac{E}{\rho} \frac{t}{L^2}}$$



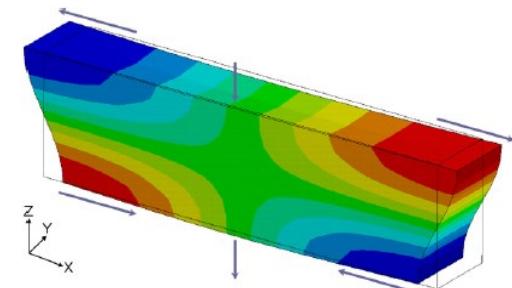
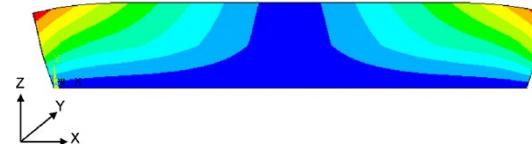
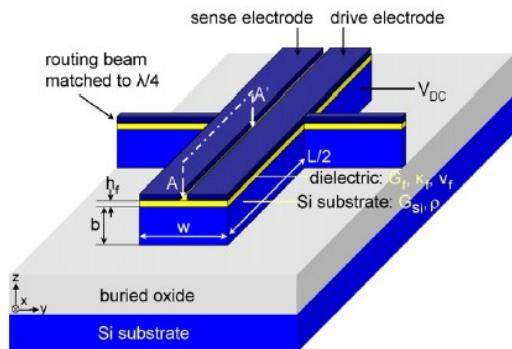
- Motion based on torsion, torque-based movement
- Usually paddle-like structures
- Equation of motion is a 2nd order differential equation
 - Solution is a combination of trigonometric functions
- Typical frequencies: 10kHz – 10MHz
- Applications: Low frequency oscillators, sensors
- Advantages:
 - Intuitive and clear understanding of motion
 - Low interaction with substrate (thin supporting rods)
- Disadvantages: very fragile and costly to fabricate (very thin rods)

$$f \propto \sqrt{\frac{G}{\rho}} \sqrt{\frac{t^3}{L_r L_p W_p^3}}$$



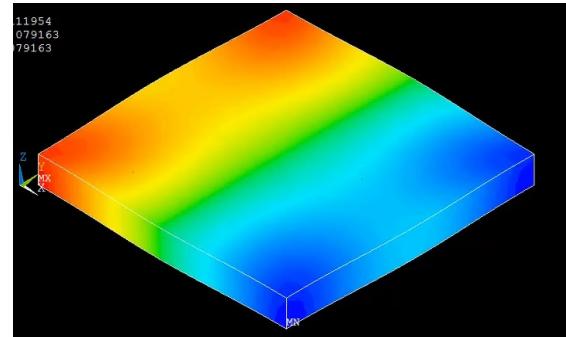
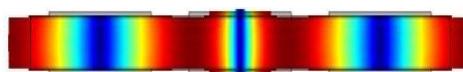
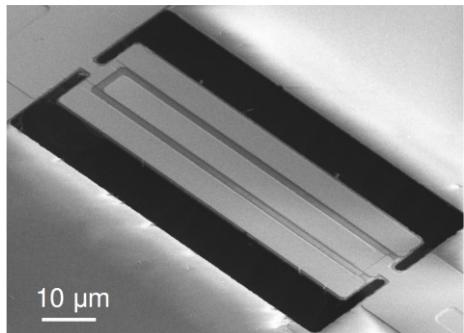
- Acoustic waves constructive interaction
- Movement is 3D (due to Poisson's ratio) – Reduced to 1D if $w > t$
- Equation of motion is a 2nd order differential equation – wave equation
 - Solution is a trigonometric function, Frequencies are multiples
- Typical frequencies: 100MHz – 10GHz
- Applications: Filters, Oscillators
- Advantages:
 - High frequency, high Q
 - Easy electromechanical modelling
- Disadvantages:
 - Complicated design (to trim properties)
 - One frequency per wafer

$$f \propto \sqrt{\frac{E}{\rho} \frac{n}{t}}$$



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- Advantages:
 - High frequency, high Q
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- Disadvantages:
 - Complicated design (to trim properties)
 - Even less intuitive than previous one

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- Acoustic waves constructive interaction
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 - Solution is a trigonometric function, Frequencies are multiples
- Typical frequencies: 100MHz – 10GHz
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- Advantages:
 - Frequency defined by lithography, high frequency, high Q
 - Easy electromechanical modelling
- Disadvantages:
 - Complicated design (to trim properties)

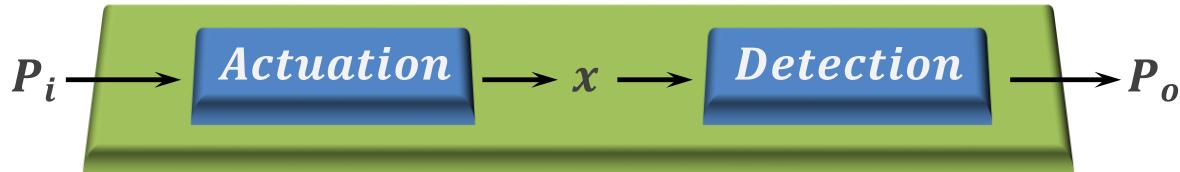
$$f \propto \sqrt{\frac{E}{\rho}} \frac{n}{w}$$

Types of MEMS Resonators

Type	Frequency	Example
Flexural	$f \propto \sqrt{\frac{E}{\rho} \frac{t}{L^2}}$	100 kHz – 100 MHz
Torsional	$f \propto \sqrt{\frac{G}{\rho}} \sqrt{\frac{t^3}{L_r L_p W_p^3}}$	10 kHz – 10 MHz
Thickness	$f \propto \sqrt{\frac{E}{\rho} \frac{n}{t}}$	
Shear	$f \propto \sqrt{\frac{G}{\rho} \frac{n}{t}}$	100 MHz – 10 GHz
Lateral	$f \propto \sqrt{\frac{E}{\rho} \frac{n}{w}}$	

$$Q = 2\pi \frac{E_{stored}}{E_{lost}}$$

- **Viscous damping**
 - Displacement of gas or liquid molecules
 - Pressure and mode-shape dependent
- **Anchoring losses**
 - Radiation of energy to the substrate
 - Minimized using phononic crystals (artificial mirror for acoustic energy)
- **Material losses**
 - Surface states
 - Volume losses
 - Defects motion
 - Thermo-elastic damping
 - Akhiezer effect (electro-phonon dissipative coupling)

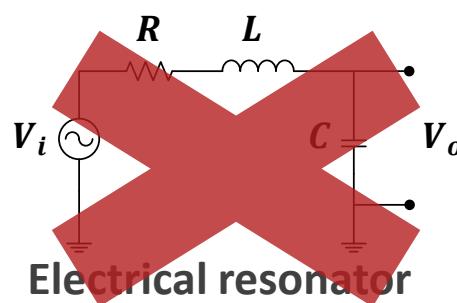
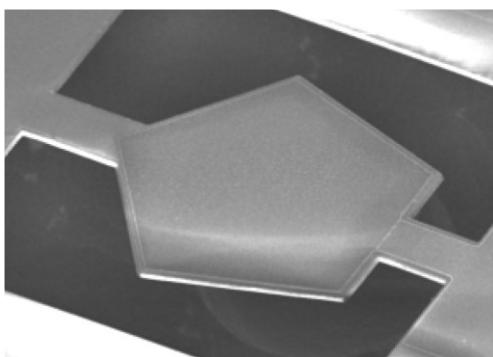
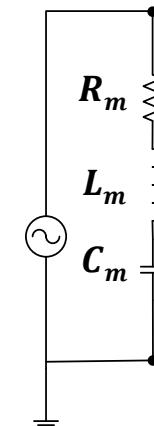
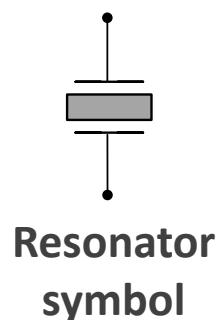
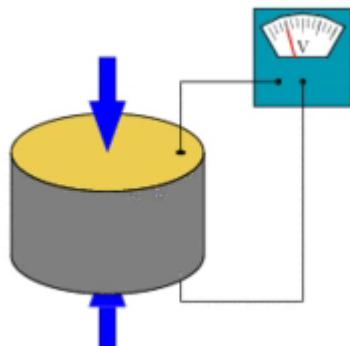


- Capacitive/Electrostatic
- Thermal
- Piezoresistive
- **Piezoelectric**
- Electrostrictive
 - Polarizing a dielectric material – effectively turning it piezoelectric

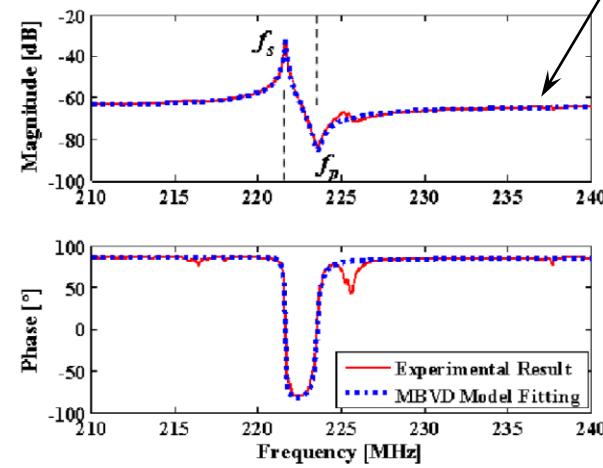
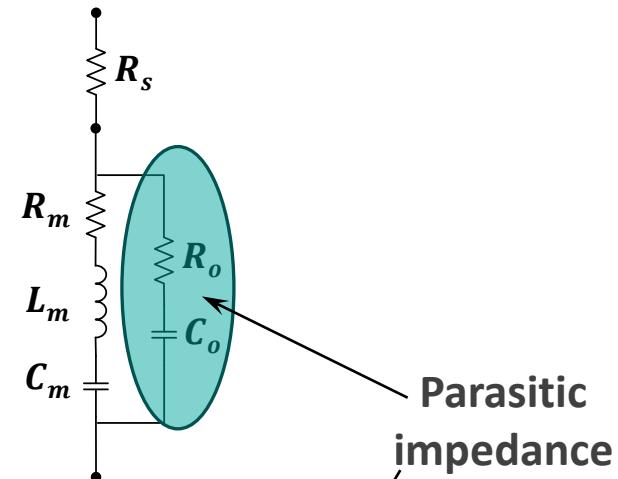
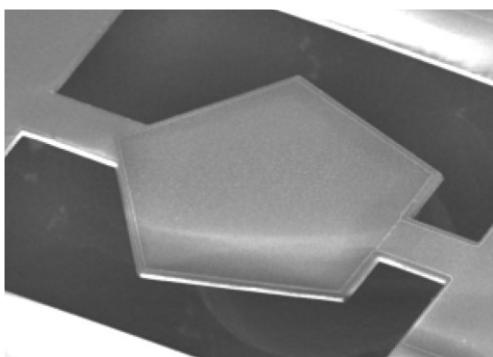
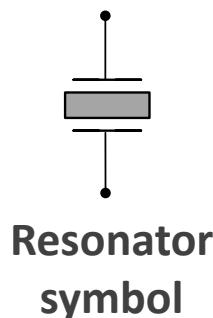
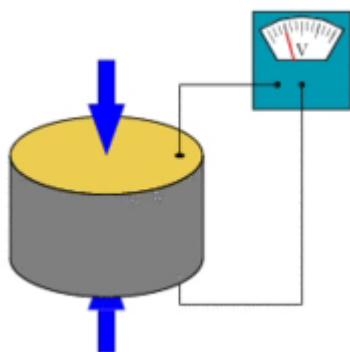
- {
- Non dissipative
 - Based on material property
 - No need for external DC
 - Good scaling with frequency

- It's difficult to compare “*apples and oranges*”
- Figures Of Merit (*FOM*)
 - Useful to get much information into a single parameter
- $FOM_1 = f_r \cdot Q$
 - Determines which resonator would work better as an *oscillator*
 - It can be seen that there is kind-of a trade-off between f_r and Q
- $FOM_2 = k_t^2 \cdot Q$
 - k_t^2 measures how much mechanical energy gets converted into electrical energy
 - This *FOM* determines which resonator would work better as a *filter*
 - Piezoelectric resonators have the highest values

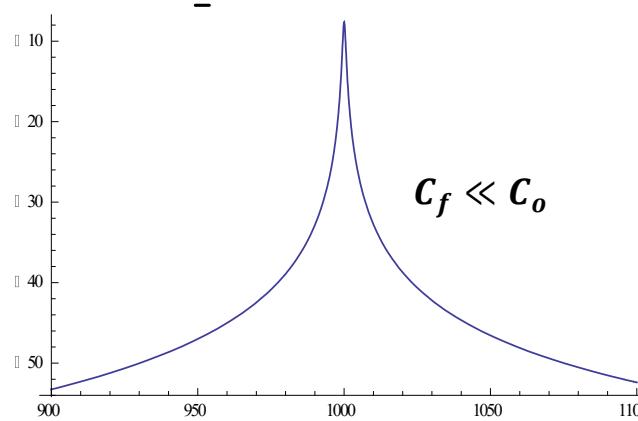
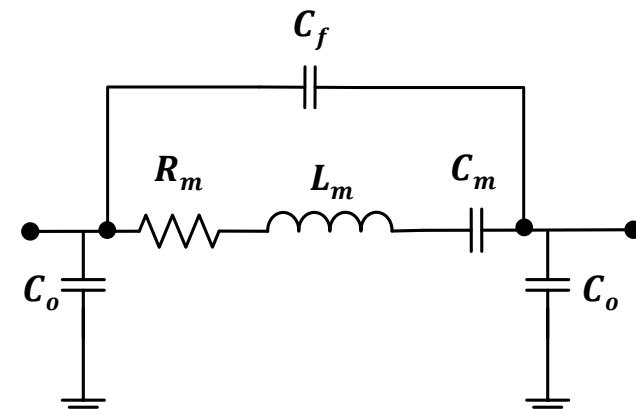
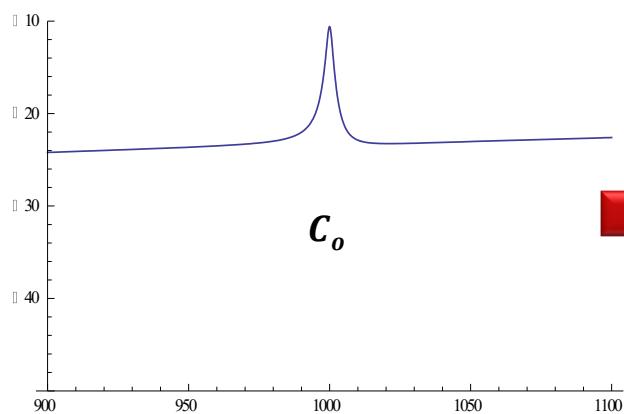
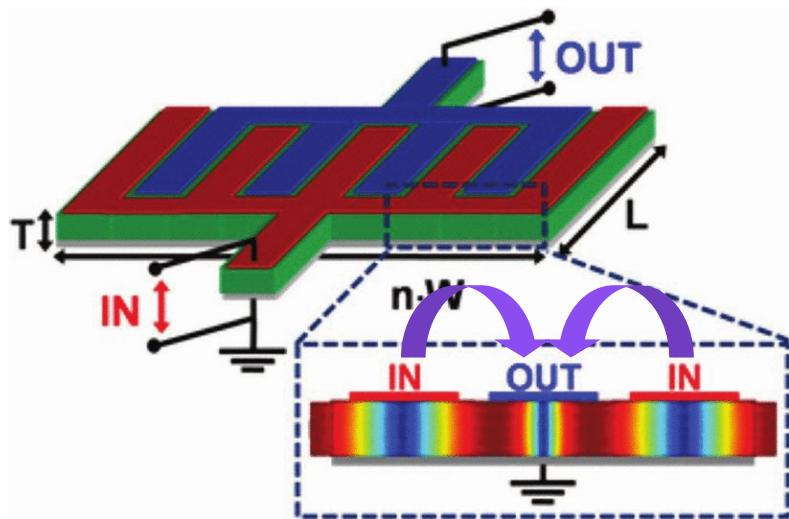
- **Equivalent circuit**
 - Allows to reproduce mechanical resonator behavior with circuit simulation tools
- Historically, the first one to be developed was a 1-port model for Quartz crystals



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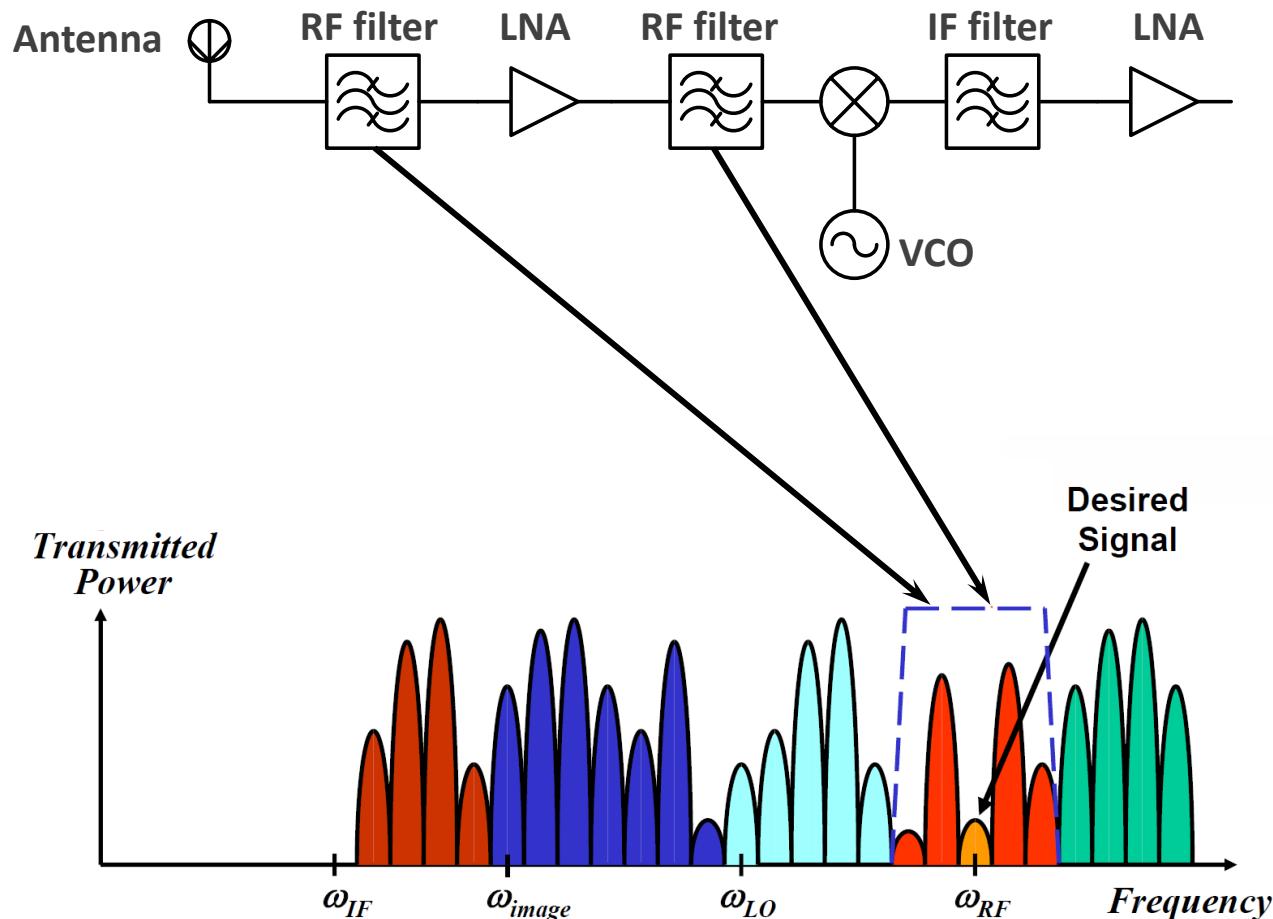


- In order to reduce the effect of parasitics
 - Two separate ports for excitation and readout

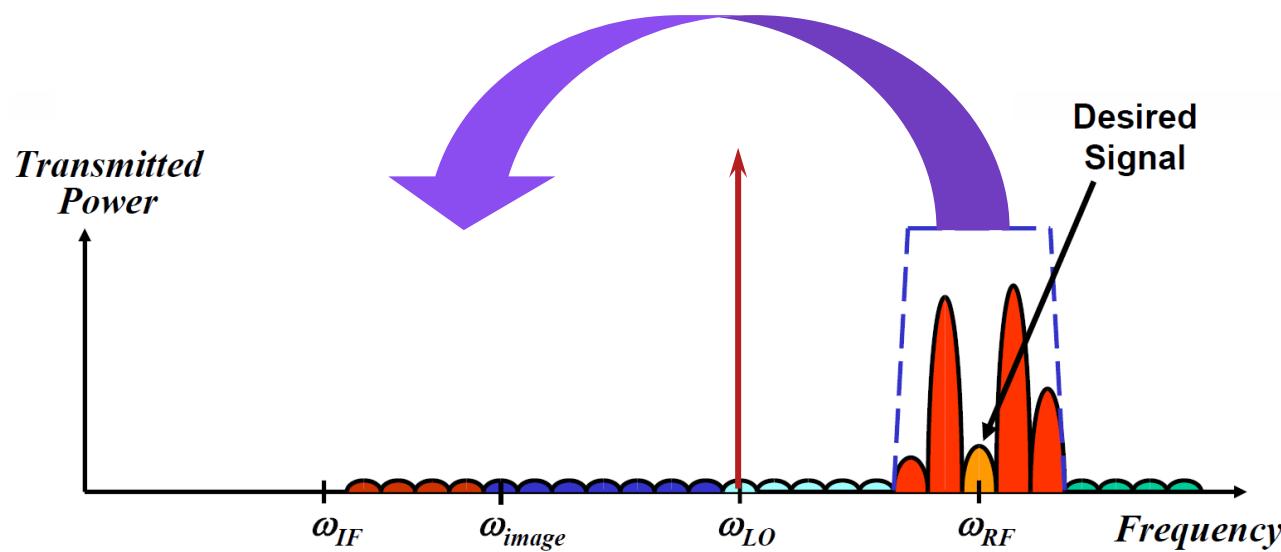
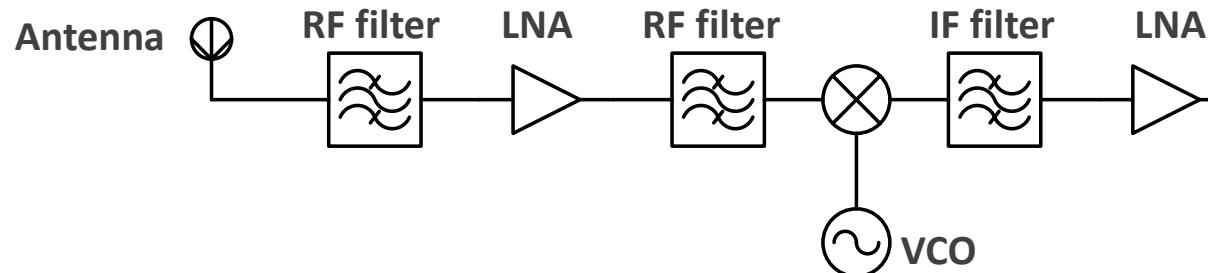


MEMS RF-FILTERS

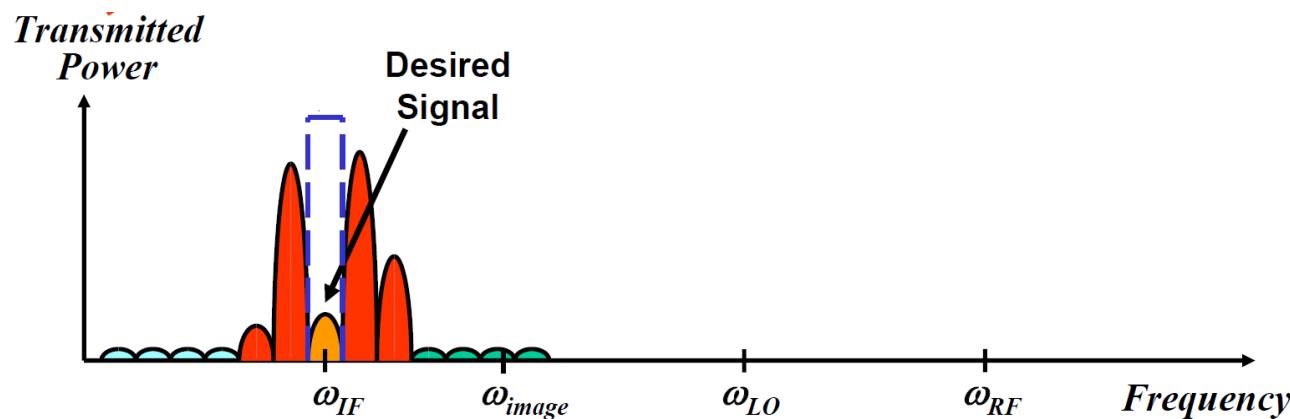
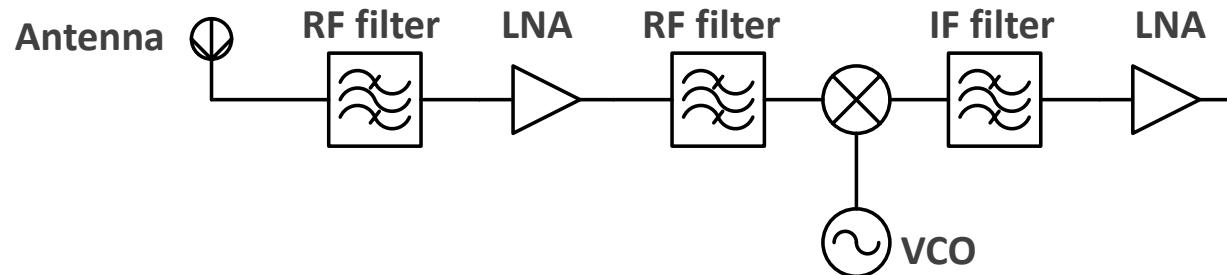
- Typically – Receivers work using heterodyne conversion



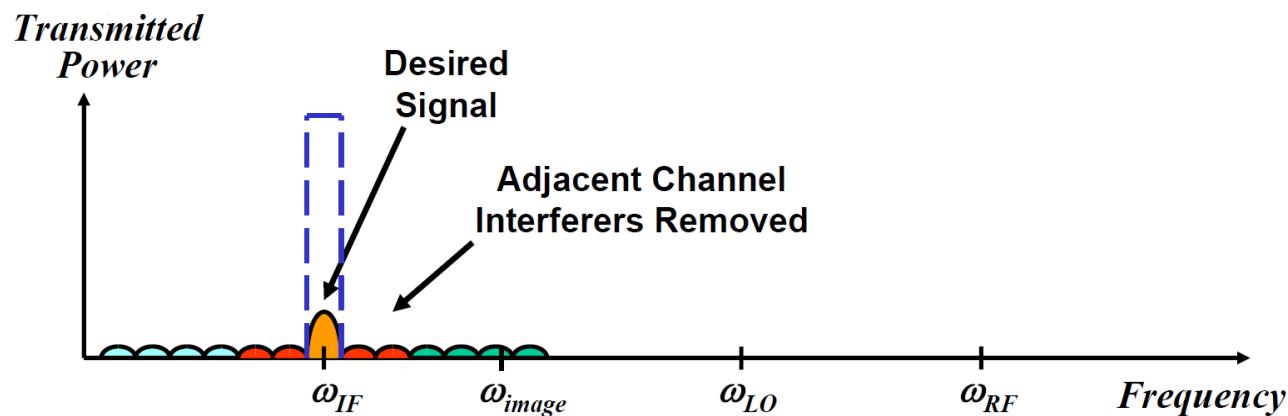
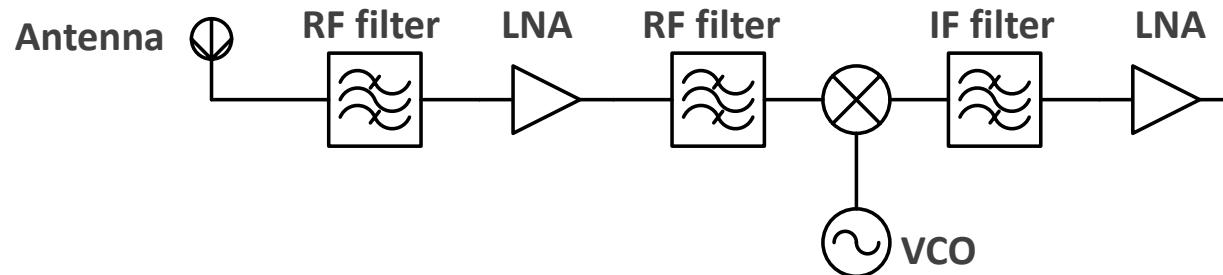
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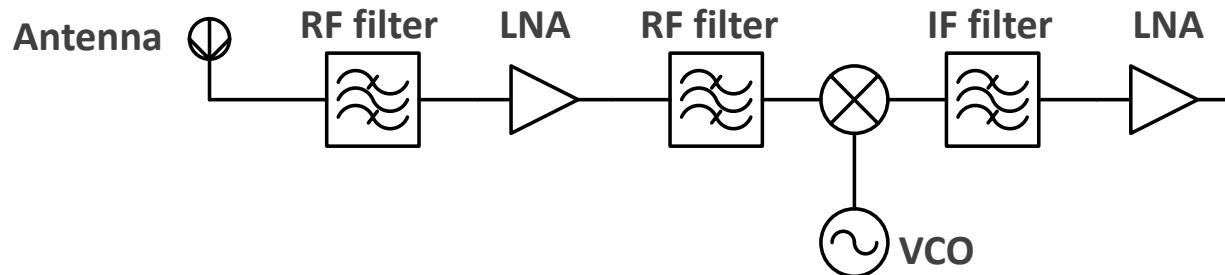
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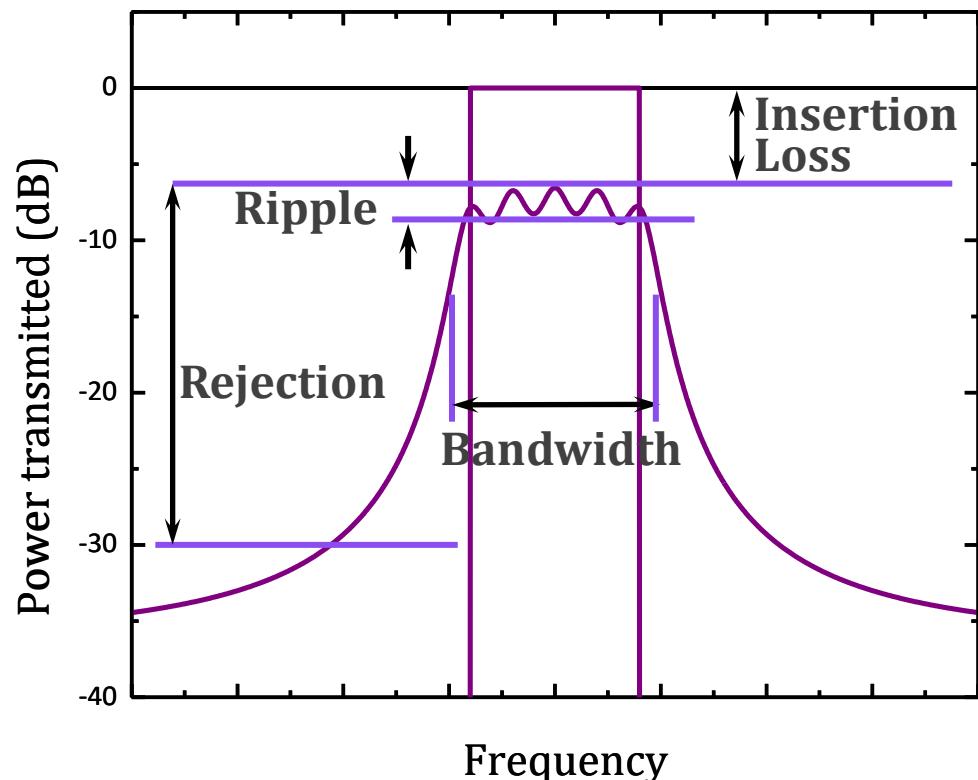


- Typically – Receivers work using heterodyne conversion

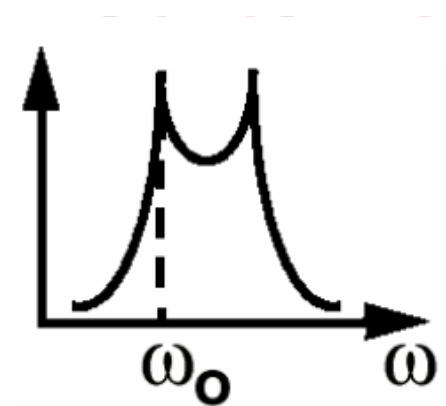
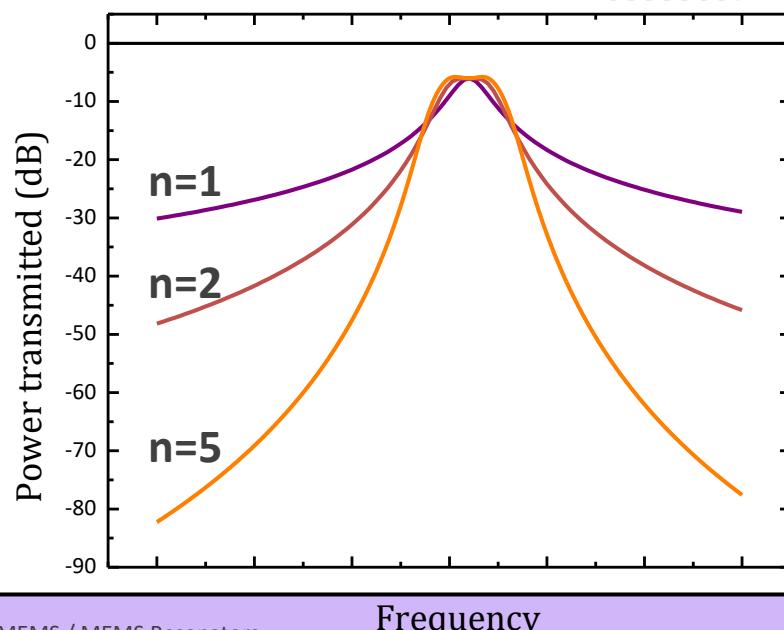
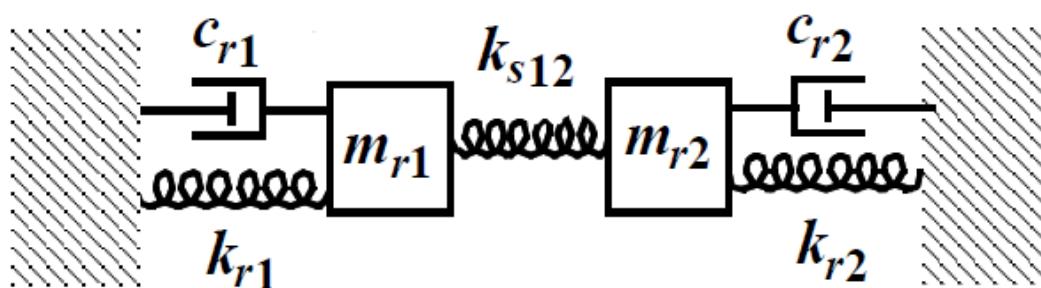


- It is necessary to do conversion down to IF because at RF, Qs are not good
- With RF-MEMS filters – Direct filtering is possible

- Ideal is a rectangular filter
- Filter design focus is mainly on
 - Insertion loss (and ripple)
 - Bandwidth
 - Rejection
 - Impedance
- Arrays of coupled resonators
 - High Q = high rejection
 - Separation = Bandwidth
- Coupling can be
 - Electrical
 - Mechanical
 - Acoustical



- Basic idea
 - 2 coupled resonators
 - Symmetric and Anti-Symmetric motion
 - New frequencies are defined by coupling factor

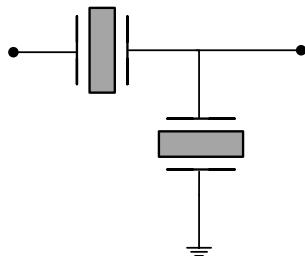


Sharper rejection for a larger Bandwidth with more coupled resonators

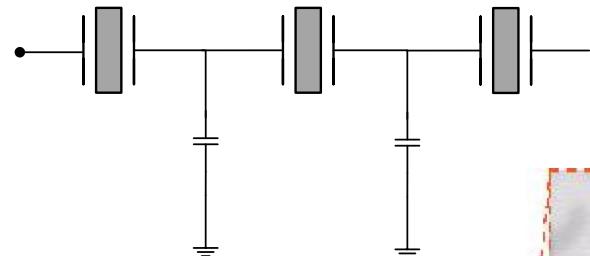
Coupling for filters

- **Electrical**

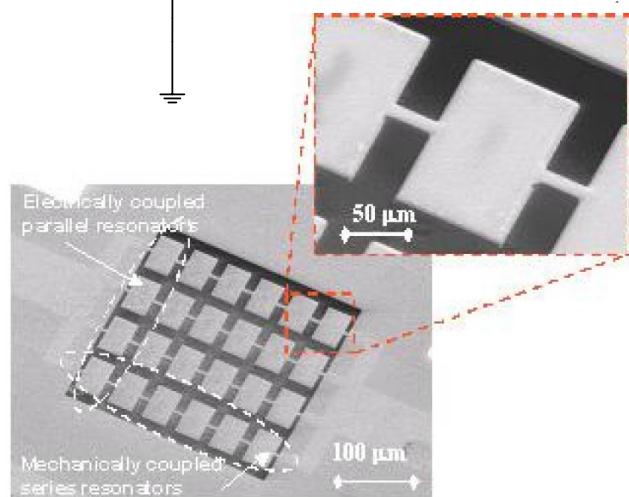
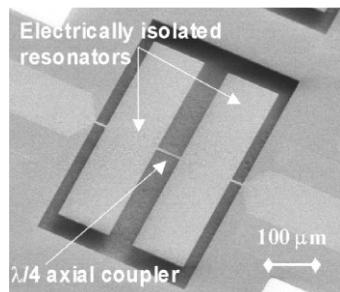
- **Ladder-like**



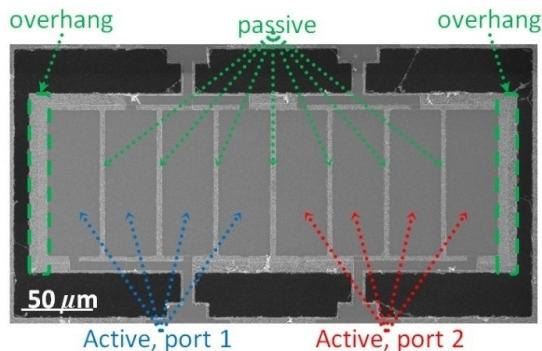
- **Series**



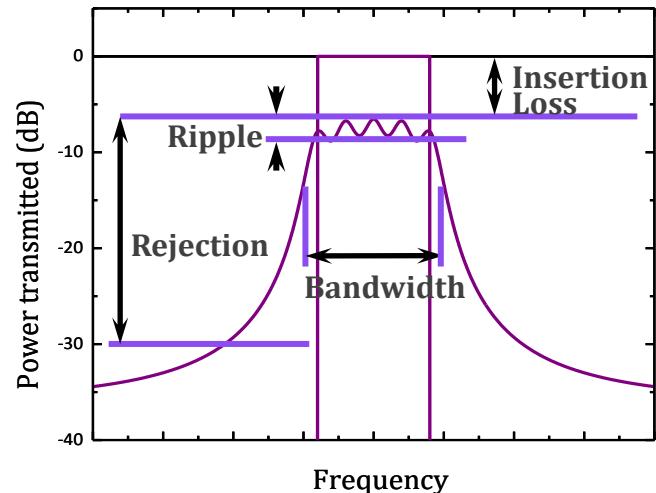
- **Mechanical**



- **Acoustic**



- Depends on transduction and geometry
- Piezoelectric contour-mode resonators:
 - Bandwidth
 - Set by the electromechanical coupling coefficient
 - Insertion Loss
 - Set by $FOM_2 = k_t^2 \cdot Q$
 - Rejection
 - Controlled by parasitics (C_f)
 - Impedance
 - Termination capacitance, can be tuned



$$BW \sim \frac{3}{\pi^2} k_t^2$$

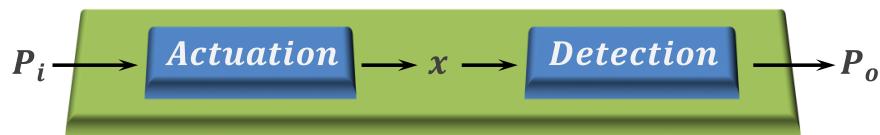
$$IL \sim -20 \log \left(\frac{4}{4 + (3\pi^2)/(k_t^2 Q)} \right)$$

$$Reject \sim -20 \log \left(\frac{C_f}{C_o} \right) - IL$$

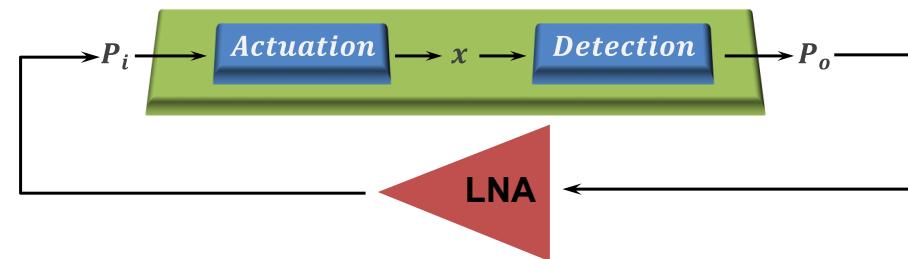
$$IL \sim \left| \frac{1}{j\omega_c C_o} \right|$$

MEMS OSCILLATORS

Passive/Resonator

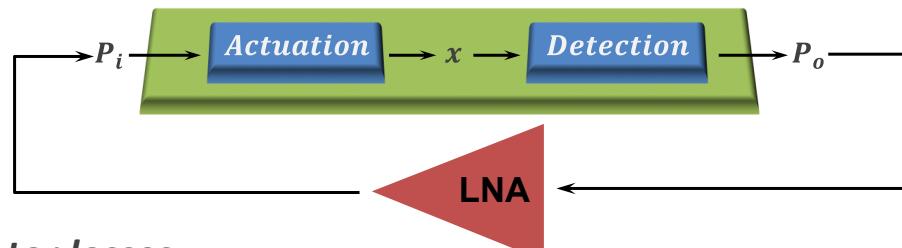


Active/Oscillator

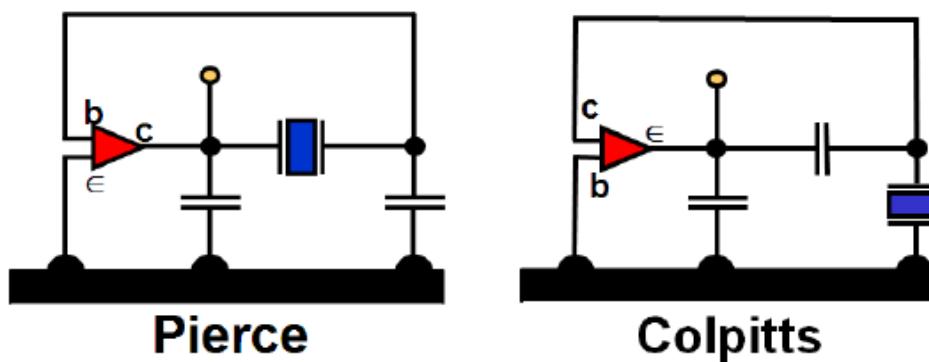


- Power output linearly depends on power input
- Requires a harmonic drive to have response

- Outputs a harmonic signal by only applying DC power



- Idea
 - Amplify P_o enough to *compensate resonator losses*
 - Feed it back to device with *appropriate phase*
 - *Barkhausen's criteria*
- Two simplest implementations
 - Pierce & Colpitts oscillators
 - 1 transistor, 2 capacitors – oscillator is running!

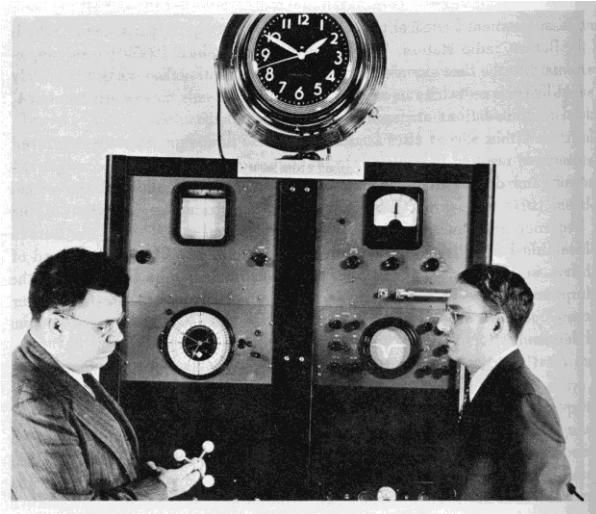


Application I - Timekeeping

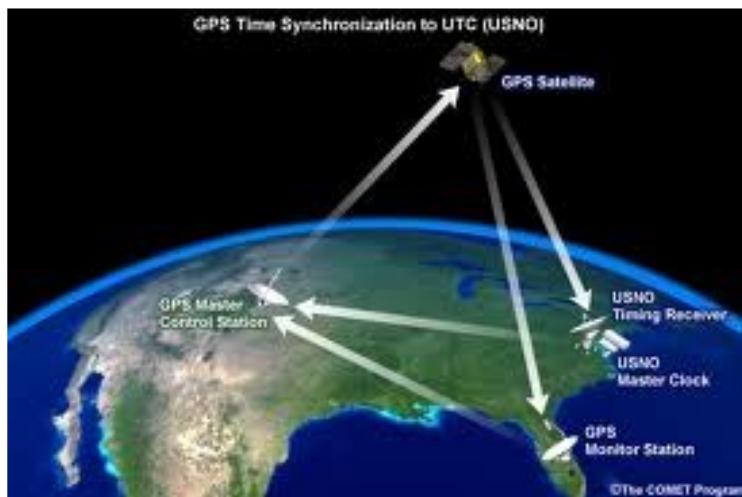
- Every watch has an oscillator inside – to keep track of time
- Oscillator's beats are later translated into seconds (e.g. by a counter)
- For a precise watch – necessary a precise oscillator
- Precision is required in the long term (this is important)



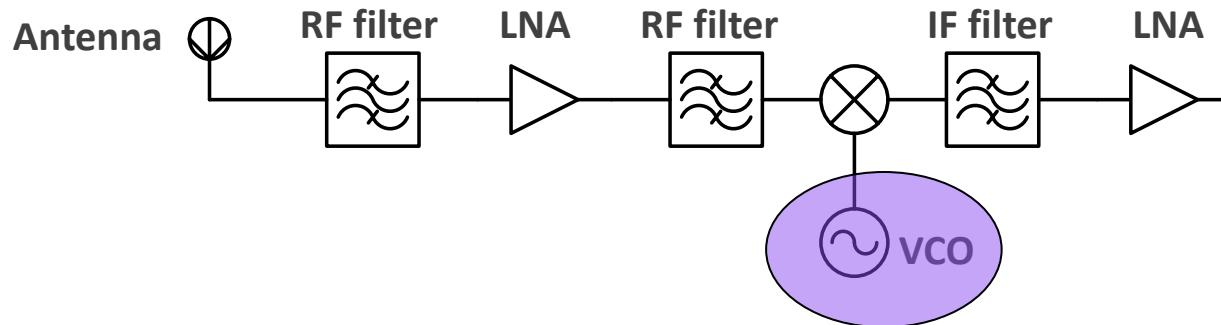
- What is the most precise clock?
 - Atomic Clock – 30 fs error per day!!!!



- Applications that require very high precision?
 - Geolocation (GPS, Galileo...)
 - Radar, LiDAR,...



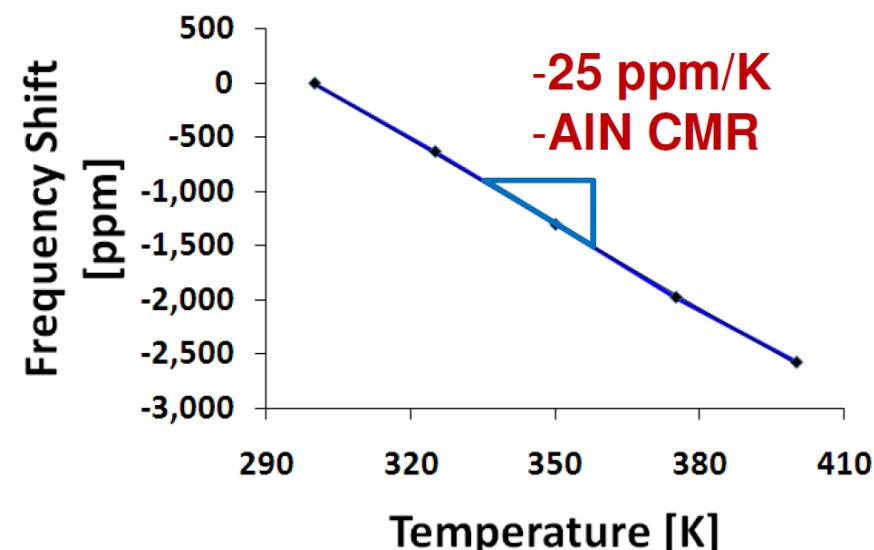
- Communications
 - Front-End/Receiver



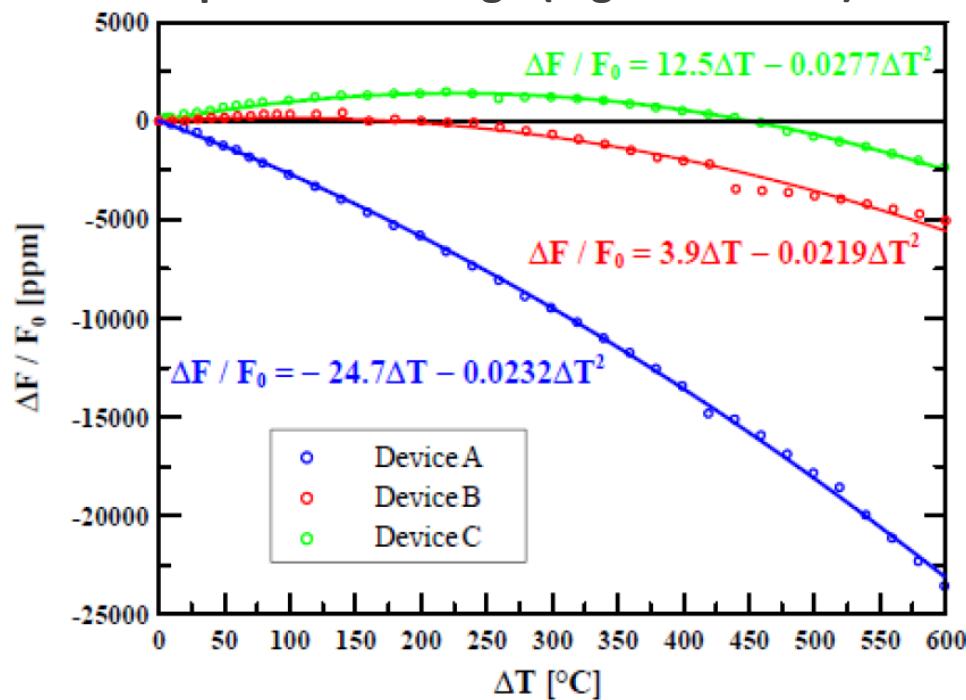
- Oscillator signal is used to encode and decode signals
- Clean communication needs a precise oscillator
- Precision is important at very short timescales, < 1 ms

- Phase noise
- Temperature stability
- Acceleration stability
 - Vibrations affect resonant frequency
 - $f = f_0(1 + \Gamma \cdot |\vec{a}|)$
 - $\Gamma \sim 10^{-5} \text{g}^{-1}$ for most MEMS devices
- Power consumption
 - More autonomous devices
 - Stand-by and clocking applications
 - 32.768 kHz ($= 2^{15} \text{Hz}$)
 - $\sim 1 \mu\text{W}$
- Size
 - Smaller footprint = Cheaper

- Frequency depends on temperature
 - $f = f_0(1 + \text{TCF} \cdot \Delta T)$
- TCF can have different origins
 - Change in Young's modulus $\partial E / \partial T$
 - Change in volume/dimensions/density $\alpha = \partial L / \partial T$
 - Change in tension, surface stress, etc.
- Specification asks for ~ 10 ppm over the whole operational range (e.g. $-30 - 70^\circ\text{C}$)
 - $\partial E / \partial T \sim \pm 10$ ppm/K!!!!!!
- Solutions for compensation
 - Quartz crystals get special cuts

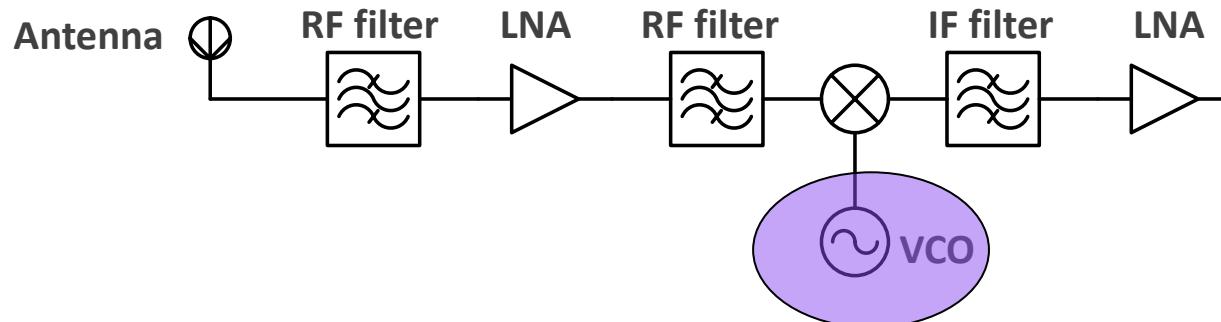


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 - MEMS – hybrid structures to balance (using positive and negative $\partial E / \partial T$)
 - Not linear over wide T range

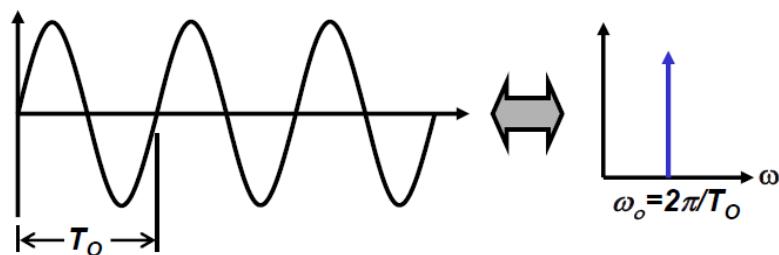


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- Solutions for compensation
 - Quartz crystals get special cuts
 - MEMS – hybrid structures to balance (using positive and negative $\partial E / \partial T$)
 - Not linear over wide T range
 - Circuit compensation
 - Use external circuit to detect T and correct the frequency
 - Best results but causes Power consumption to increase
 - Cheaper resonators

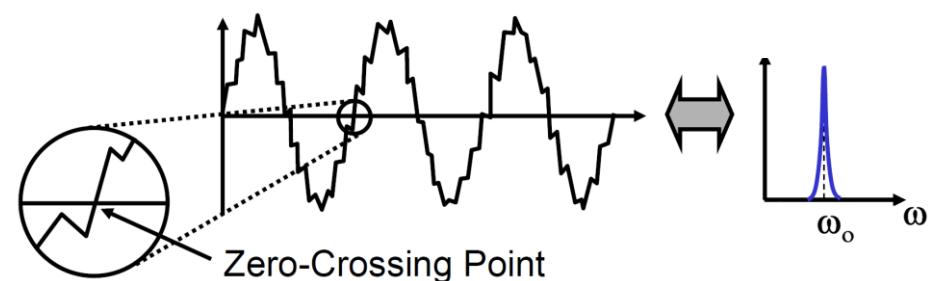
- Communications

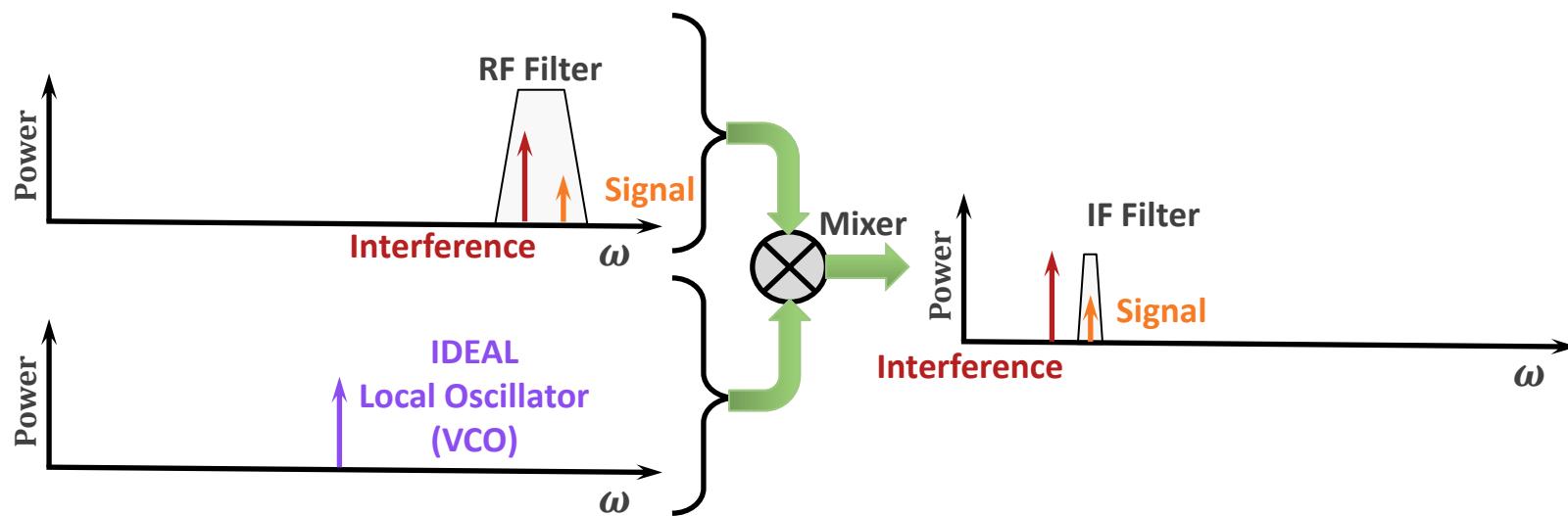
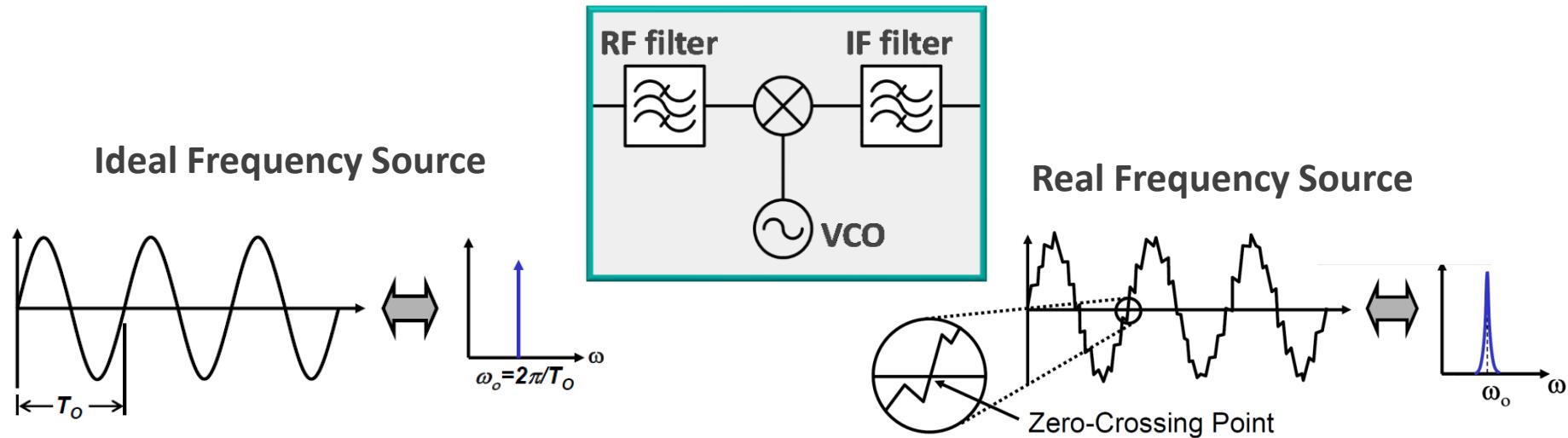


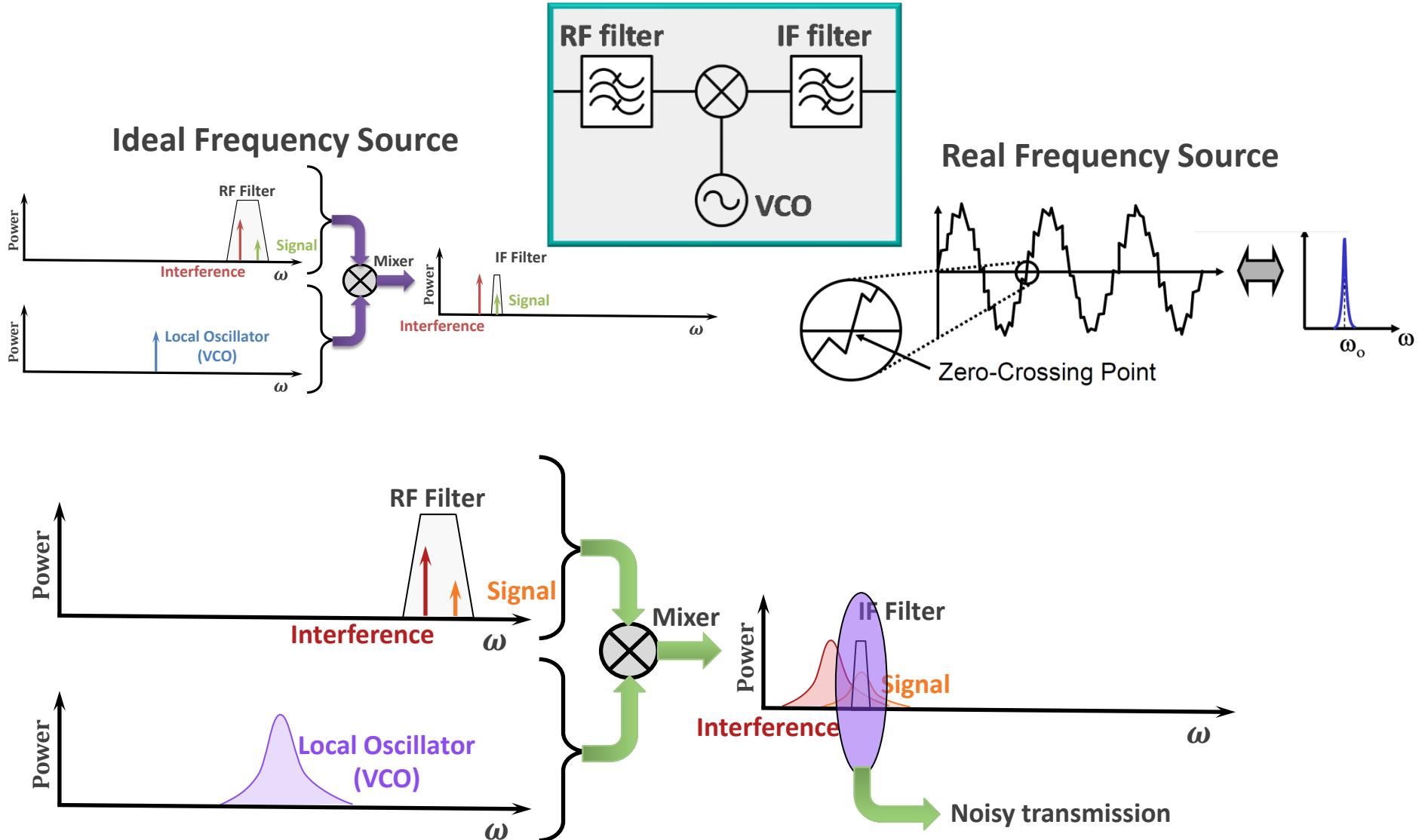
Ideal Frequency Source



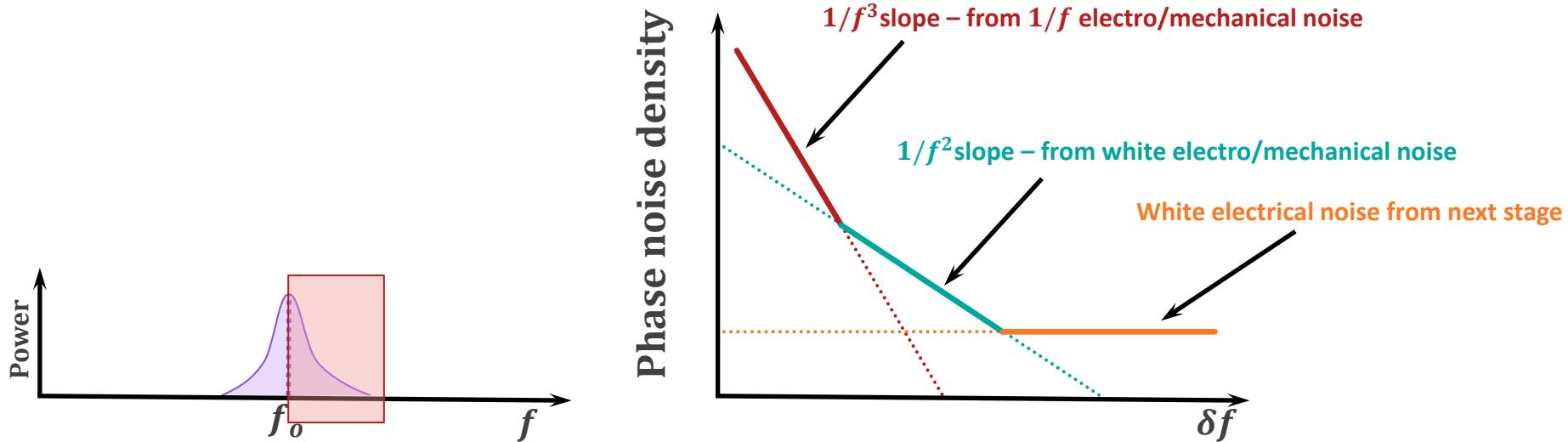
Real Frequency Source







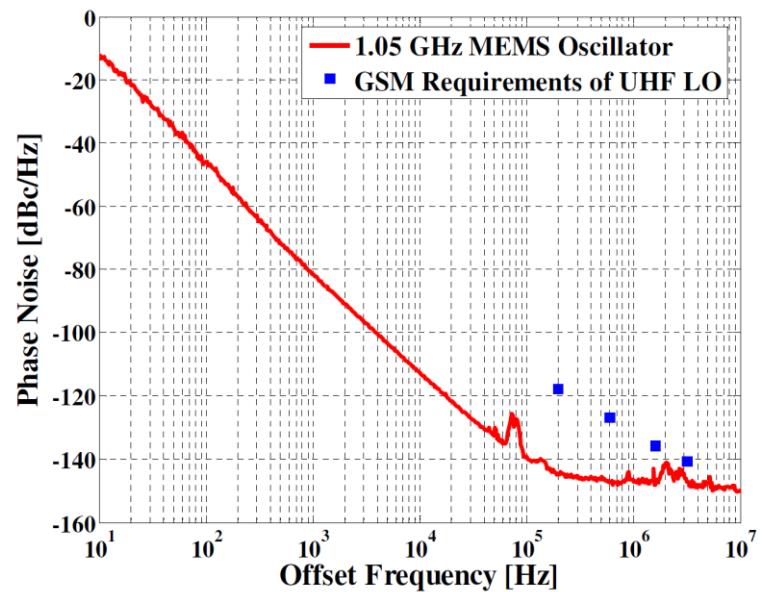
- Phase noise determines the precision of the oscillator
 - How accurate the generated frequency signal is
- It is measured in relative power to the total carrier power per Hz
 - $\frac{dBc}{Hz}$
- Leeson's formula
 - $S_\phi(\delta f) = 10 \log \left(F \frac{k_B \cdot T \cdot f_0}{Q \cdot E} \frac{1}{\delta f^2} \right)$
 - Incomplete, needs some modifications/additions

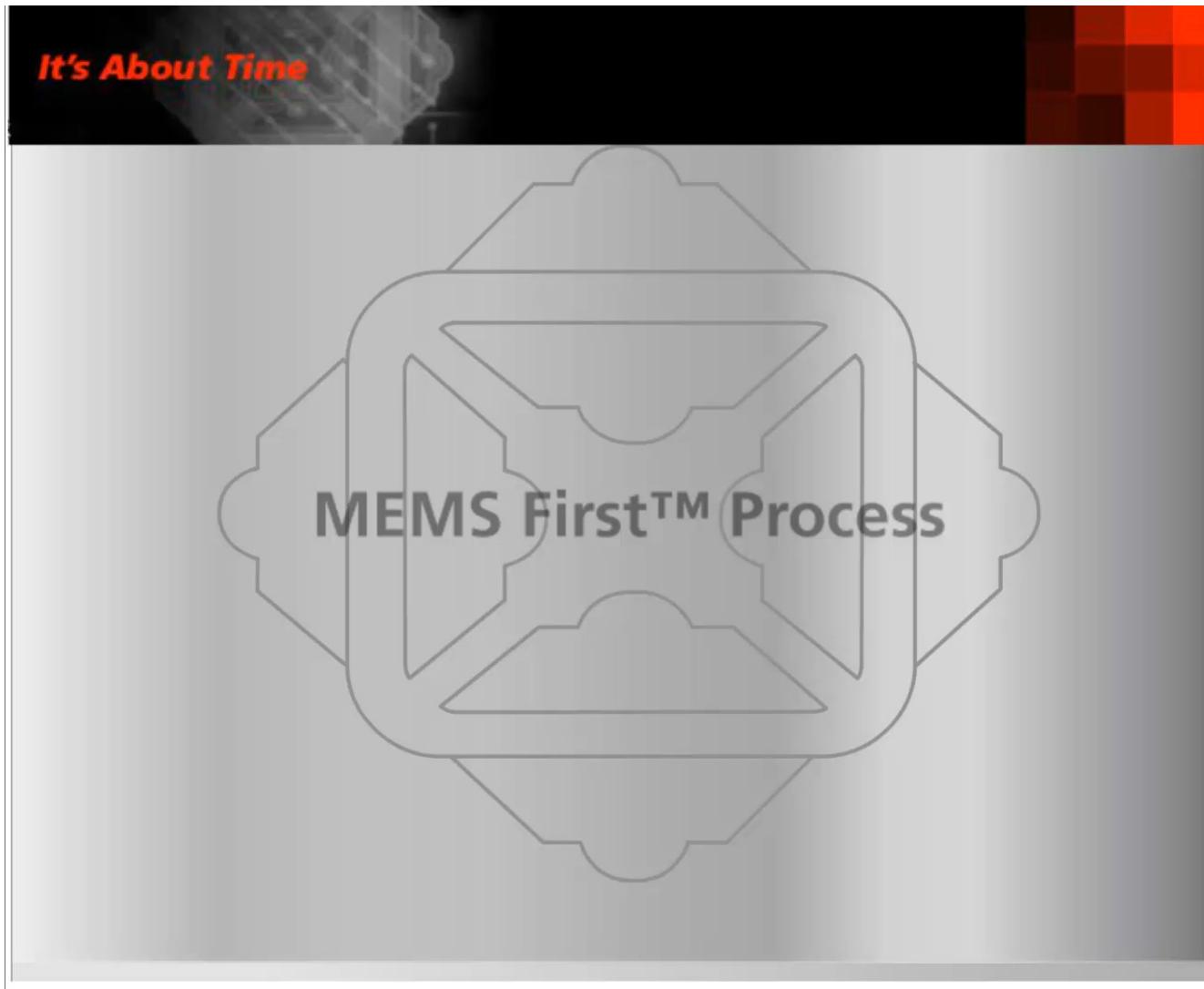


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 - $S_\phi(\delta f) = 10 \log \left(F \frac{k_B \cdot T \cdot f_0}{Q \cdot E} \frac{1}{\delta f^2} \right)$
 - Incomplete, needs some modifications/additions
- Specifications/Requirements
 - Depend on the *carrier frequency*
 - High frequencies can be divided
 - “Averages” $1/f^2$ noise
 - Great advantage of MEMS
 - High $FOM_1 = f_r \cdot Q$
- Phase noise is a very critical parameter because it cannot be filtered out or adjusted externally

GSM Requirements	
f_m	PN
kHz	dBc/Hz
200	≤ -118
400	≤ -124
600	≤ -127
800	≤ -130
1600	≤ -136
> 3200	≤ -141

[Q. Gu, Springer 2005]





- **What is a Resonator?**
- **Quality factor**
 - High or low?
 - What determines if it's high or low?
- **Why MEMS resonators?**
- **Types of MEMS resonators**
 - Frequency dependence on dimensions
 - Major application fields
- **MEMS filters (passive)**
 - What are the most important parameters to optimize?
- **MEMS oscillators (active)**
 - Why is phase noise important?
 - Why is T stability important and how is it achieved?

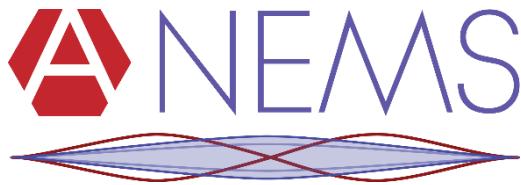
Advanced MEMS and Microsystems

Lecture 6 – NEMS

Prof. Guillermo Villanueva

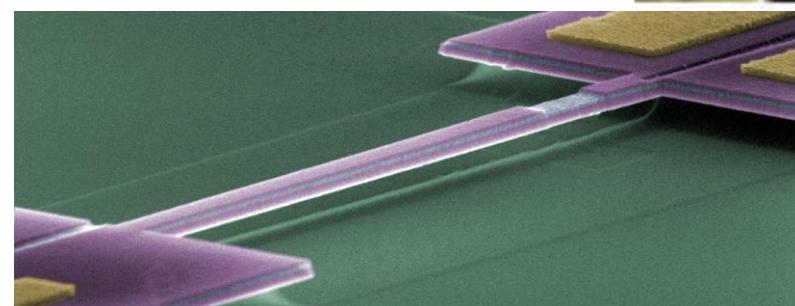
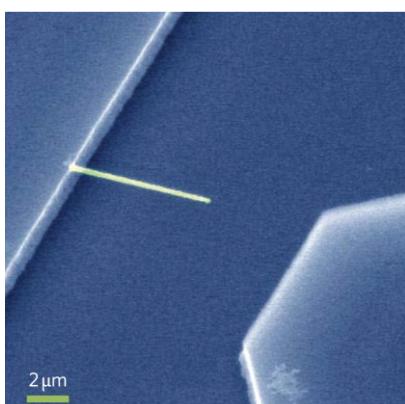
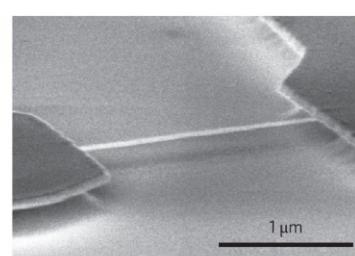
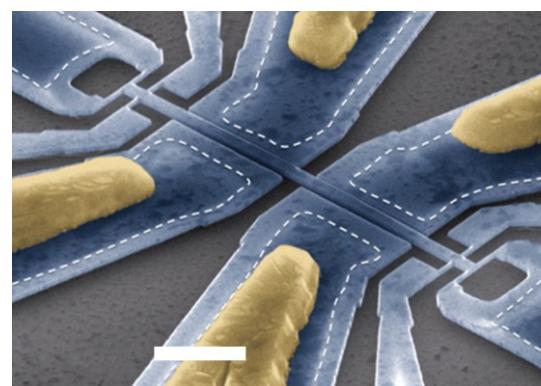
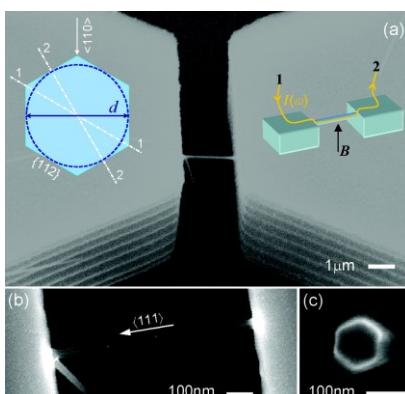
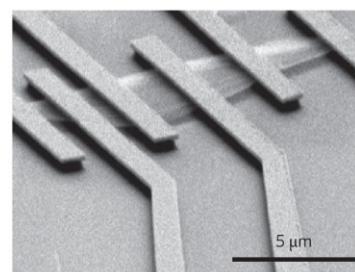
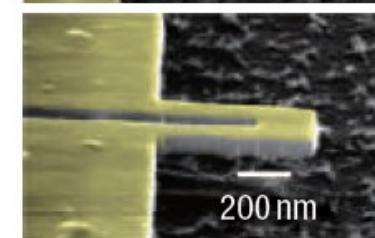
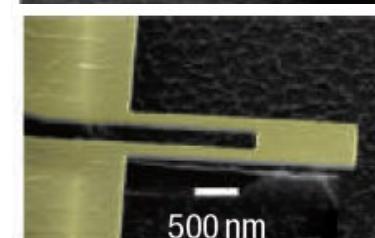
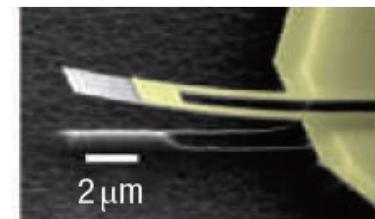
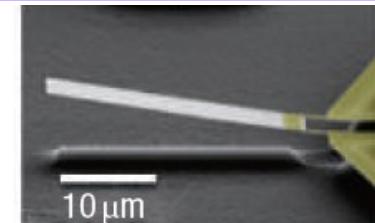
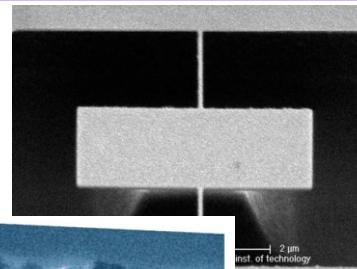
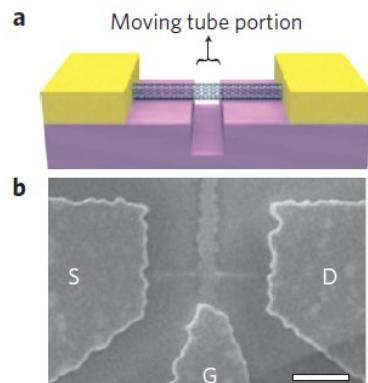
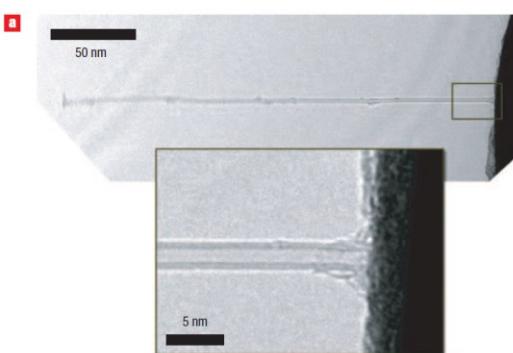
Advanced NEMS Lab (ANEMS)

EPFL-IGM NEMS

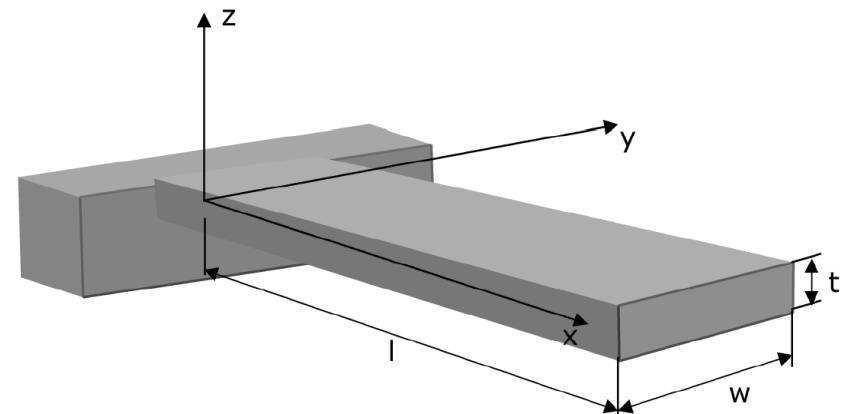


- **Introduction**
 - NEMS examples
 - NEMS definition(s)
 - Why NEMS?
 - NEMS Fabrication
 - Main challenges

NEMS examples



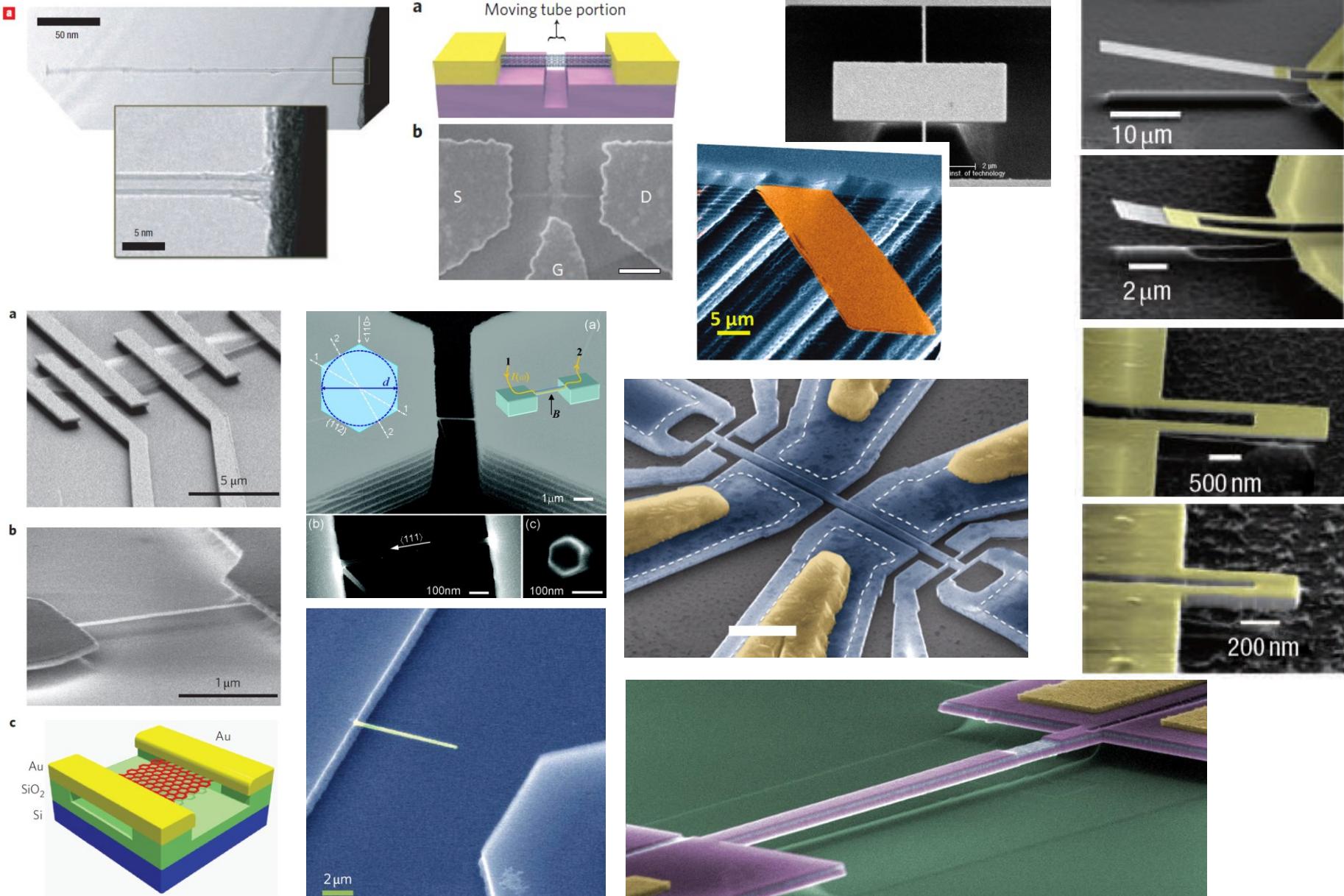
- NEMS tends to include “small MEMS”
- 1 possible definition
 - 2 out of 3 dimensions $\leq 1\mu\text{m}$
- But then...
 - What about graphene resonators?
 - Or extremely thin MEMS?

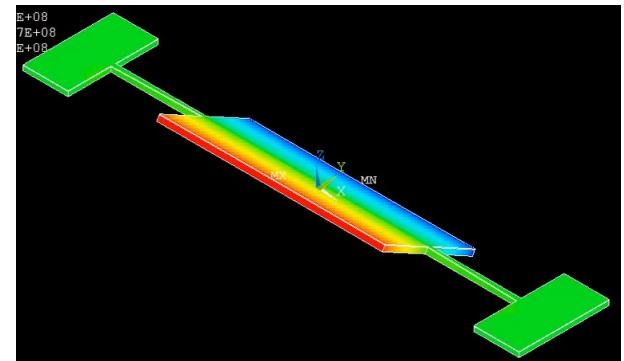
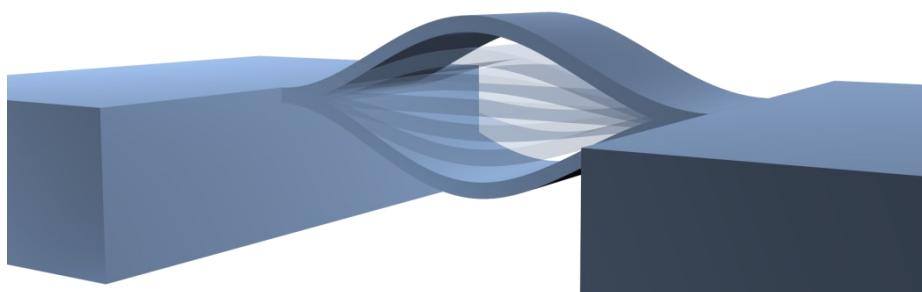
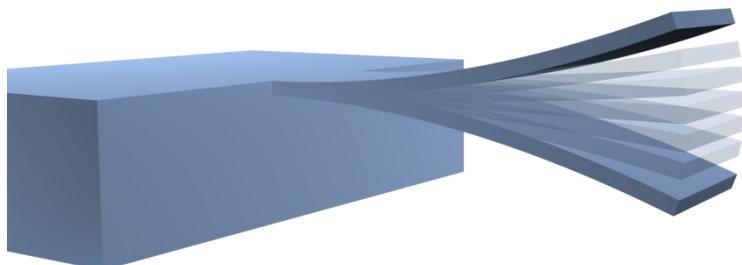


- Another possible definition – “mesoscopic system”
 - Referring to number of atoms in the mechanical device
 - Golden Gate – $\sim 10^{34}$ atoms
 - Trampoline – $\sim 10^{28}$ atoms
 - Guitar string – $\sim 10^{23}$ atoms
 - Macroscopic
 - MEMS accelerometer – $\sim 10^{16}$ atoms
 - Thin plate – $\sim 10^{12}$ atoms
 - Si-based NEMS – $\sim 10^{10}$ atoms
 - CNT – $\sim 10^5$ atoms
- Microscopic
- Mesoscopic

- **Top-Down**
 - Pushing down the dimensions of standard μ fab tools
 - EBL, DUV, NIL, Stencil, FIB – To improve the resolution of UV Lithography
 - Finer tuning of etching and deposition recipes
 - Smooth edges
 - Accurate thicknesses
 - Easy integration and connection to “macro” world
 - Very high cost to reduce dimensions
- **Bottom-up**
 - Direct growth/synthesis of structures
 - Highly based on chemical processes and reactions
 - CVD, VLS method, Arc-discharge...
 - Very cheap to produce millions of devices
 - Very difficult to integrate and connect them (eventually using top-down techniques)

NEMS examples





- Intuitive and clear understanding of motion
- Very low masses
- Very low stiffness

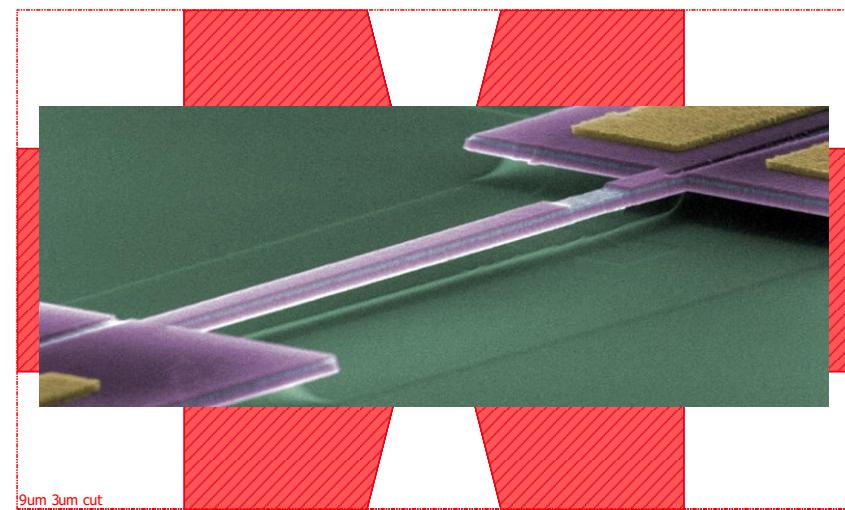
- **Size**
 - Higher level of integration
 - Very thin – good for stress-based sensing
- **Mass**
 - Low thermal mass – good for T or heat sensing
 - Low mass – good for detection of small mass landing
 - Gravity/Acceleration can be mostly neglected
- **Stiffness**
 - Low stiffness for a given frequency – good for Force sensing
- **Frequency**
 - High frequency – less influence from vibrations & faster measurement

- **Fabrication**

- **Expensive (top-down)**
 - **Difficult to contact (bottom-up)**
 - **Imperfections become (relatively) too large**
 - Surface roughness
 - Surface contaminants
 - Material defects
 - Grain boundaries
- 
 - **Low reproducibility**
 - **Mechanical properties deteriorate**
 - **Lower Q factors**

- **Measurement**

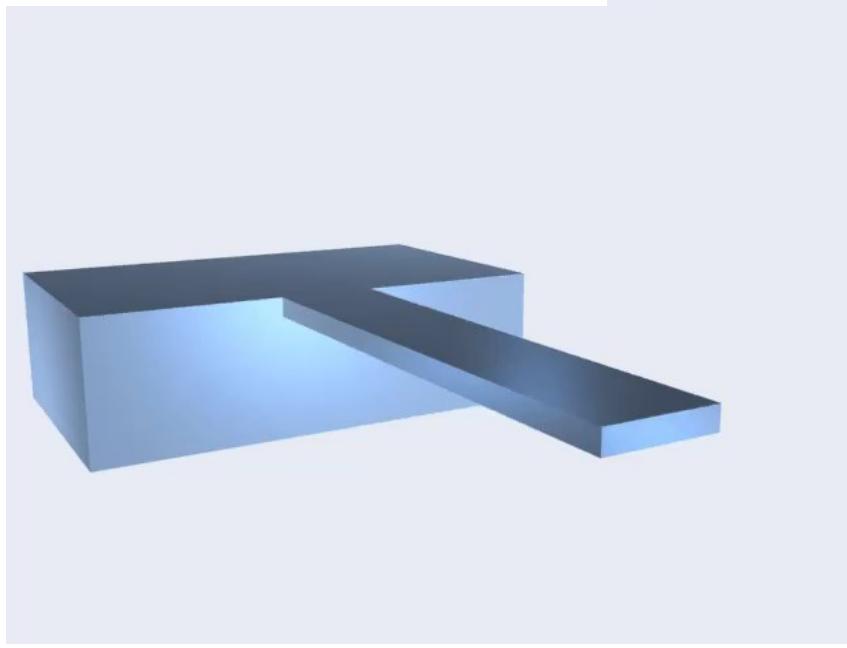
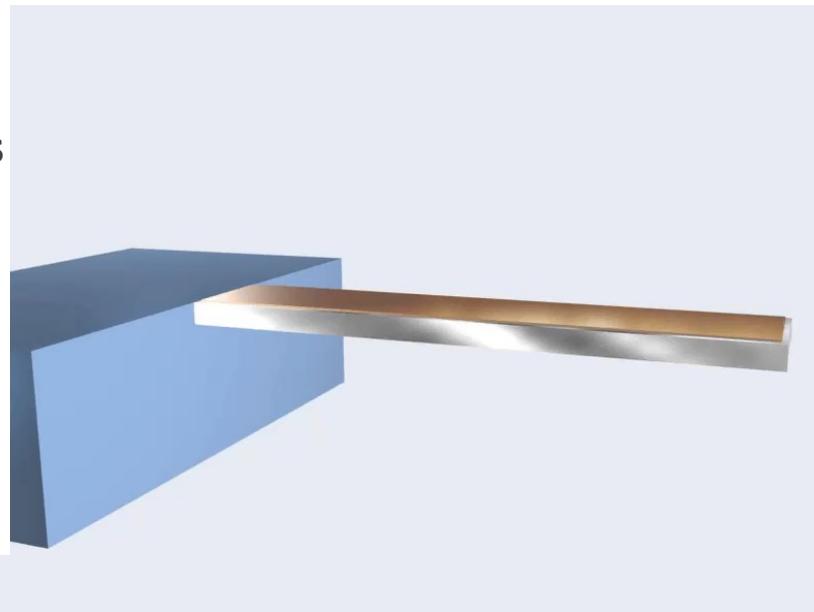
- Connection to “macro” world unavoidable
- Motional signal is “buried” in parasitics
- Very challenging to
 - Match impedance
 - Remove background
 - Amplify signal



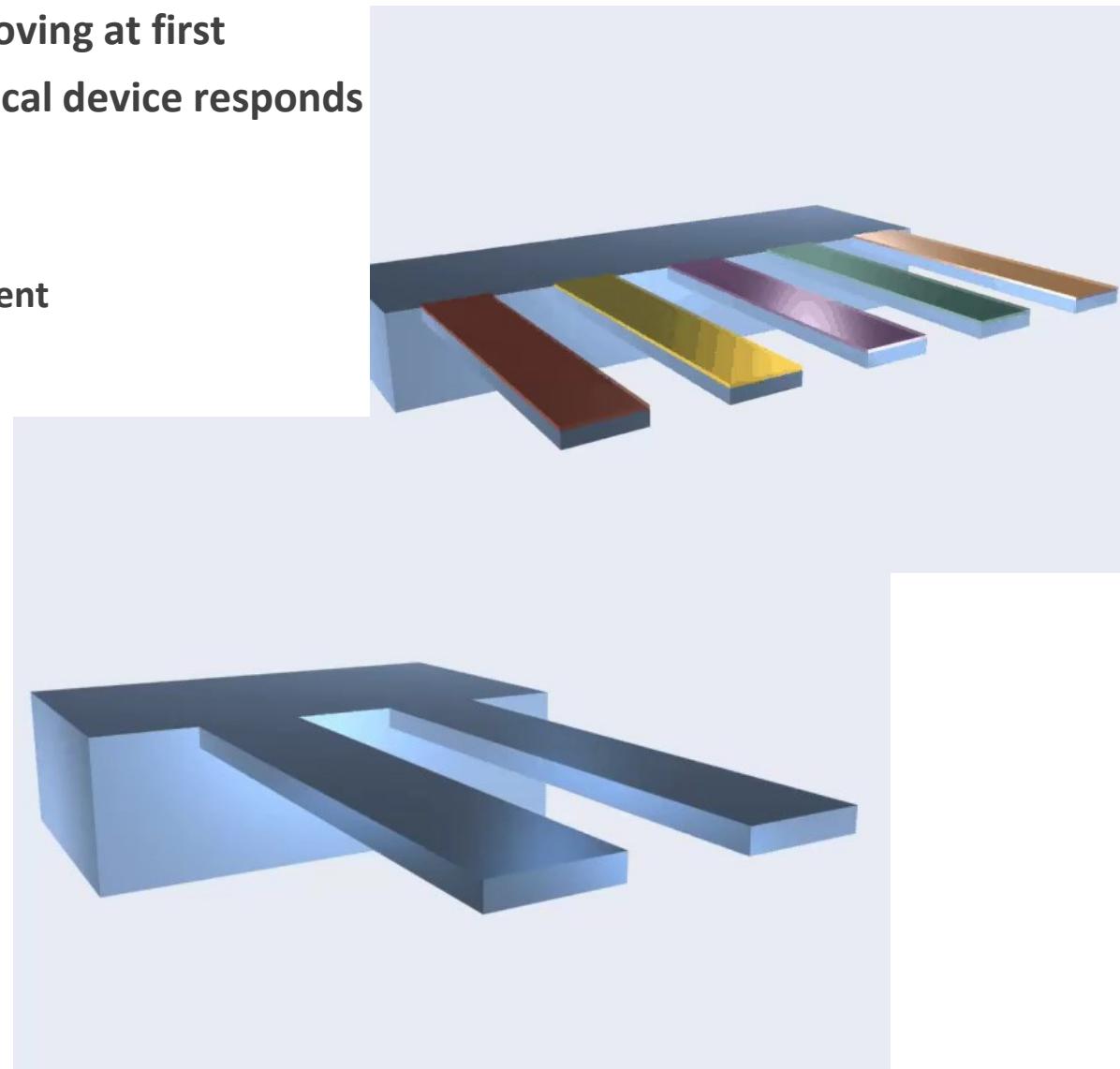
STATIC DETECTION

- Mechanical system is not moving at first
- Event happens and mechanical device responds

- Mechanical system is not moving at first
- Event happens and mechanical device responds
- Temperature
 - Thermal expansion gradient
- Gas sensor
 - T based

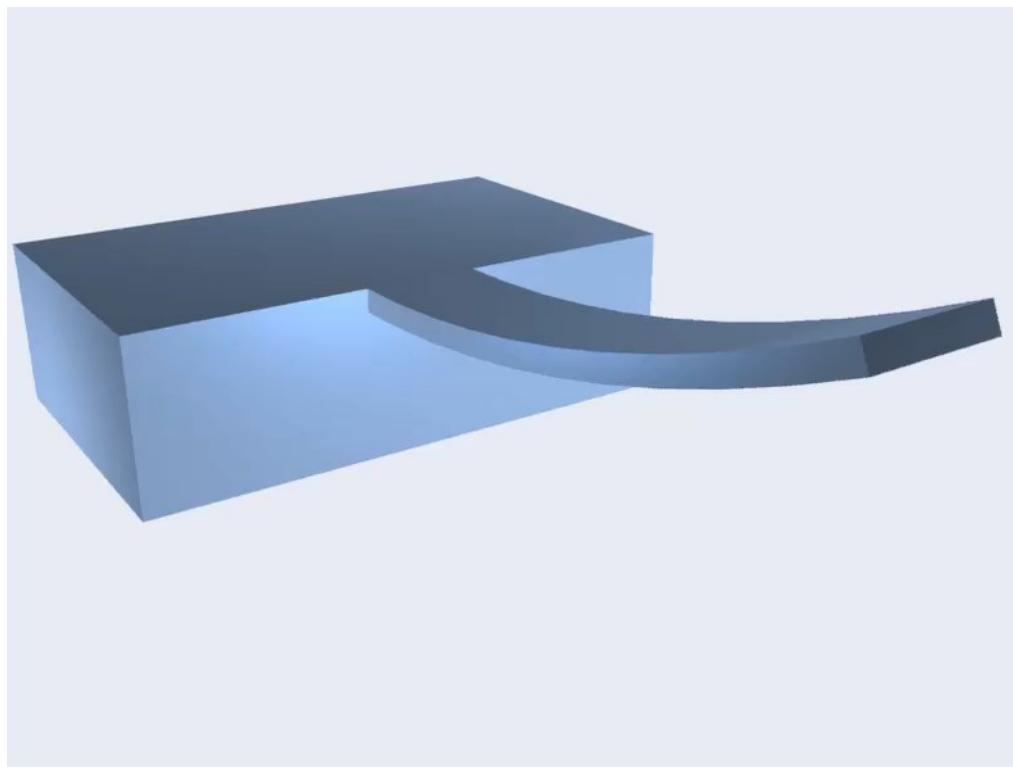
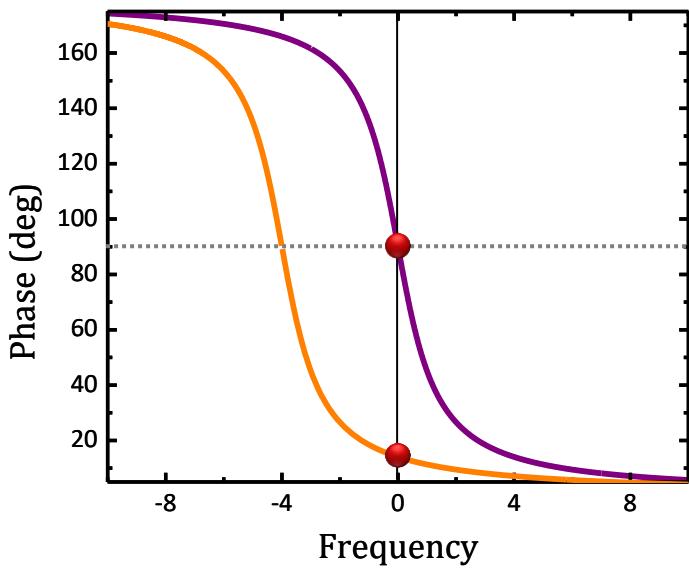


- Mechanical system is not moving at first
- Event happens and mechanical device responds
- Temperature
 - Thermal expansion gradient
- Gas sensor
 - T based
 - Surface stressed based
- Reference always needed



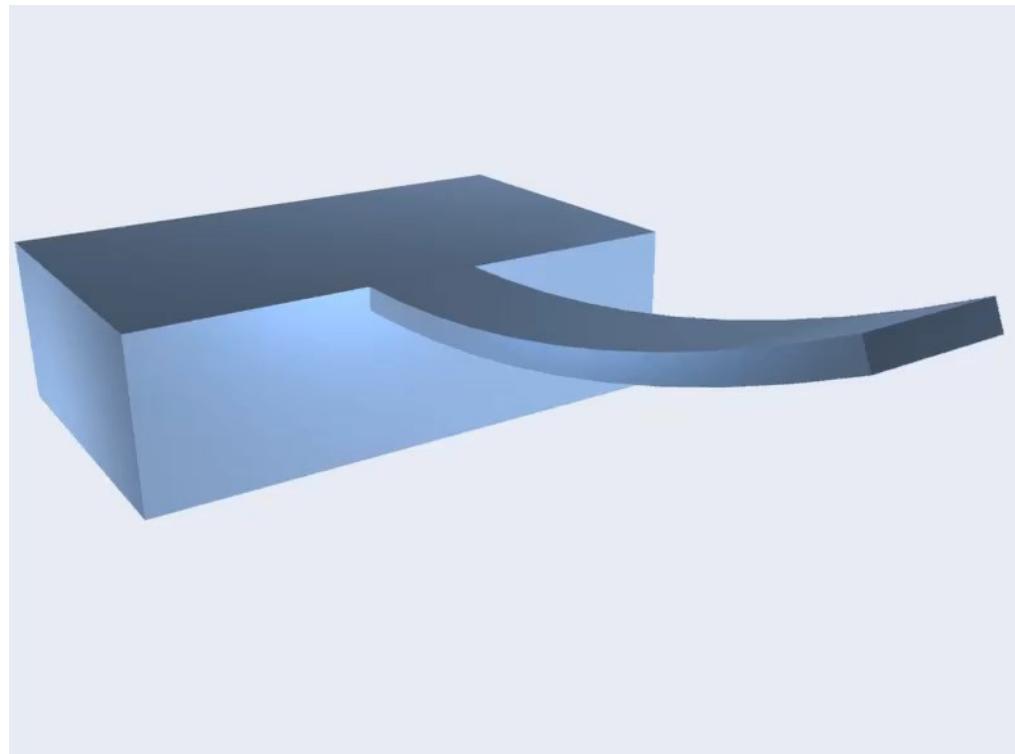
DYNAMIC DETECTION

- Mechanical system moving constantly
 - At or close to the resonance frequency
- Event happens and mechanical device responds
 - By changing its resonance frequency
- Frequency is the magnitude that is tracked
 - PLL or oscillator
 - Frequency counter



- Mechanical system moving constantly
 - At or close to the resonance frequency
- Event happens and mechanical device responds
 - By changing its resonance frequency
- Frequency is the magnitude that is tracked
 - PLL or oscillator
 - Frequency counter
- Mass
 - Deposition or removal of material
 - Gases, mass spectrometry
- Material properties
- Temperature
- Stiffness
- Stress

Noise in frequency determines device performance



- Why NEMS?
- Static & dynamic sensing
 - How do they work in general?
 - What are the main differences between NEMS and MEMS?
 - Why is it interesting to go to NEMS?
 - Examples
 - What is most important?
 - How to build a better sensor?